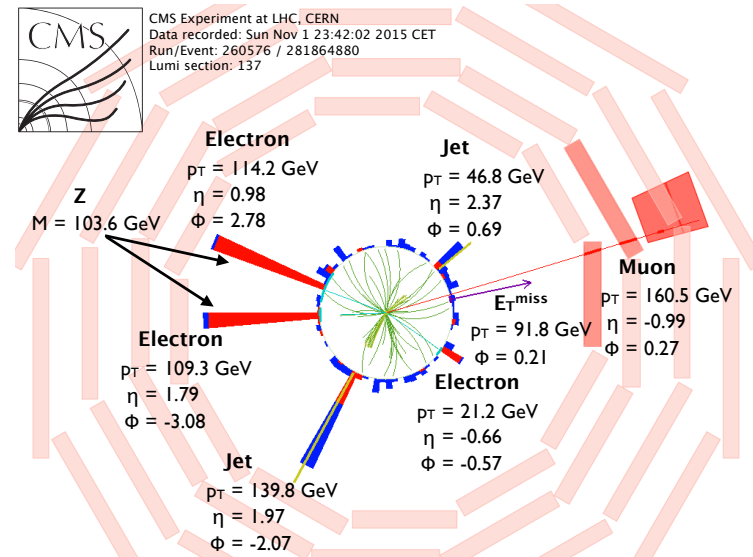


Top Quark Physics

Efe Yazgan

CMS Experiment, CERN

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Hadron Collider School – HASCO 2016

Georg-August-Universität, Göttingen, Germany

19-24 July 2016

Three Generations of Matter (Fermions)

	I	II	III	
mass →	2.4 MeV/c ²			0
charge →	2/3			0
spin →	1/2			1
name →	u up			γ photon
Quarks	4.8 MeV/c ² -1/3 1/2 d down	104 MeV/c ² -1/3 1/2 s strange		
	<2.2 eV/c ² 0 1/2 ν _e electron neutrino	<0.17 MeV/c ² 0 1/2 ν _μ muon neutrino		
	0.511 MeV/c ² -1 1/2 e electron	105.7 MeV/c ² -1 1/2 μ muon		
Leptons				

Gauge Bosons

Progress of Theoretical Physics, Vol. 49, No. 2, February 1973

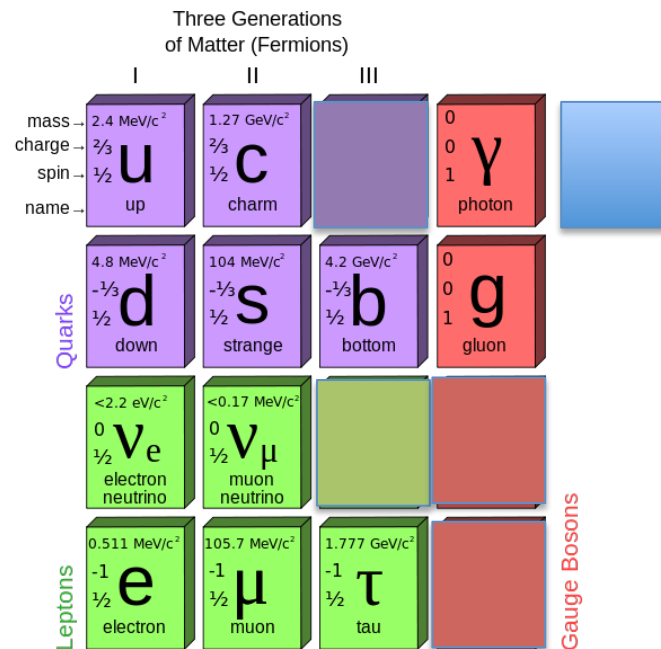
Makoto KOBAYASHI and Toshihide MASKAWA

(Received September 1, 1972)

2

Standard Model in 1978

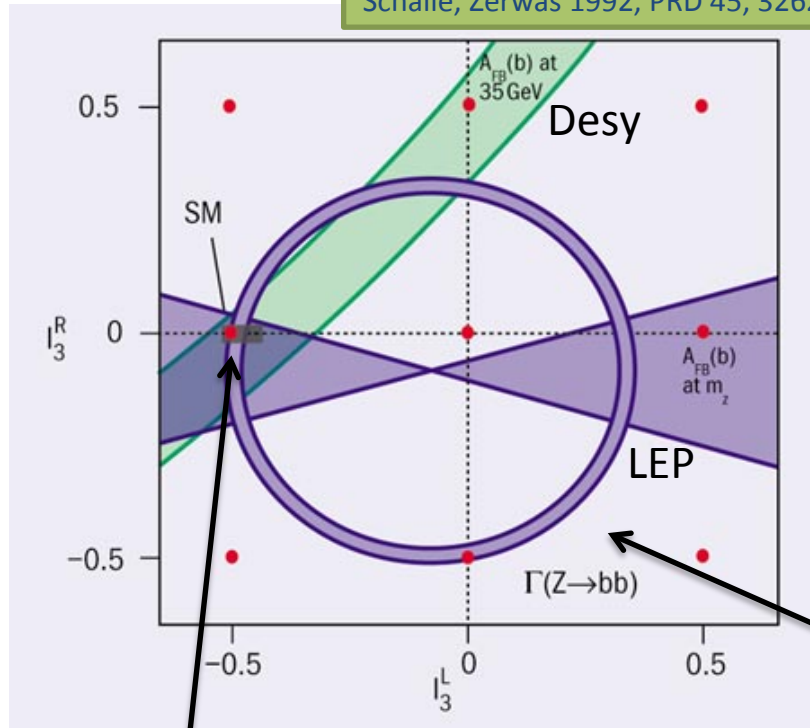
- b-quark discovered ('77) and its iso-spin is measured.
- To complete the third generation $\rightarrow$ the weak isospin partner of the b-quark.



Weak Isospin of b Quark and its Partner

Schaile, Zerwas 1992, PRD 45, 3262

(right handed b-quark)



(left handed b-quark)

$V \rightarrow$ vector coupling

$A \rightarrow$ Axial coupling

If V_e, A_e known

$\rightarrow$ Extract couplings of the b-quark using A_{FB} and Γ measurements.

$$A_{FB}^{m_Z}(b) = \frac{3}{4} \frac{2V_e A_e}{V_e^2 + A_e^2} \frac{2V_b A_b}{V_b^2 + A_b^2}$$

$$\Gamma(Z \rightarrow b\bar{b}) = \frac{G_F M_Z^3}{2\sqrt{2}\pi} (V_b^2 + A_b^2)$$

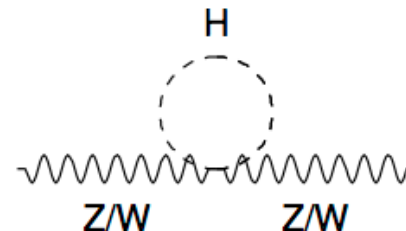
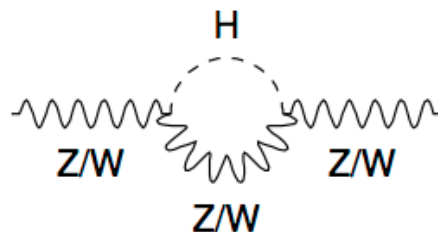
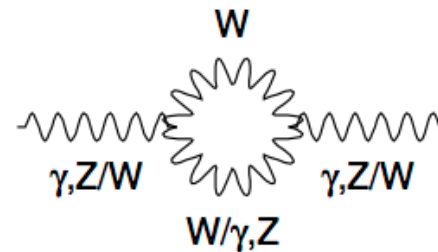
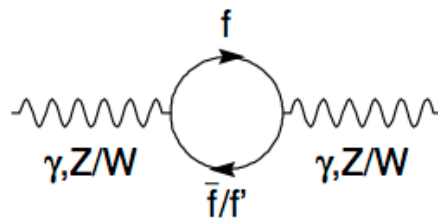
All measurements meet at:

$$[I_3^L, I_3^R] = [-1/2, 0]$$

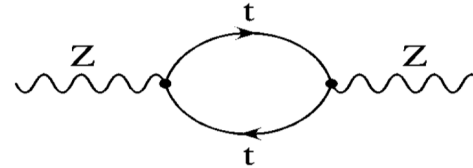
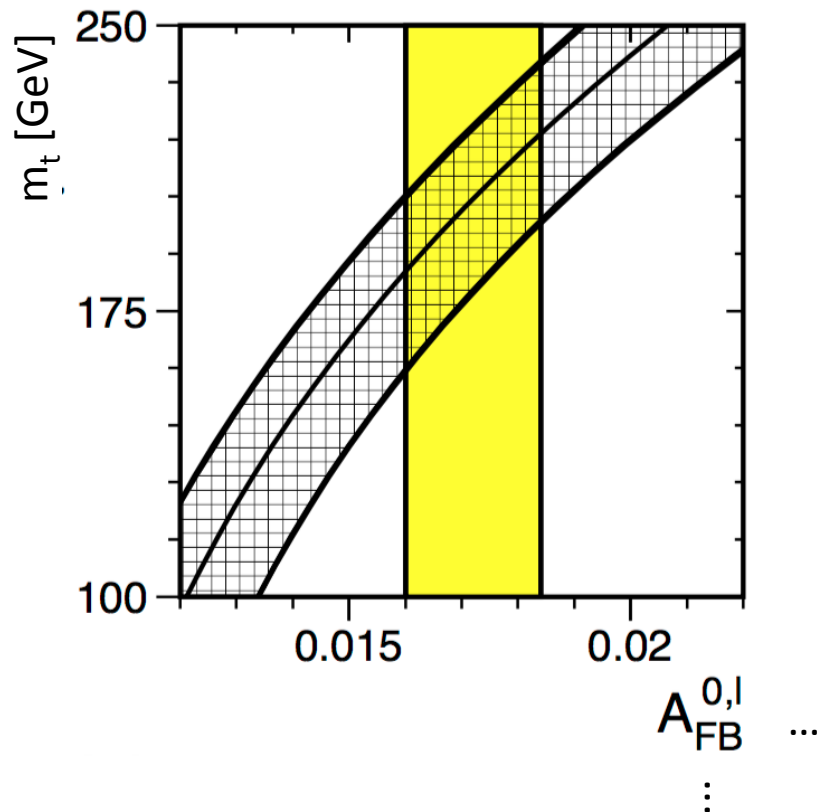
$\rightarrow$ Isospin partner with
 $[I_3^L, I_3^R] = [+1/2, 0]$ should exist.

Quantum Fluctuations Seeing Invisible Particles

- Heisenberg uncertainty principle implies
 - Particles can be created from nothing (for a short period of time) w/o the necessary energy supply (virtual or off-mass-shell particle).
- Tree level SM processes modified by radiative corrections.
- Indirect effect of the top quark (and Higgs) observable
 - even if the collider energy is not sufficient to create the real particle.



Top Quark's Effect at $\sqrt{s} \approx 100 \text{ GeV} < m_t$

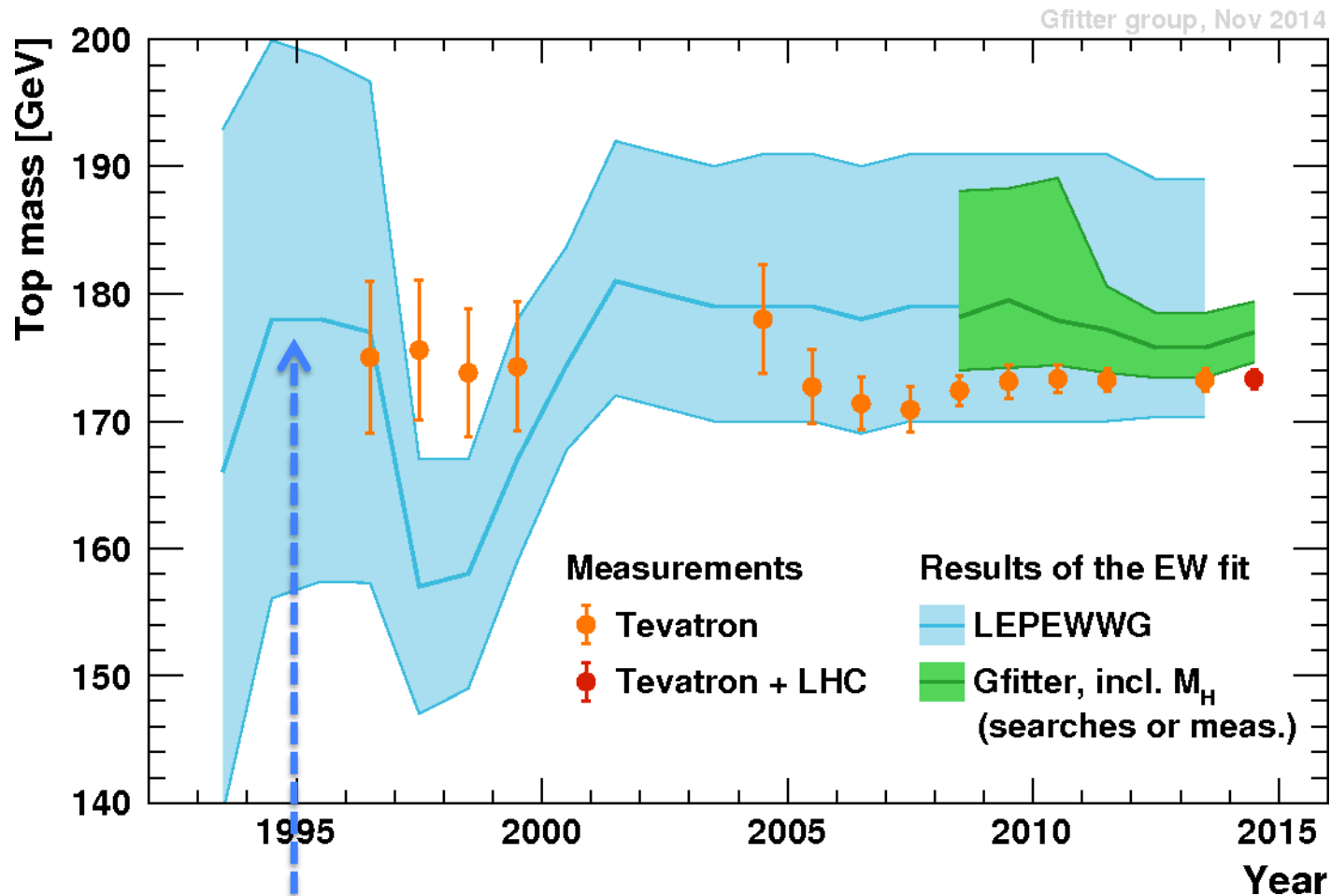


LEP 1 prediction:

$$m_t = 173_{-10}^{+13} \text{ GeV}$$

LEP Collaborations CERN-PPE/95-172

One of the most critical tests of the standard model!

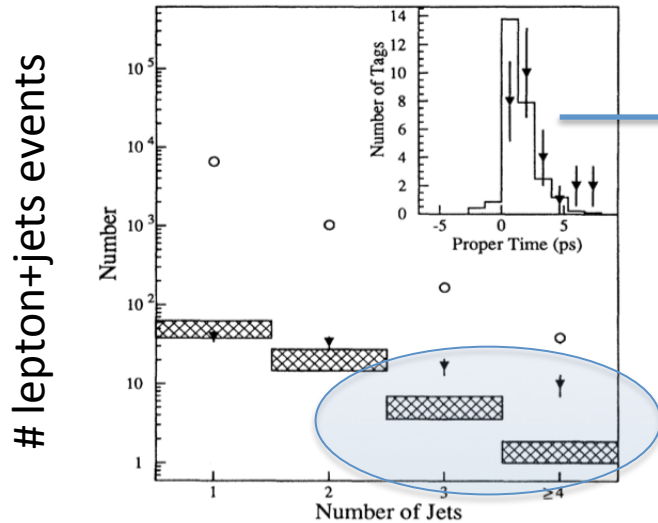


- Indirect measurements showed the existence of the top quark and predicted its mass precisely before it was discovered.

The Discovery of the Top Quark at the Tevatron

with $O(10)$ events.

CDF, PRL 74, 2626 (1995)

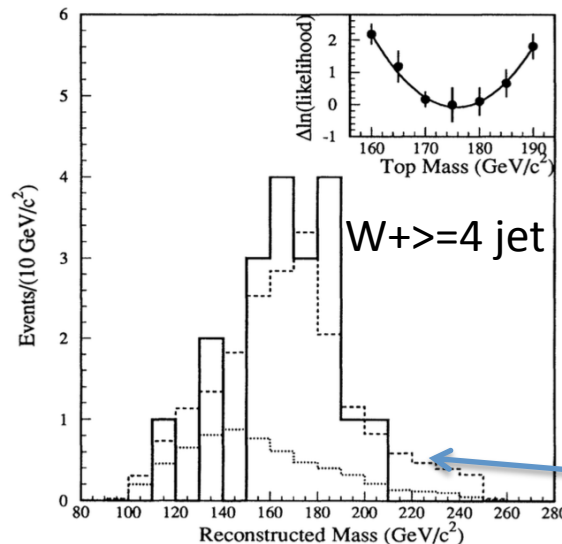


Decay lifetime of secondary vertex tags for $W^+ \geq 3$ jet events.

→ Consistent with the prediction for b decays from $t\bar{t}$ simulation.

Signal consistent with $t\bar{t} \rightarrow W^+ b W^- \bar{b}$ and inconsistent w/ the background prediction.

Circles:
Before b-tagging



$$\sigma_{t\bar{t}}^{CDF}(\sqrt{s} = 1.8 \text{ TeV}) = 6.8^{+3.6}_{-2.4} \text{ pb}$$

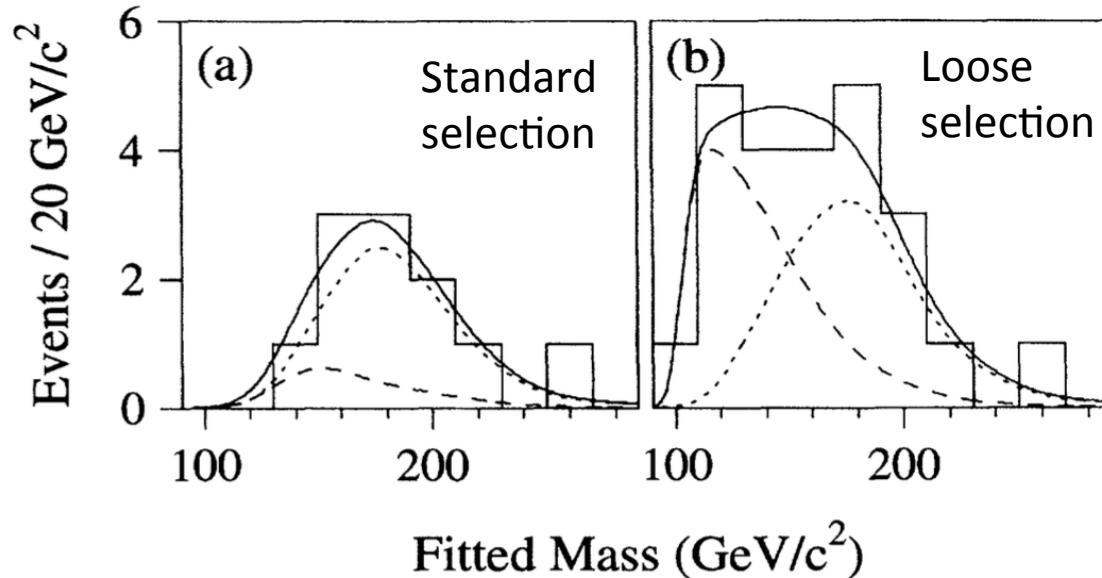
$$m_t^{CDF} = 176 \pm 8(\text{stat.}) \pm 10(\text{syst.}) \text{ GeV}$$

Dashed:
Background+ $t\bar{t}$ simulation

The Discovery of the Top Quark at the Tevatron

D0, PRL 74, 2632 (1995)

with $O(10)$ events.



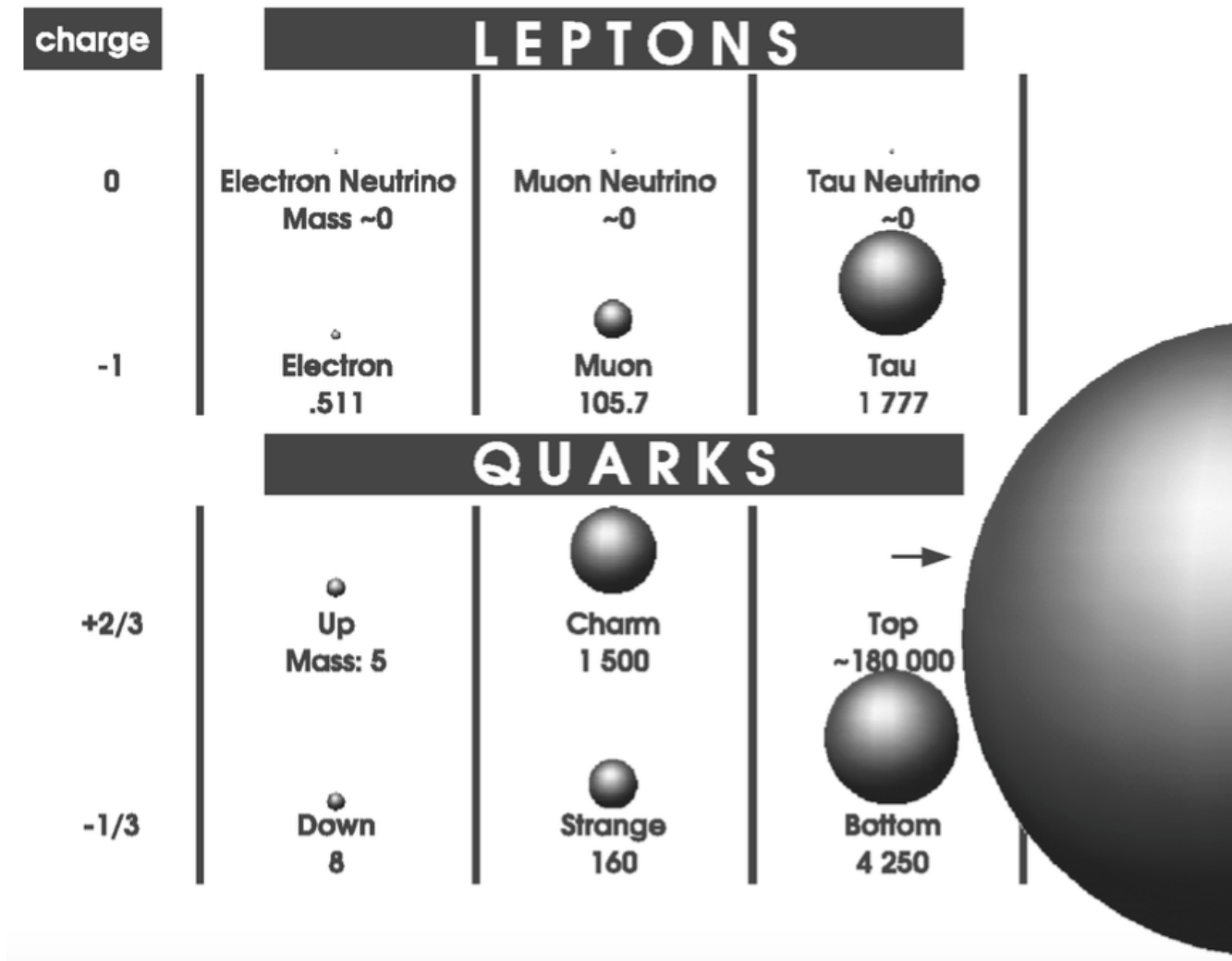
Signal consistent with
 $t\bar{t} \rightarrow W^+ b W^- \bar{b}$
and inconsistent w/ the
background prediction.

$$\sigma_{t\bar{t}}^{D0}(\sqrt{s} = 1.8 \text{ TeV}) = 6.4 \pm 2.2 \text{ pb}$$

$$m_t^{D0} = 199_{-21}^{+19}(\text{stat.}) \pm 22(\text{syst.}) \text{ GeV}$$

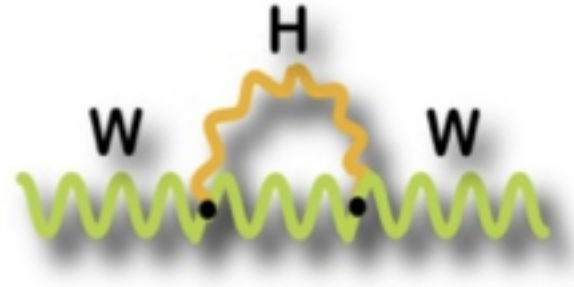
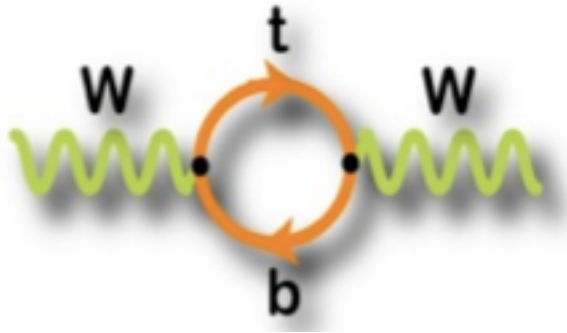
The Top Quark

- The most massive particle known to date ($m_t \sim 173 \text{ GeV}$).



Quantum Fluctuations → Higgs Boson

e.g.



HW: Read the Nobel lectures of 't Hooft and Veltman (1999)

$$\Delta\rho = (\rho - 1) \propto m_t^2$$

Propagator for fermions $\propto 1/q$
(Dirac equation)

$$\Delta\rho \propto \ln(m_H)$$

Propagator for boson $\propto 1/q^2$
(Klein-Gordon equation)

$$M_W^2 = \rho \left(M_W^{tree-level} \right)^2 \quad \text{w/} \quad \rho = 1 + \Delta\rho_t + \Delta\rho_H$$

Veltman,
NPB 123, 89 (1977)

$$\Delta\rho_t \sim G_F m_t^2$$

$$\Delta\rho_H \sim G_F m_W^2 \log \frac{m_H^2}{m_W^2}$$

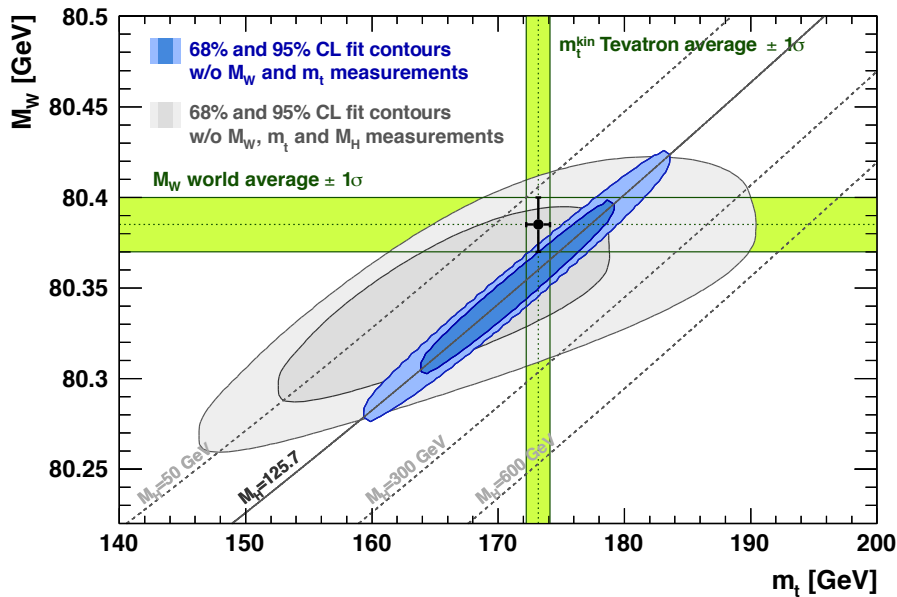
Precision Measurements of Top and W → Higgs

Electroweak fit before
Higgs discovery:

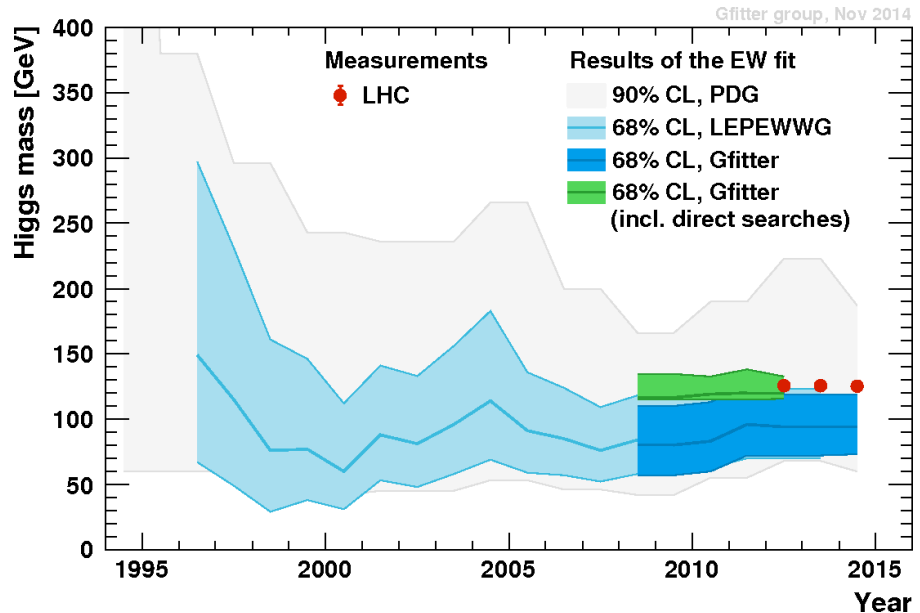
$$m_H = 94^{+25}_{-22} \text{ GeV}$$

consistent with measured m_H within 1.3σ .

The Gfitter Group, M. Baak et al., EPJC 72, 2205 (2012)



<http://project-gfitter.web.cern.ch/project-gfitter/History/>

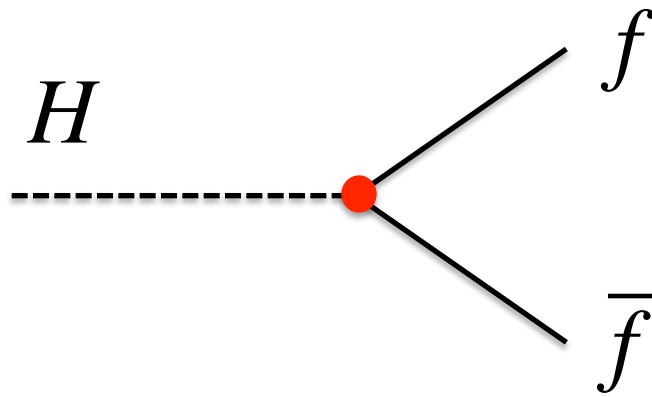


Quantum fluctuations showed the existence of the Higgs boson and predicted its mass precisely before it was discovered.

The most critical test of the standard model!

Top Quark Yukawa Coupling

The largest among the fermions – special role in electroweak symmetry breaking?

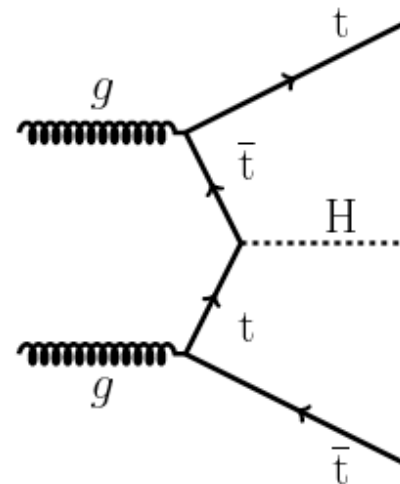
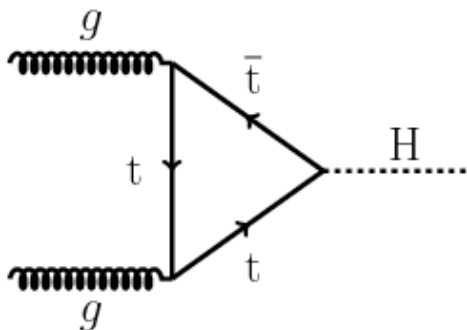


$$y_t = \frac{\sqrt{2}m_t}{v} \cong 1$$

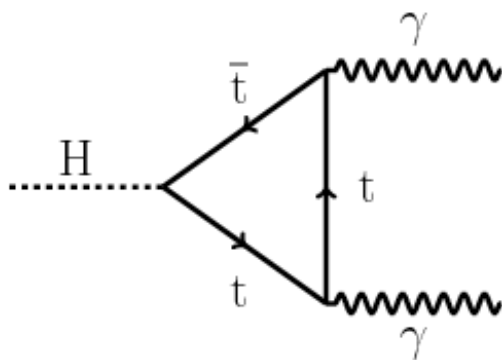
→ Top-Higgs boson coupling hasn't been directly measured yet.

Top – Higgs Coupling

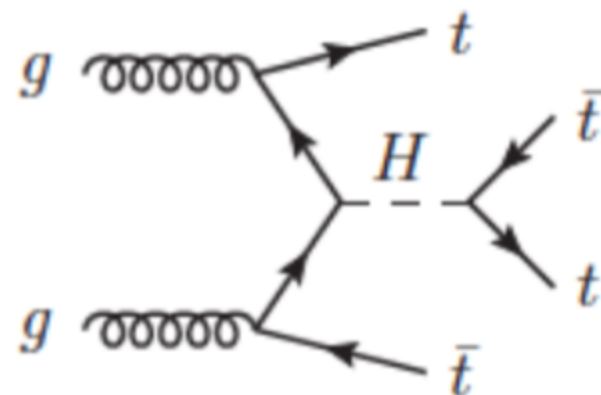
Test fermion mass generation



$t\bar{t}H$



Indirect



Four-top

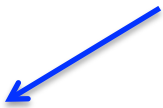
direct

Top Quark Properties

- Top quark has a very short lifetime

$$\tau_t = \frac{1}{\Gamma_t} \sim 0.5 \times 10^{-24} s < \frac{1}{\Lambda_{QCD}} < \frac{m_t}{\Lambda_{QCD}^2} \sim 3 \times 10^{-21} s \ll \tau_b \sim 10^{-12} s$$
$$\tau_t < \tau(\text{hadronization}) < \tau(\text{spin-decorrelation}) \ll \tau_b$$

Λ_{QCD} :
→ scale for which α_s becomes very strong
→ ~1 fm scale of a hadron (proton radius)



No hadronic bound states



Spin effects propagate to decay products.

→ Behaves like a bare quark

→ Top quark properties “directly” accessible (mass, V_{tb} , spin, charge, y_t , ...)

Top Properties

Citation: K.A. Olive *et al.* (Particle Data Group), Chin. Phys. C, **38**, 090001 (2014) and 2015 update



$$I(J^P) = 0(\frac{1}{2}^+)$$

$$\text{Charge} = \frac{2}{3} e \quad \text{Top} = +1$$

Mass (direct measurements) $m = 173.21 \pm 0.51 \pm 0.71 \text{ GeV}$ [a,b]

Mass ($\overline{\text{MS}}$ from cross-section measurements) $m = 160^{+5}_{-4} \text{ GeV}$ [a]

Mass (Pole from cross-section measurements) $m = 174.6 \pm 1.9 \text{ GeV}$

$m_t - m_{\bar{t}} = -0.2 \pm 0.5 \text{ GeV}$ (S = 1.1)

Full width $\Gamma = 1.41^{+0.19}_{-0.15} \text{ GeV}$ (S = 1.4)

$\Gamma(Wb)/\Gamma(Wq(q=b, s, d)) = 0.957 \pm 0.034$ (S = 1.5)

t-quark EW Couplings

$$F_0 = 0.690 \pm 0.030$$

$$F_- = 0.314 \pm 0.025$$

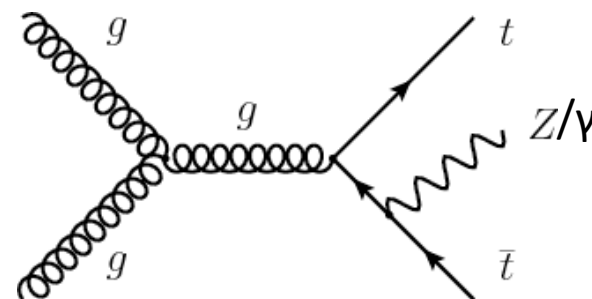
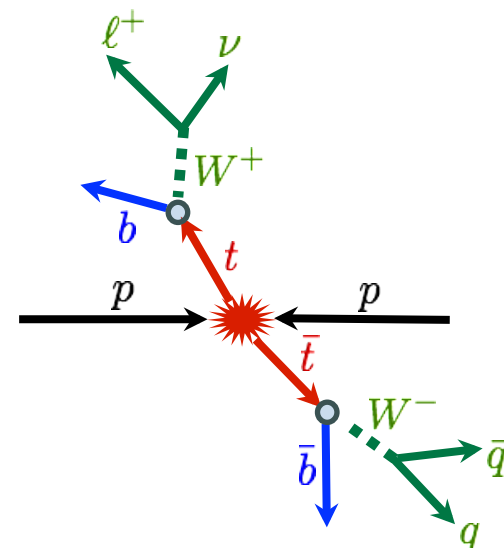
$$F_+ = 0.008 \pm 0.016$$

$$F_{V+A} < 0.29, \text{ CL} = 95\%$$

t DECAY MODES	Fraction (Γ_i/Γ)	Confidence level	P (MeV/c)
$t \rightarrow Wq(q=b, s, d)$			—
$t \rightarrow Wb$			—
$t \rightarrow \ell \nu_\ell$ anything	[c,d] $(9.4 \pm 2.4) \%$		—
$t \rightarrow \gamma q(q=u, c)$	[e] $< 5.9 \times 10^{-3}$	95%	—

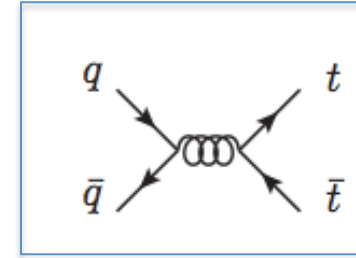
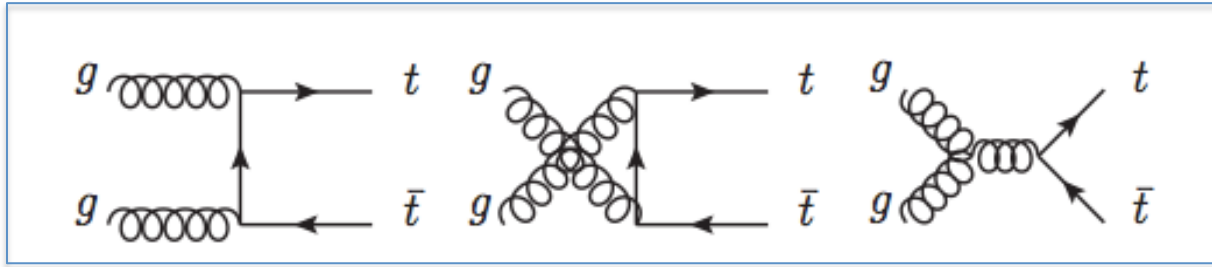
$\Delta T = 1$ weak neutral current (T1) modes

$t \rightarrow Zq(q=u, c)$	T1	[f] $< 5 \times 10^{-4}$	95%	—
$t \rightarrow Hq$		$< 5.6 \times 10^{-3}$	95%	—
$t \rightarrow \ell^+ \bar{q} q'(q=d, s, b; q'=u, c)$		$< 1.6 \times 10^{-3}$	95%	—



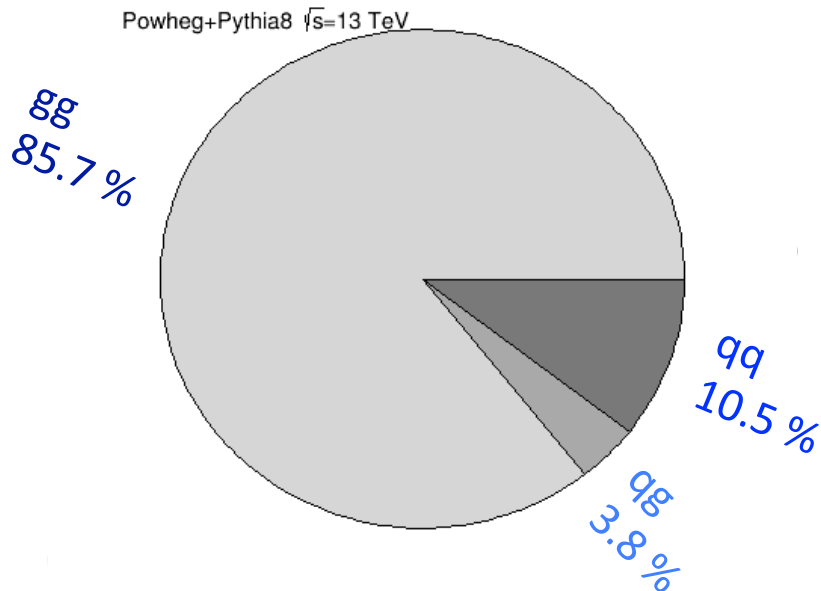
+ Cross sections, asymmetries, spin correlation, ...

Top pair production through QCD interactions.



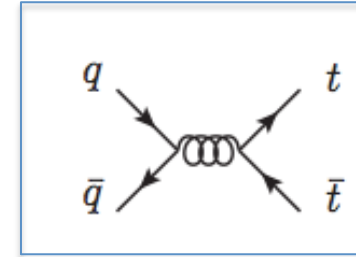
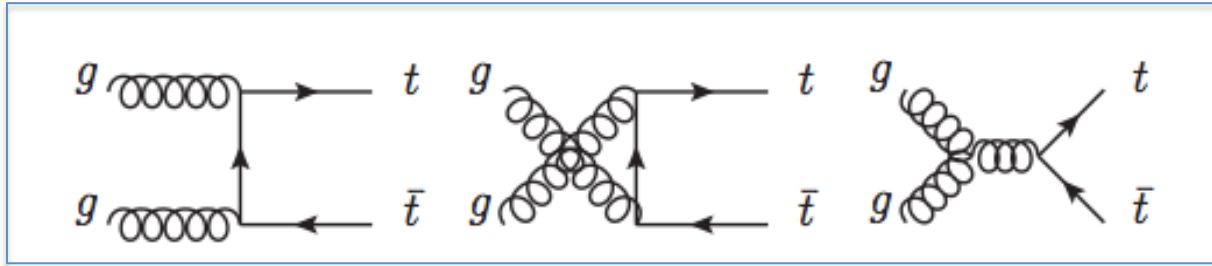
$$\sigma(t\bar{t}) \sim 830 \text{ pb @ } 13 \text{ TeV}$$

$$\sigma_{t\bar{t}}^{13\text{TeV}} \sim 3 \times \sigma_{t\bar{t}}^{8\text{TeV}}$$



- Sensitive to PDFs, α_s , m_t
- Backgrounds to Higgs and many new physics searches

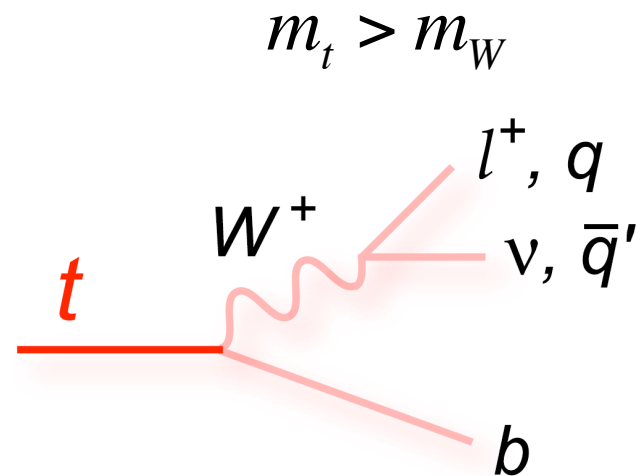
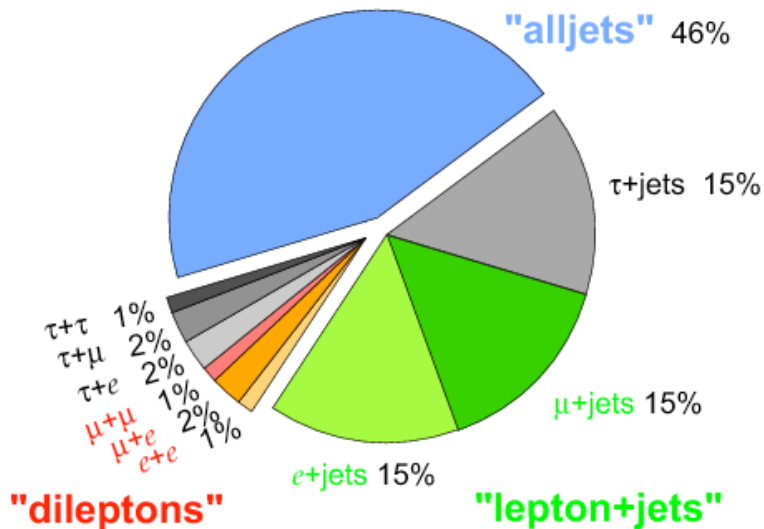
Top pair production through QCD interactions.



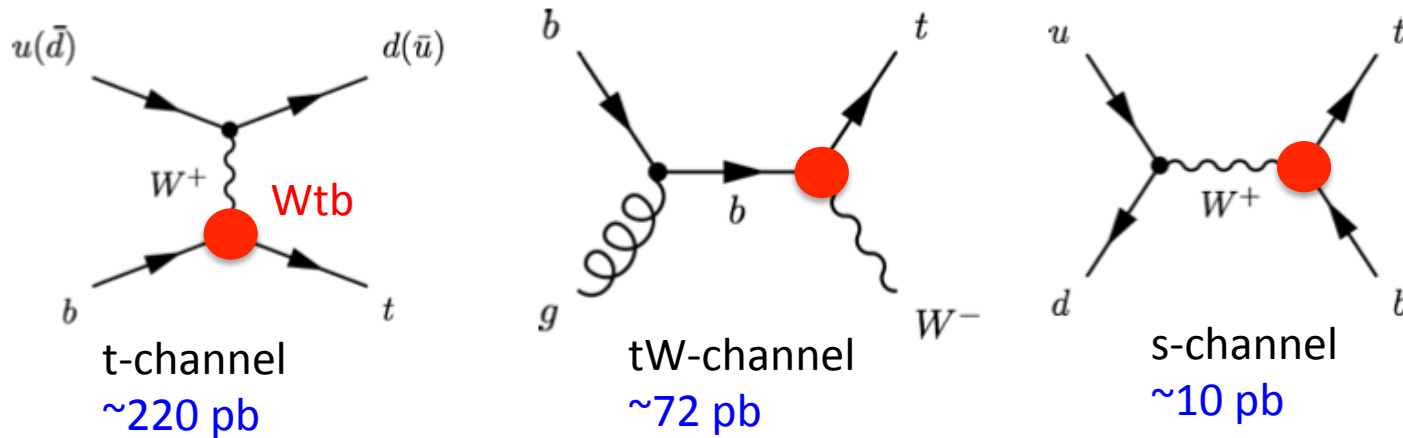
$$\sigma(t\bar{t}) \sim 830 \text{ pb @ } 13 \text{ TeV}$$

$$\sigma_{t\bar{t}}^{13\text{TeV}} \sim 3 \times \sigma_{t\bar{t}}^{8\text{TeV}}$$

Top Pair Branching Fractions



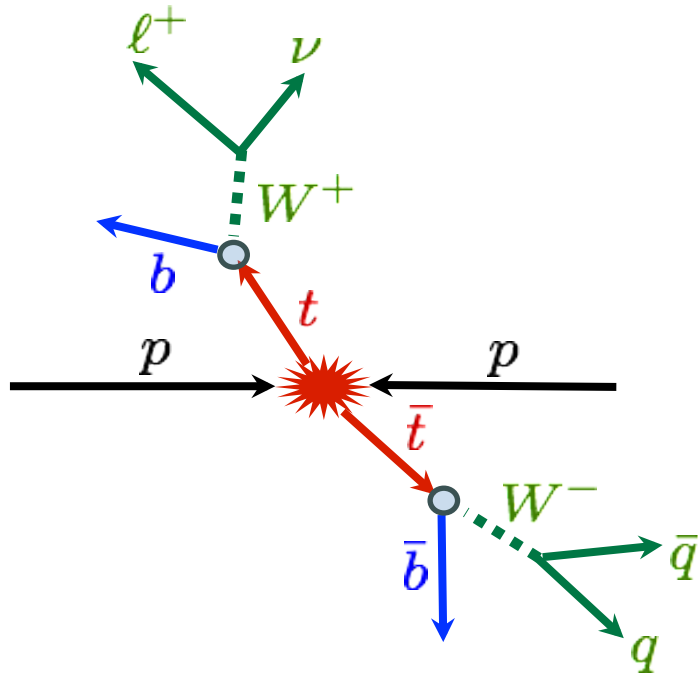
Electroweak single top production



$$\sigma_{t\text{-chan}}^{13\text{TeV}} \sim 2.5 \times \sigma_{t\text{-chan}}^{8\text{TeV}}$$

- Sensitive to Wtb vertex (V-A coupling), b- and u/d-PDFs.
 - ◆ V-A coupling: cross sections, W boson and top quark polarizations.
- Backgrounds to Higgs and many searches

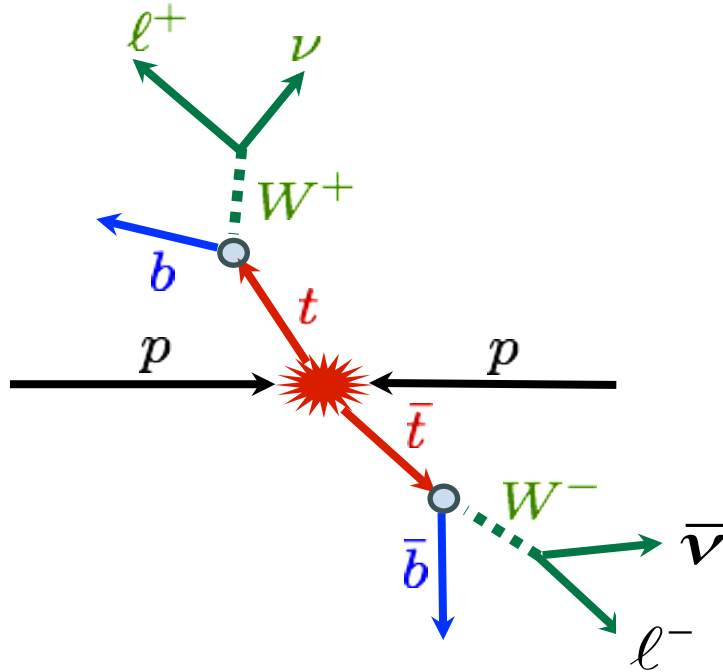
Top Quark Signatures and Backgrounds



- Lepton+jets channel
 - ◆ A high p_T lepton
 - ◆ ≥ 4 high p_T jets (2 of which are jets from b -decays)
 - ◆ Missing transverse energy

- Main backgrounds:
 - ◆ $t\bar{t}$ other, Single top, W +jets

Top Quark Signatures and Backgrounds



■ Dilepton channel

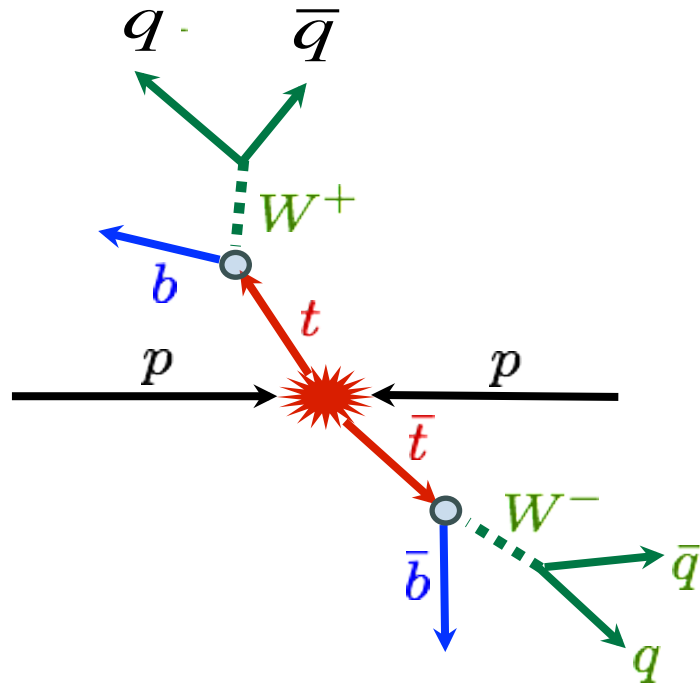
- ◆ Two high p_T leptons
- ◆ ≥ 2 high p_T jets (2 of which are from b-decays)
- ◆ Missing transverse energy

■ Main backgrounds:

- ◆ $t\bar{t}$ other
- ◆ Single top
- ◆ W/Z +jets

- Fewer number of events
- But purer
- Best channel: $e\mu$

Top Quark Signatures and Backgrounds



- Main backgrounds:
 - ◆ QCD multijets

- All-hadronic channel
 - ◆ ≥ 6 high p_T jets (2 of which are from b-decays)
 - Possible to fully reconstruct the event (i.e. no neutrinos)
 - But larger uncertainties compared to other channels due to multiple jets
 - Jet energy scale and b-tagging.

~Plan for the Lectures

- Top quark production and Event Modelling
- Boosted top
- Questions & Break
- Top quark mass measurements
- Asymmetry measurements
- $t\bar{t}$ spin Correlation
- Top quark couplings
- Questions

Example results/plots taken from top quark public pages of Tevatron and LHC experiments (**experimental view and most examples from CMS**):

ATLAS: <https://twiki.cern.ch/twiki/bin/view/AtlasPublic/TopPublicResults>

CMS: <https://twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResultsTOP>

CDF: <http://www-cdf.fnal.gov/physics/new/top/top.html>

D0: http://www-d0.fnal.gov/Run2Physics/top/top_public_web_pages/

Cross section Extraction

Total Inclusive cross section

→ count signal events:


$$\sigma = \frac{N_{obs} - N_{bkg}}{(A \times \varepsilon) \times B \times L}$$

A: Acceptance (depends on PDF, and other modeling uncertainties, e.g. renormalization and factorization scales)

ε : Selection efficiency for events in acceptance
(affected by the errors in triggers and reconstruction)

L: Integrated luminosity

B: Branching ratio

Cross section Extraction

Total Inclusive cross section

→ count signal events:


$$\sigma = \frac{N_{obs} - N_{bkg}}{(A \times \varepsilon) \times B \times L}$$

A: Acceptance (depends on PDF, and other modeling uncertainties, e.g. renormalization and factorization scales)

ε : Selection efficiency for events in acceptance
(affected by the errors in triggers and reconstruction)

L: Integrated luminosity

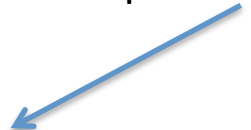
B: Branching ratio

Differential cross sections:

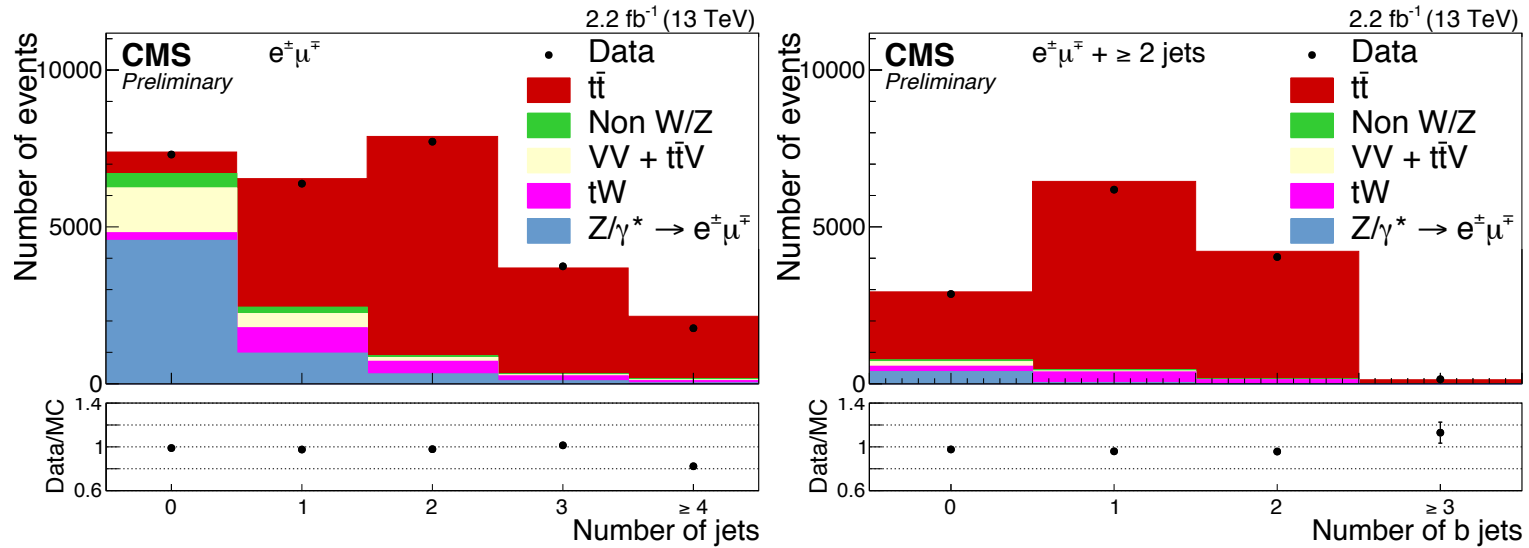
“Unfolded” to correct for detector effects (bin-to-bin migration) and acceptance

→ To particle or parton level

→ In full or fiducial phase space


$$\frac{1}{\sigma} \frac{d\sigma_i}{dX} = \frac{1}{\sigma} \frac{\sum_j R_{ij}^{-1} [N_{obs,j} - N_{bkg,j}]}{\Delta_i^X (A \times \varepsilon)_i}$$

Top Pair Cross Section at $\sqrt{s} = 13$ TeV in the $e\mu$ Channel



■ Cut and count

- ◆ Select $e\mu$ pair with ≥ 2 jets and ≥ 1 b-tag

TOP-16-005

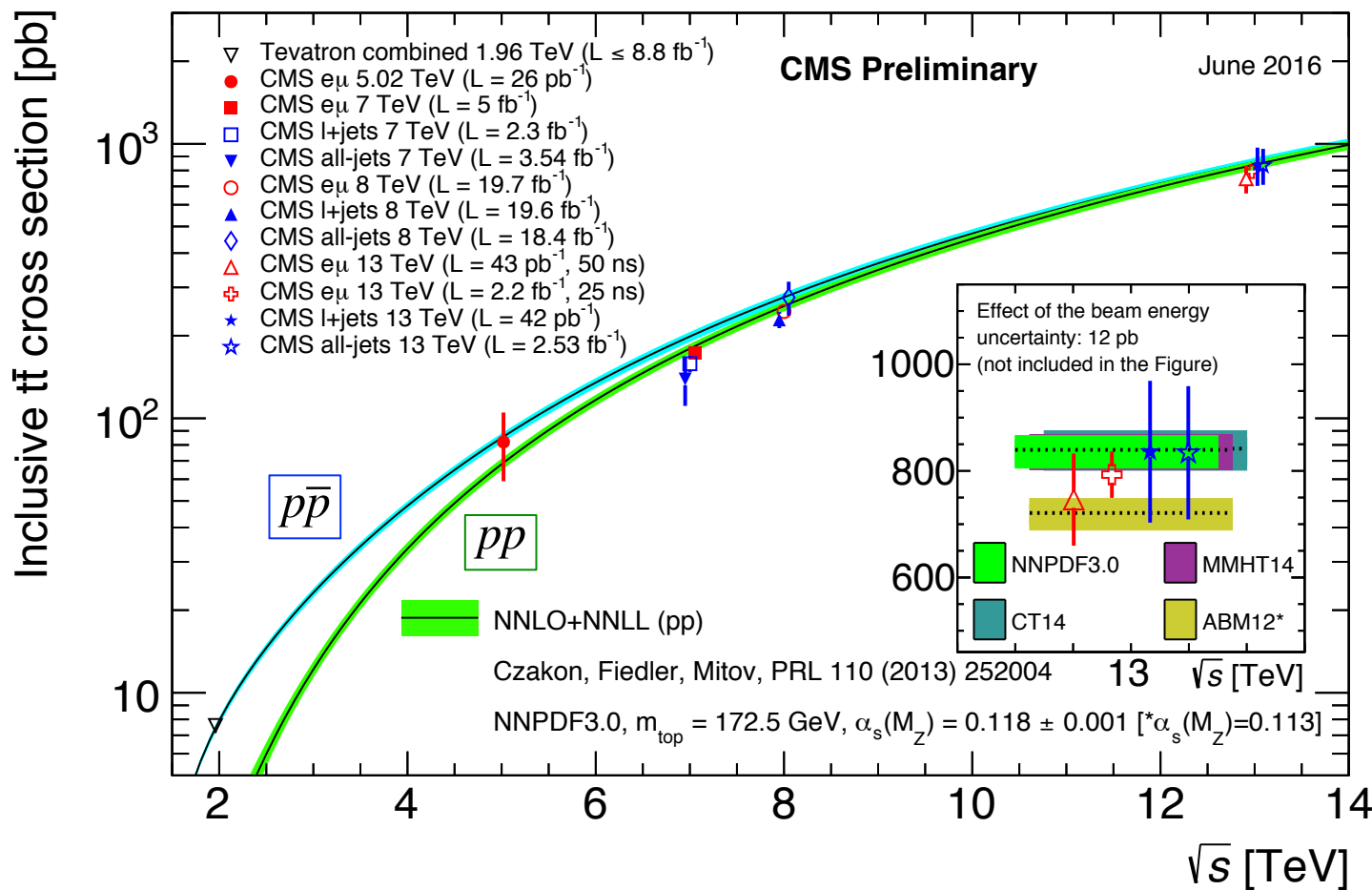
$$\sigma_{t\bar{t}}(m_t = 172.5 \text{ GeV}) = 793 \pm 8(\text{stat}) \pm 38(\text{syst}) \pm 21(\text{lumi}) \text{ pb}$$

→ Consistent with NNLO+NNLL prediction and other measurements from ATLAS and CMS.

→ Already dominated by systematic uncertainties:

- Luminosity, efficiencies, jet energy scale
- Effect of generator choice on acceptance (POWHEG vs MG5_aMC@NLO)

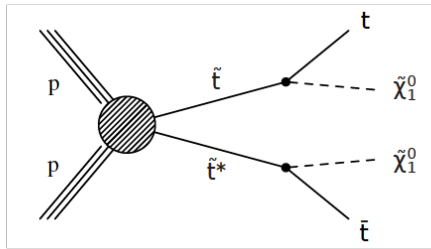
Production Cross Sections from $\sqrt{s} = 2$ to 13 TeV



■ $e\mu$ channel

- ◆ 13 TeV top pair cross section measurements: already at NNLO + NNLL precision.
- ◆ Run I legacy measurement precision: $\sim 3.5\%$. [arXiv:1603.02303](https://arxiv.org/abs/1603.02303)

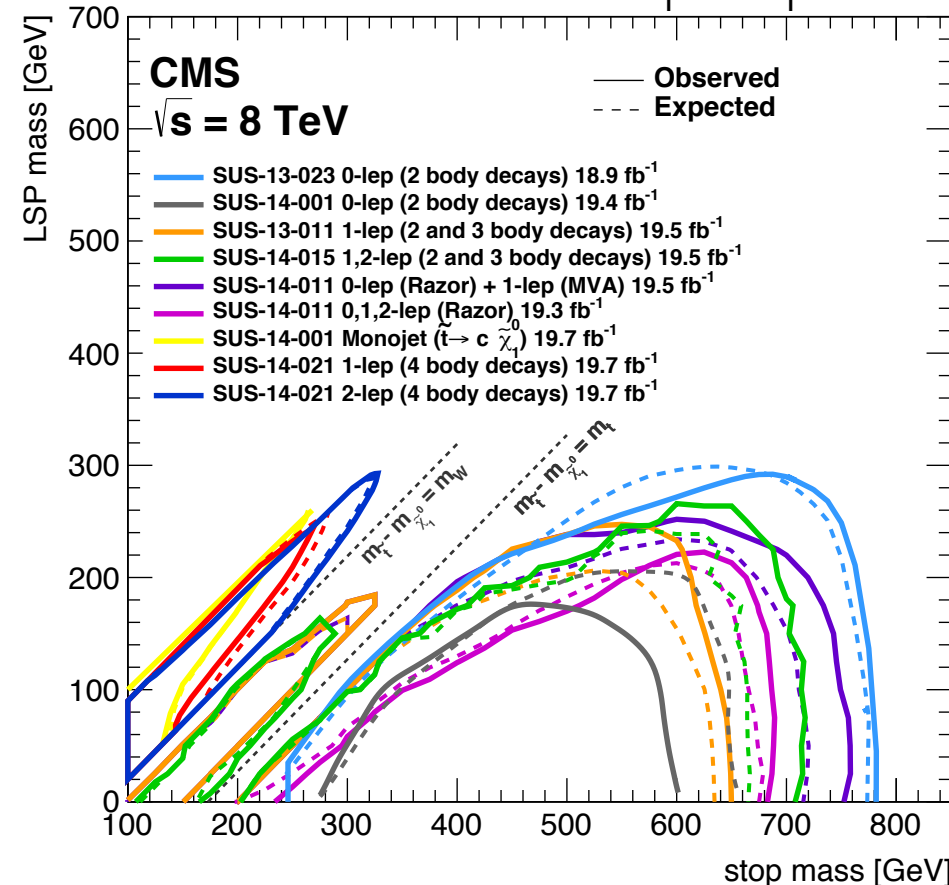
Top Squark Pair Production



$$m(\tilde{t}) \approx m(\tilde{\chi}_1^0) + m_t \longrightarrow \sigma_{t\bar{t}} \quad (\text{and } t\bar{t} \text{ spin correlations})$$

more sensitive than standard SUSY searches
for low $m(\tilde{\chi}_1^0)$ and $m(\tilde{t}) \approx m_t$

$\tilde{t}\tilde{t}^*$ production, $\tilde{t} \rightarrow t \tilde{\chi}_1^0 / c \tilde{\chi}_1^0$



Simplified model with two parameters:

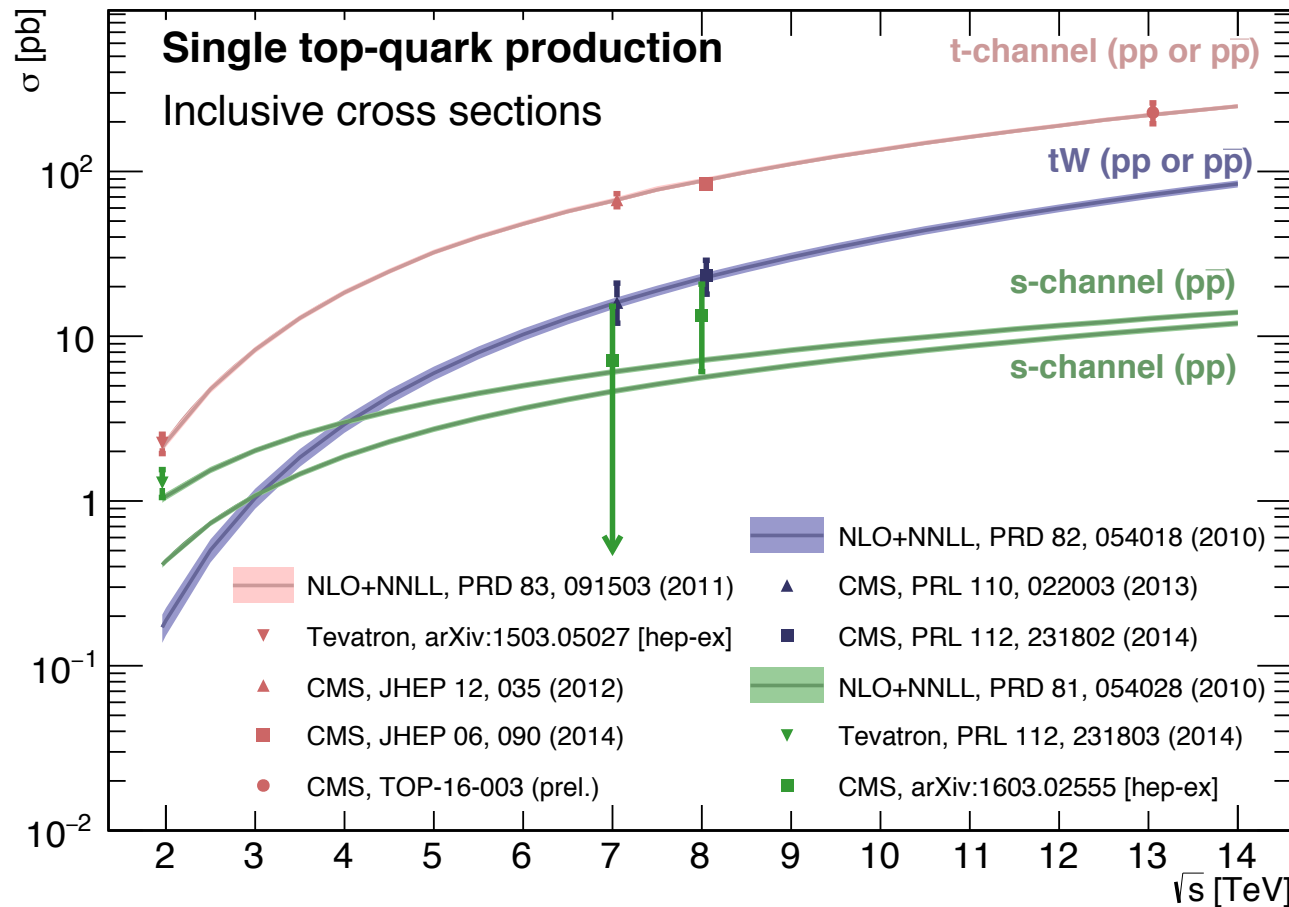
$$m(\tilde{t}), m(\tilde{\chi}_1^0)$$

[arXiv:1603.02303](https://arxiv.org/abs/1603.02303)

$$m(\tilde{t}; \tilde{\chi}_1^0 = 1 \text{ GeV}) > 189 \text{ GeV}$$

$$m(\tilde{t}; \tilde{\chi}_1^0) \notin 185 - 189 \text{ GeV}$$

Single Top Cross Sections – Current Status



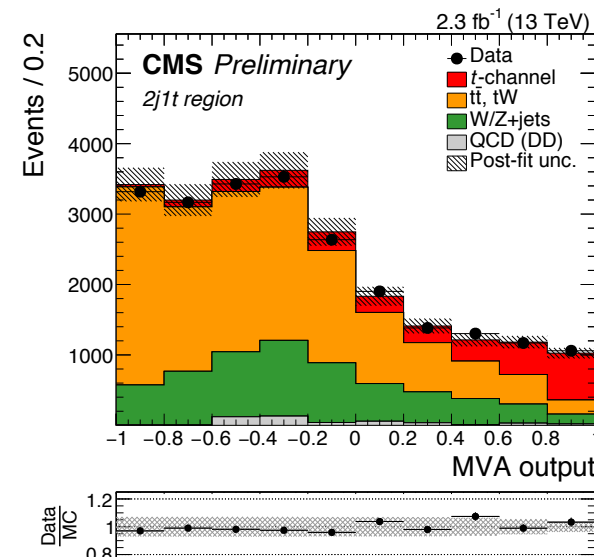
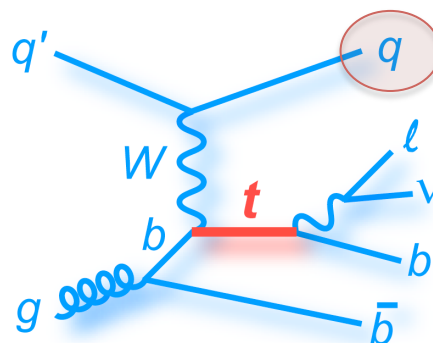
- All single top quark production modes measured at Run I.

- Single top t-channel cross section at NNLO precision
 - ◆ Theory uncertainty $\sim 1\%$
 - ◆ Measurement uncertainty
 - $\sim 10\%$ at 8 TeV (with 20 fb^{-1})
 - $\sim 15\%$ at 13 TeV (with 2.3 fb^{-1})

Single Top Cross Section at $\sqrt{s} = 13$ TeV

TOP-16-003

- Event selection: 1 μ , 2 or 3 jets, 1 or 2 b-jets.
- Signal from binned likelihood fits to MVA discriminators with η_{lj} , m_{lvb} , m_{jb} , $m_T(W)$, ... in different categories.



$$\sigma_{t\text{-ch.}}(t + \bar{t}) = 227.8 \pm 9.1(\text{stat}) \pm 14.0(\text{exp})^{+28.7}_{-27.7}(\text{theo}) \pm 6.2(\text{lumi}) \text{ pb} = 227.8^{+33.7}_{-33.0} \text{ pb}$$

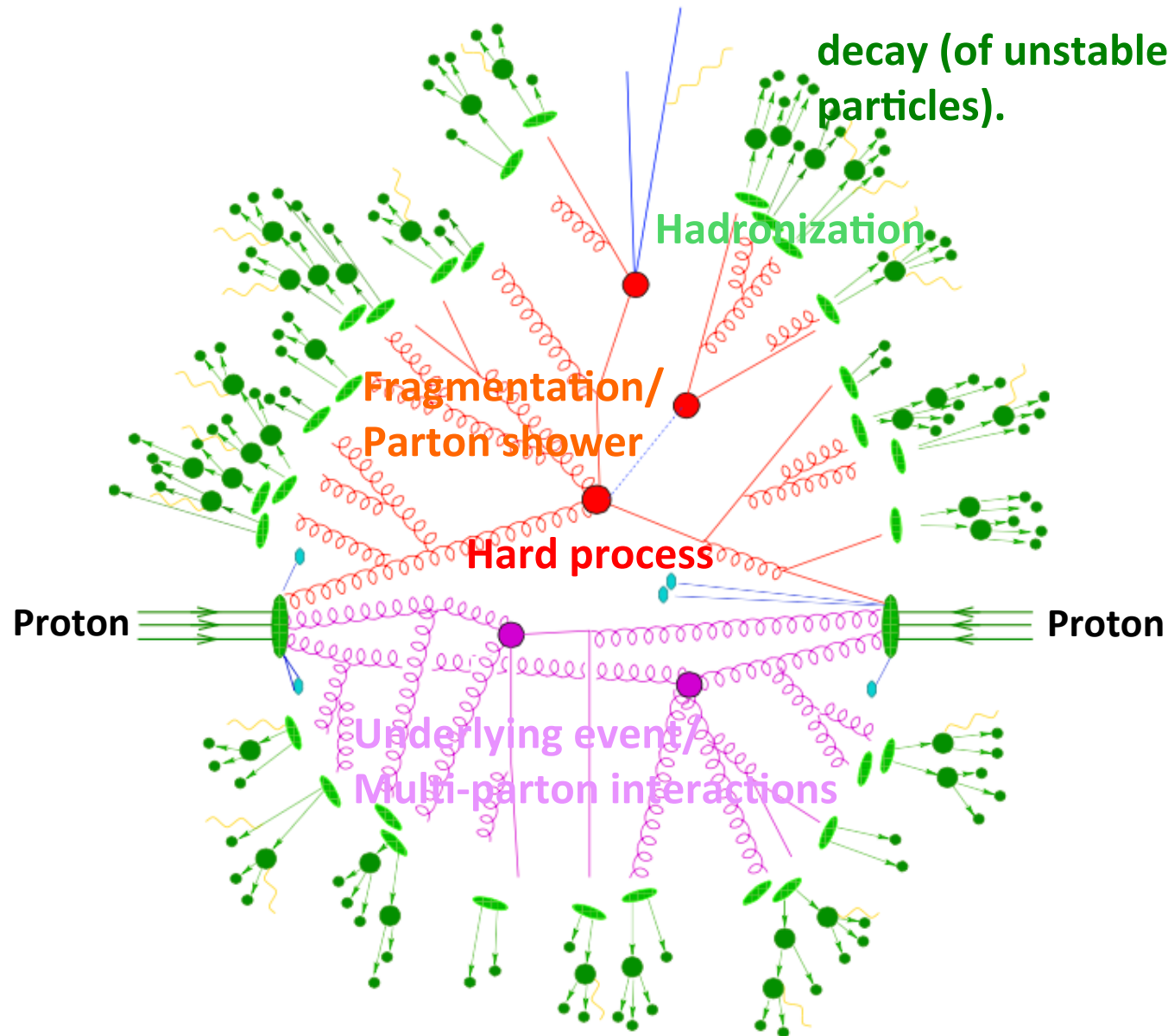
$$|V_{td}|, |V_{ts}| \ll |V_{tb}|, \text{Br} \cong 1$$

$$\rightarrow |f_V^L V_{tb}| = \sqrt{\frac{\sigma_{t\text{-ch.}}}{\sigma_{t\text{-ch.}}^{\text{theo.}}}} = 1.02 \pm 0.07(\text{exp}) \pm 0.02(\text{theo})$$

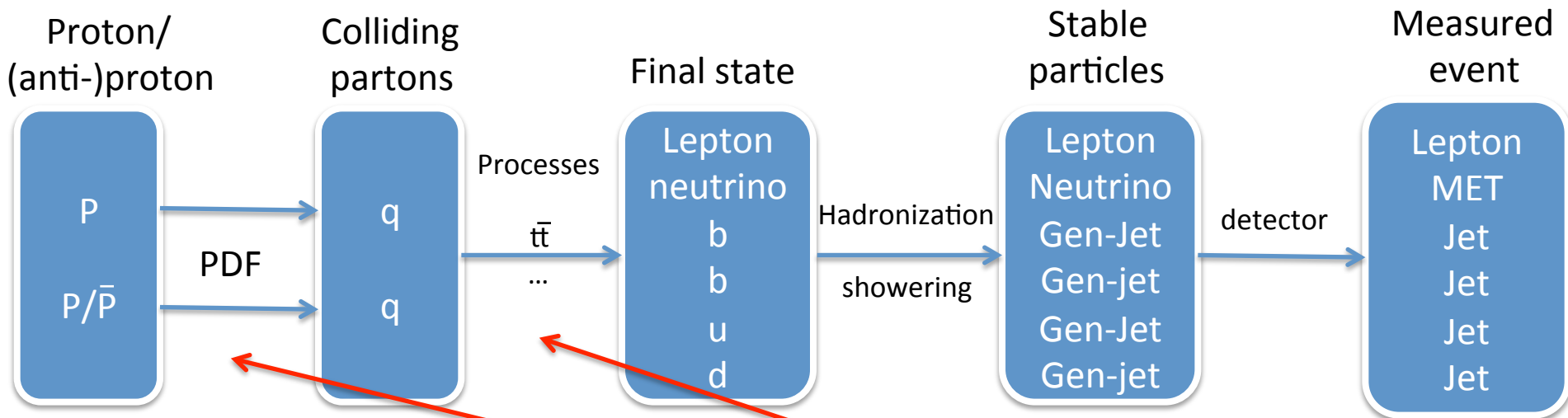
Result dominated by signal modelling and QCD scale uncertainties.

$$7+8 \text{ TeV} \rightarrow \delta_{|V_{tb}|} = 4\%$$

(Top Quark) Event Modeling



(Top Quark) Event Modeling



$$\sigma_{pp \rightarrow t\bar{t}}(s, m_t) = \sum_{i,j=\text{partons}} \int dx_1 dx_2 f_i^{pdf}(x_1, \mu_f^2) f_j^{pdf}(x_2, \mu_f^2) \hat{\sigma}_{ij \rightarrow t\bar{t}}(\hat{s}, m_t, \mu_f, \mu_r, \alpha_s(\mu_r))$$

Top Quark Event Modeling

$$\sigma_{pp \rightarrow t\bar{t}}(s, m_t) = \sum_{i,j=\text{partons}} \int dx_1 dx_2 f_i^{pdf}(x_1, \mu_f^2) f_j^{pdf}(x_2, \mu_f^2) \hat{\sigma}_{ij \rightarrow t\bar{t}}(\hat{s}, m_t, \mu_f, \mu_r, \alpha_s(\mu_r)) \oplus \text{showering/ \& hadronization}$$

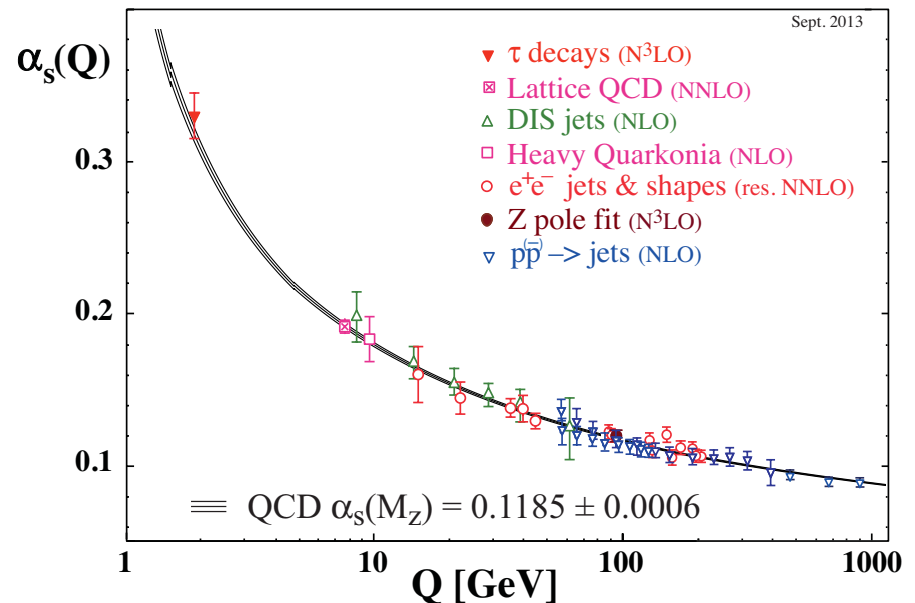
factorization $\rightarrow$ $\text{PDFs}(x, \mu_f^2) \otimes \hat{\sigma}(\hat{s}, m_t, \mu_f, \mu_r, \alpha_s(\mu_r))$

$p_T^{\text{parton}} < \mu_F$

$p_T^{\text{parton}} > \mu_F$

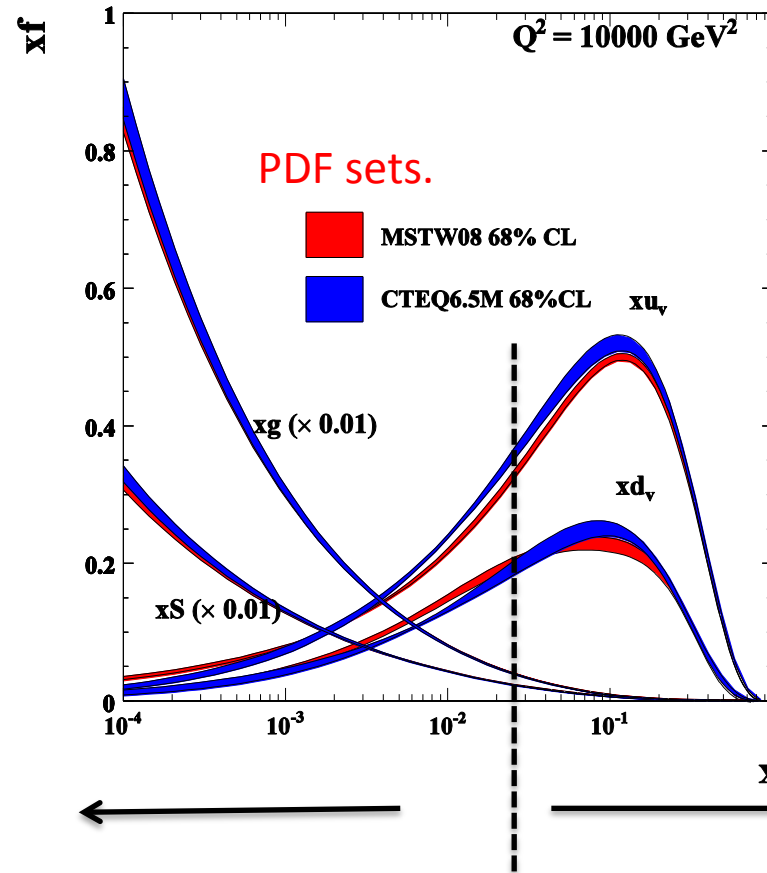
$\mu_f \sim Q \sim \sqrt{\hat{s}} \sim \sqrt{x_1 x_2 s}$ (Q : energy scale of the hard process)

$\rightarrow$ inputs: m_t , α_s
and PDFs



- The quark sea:*

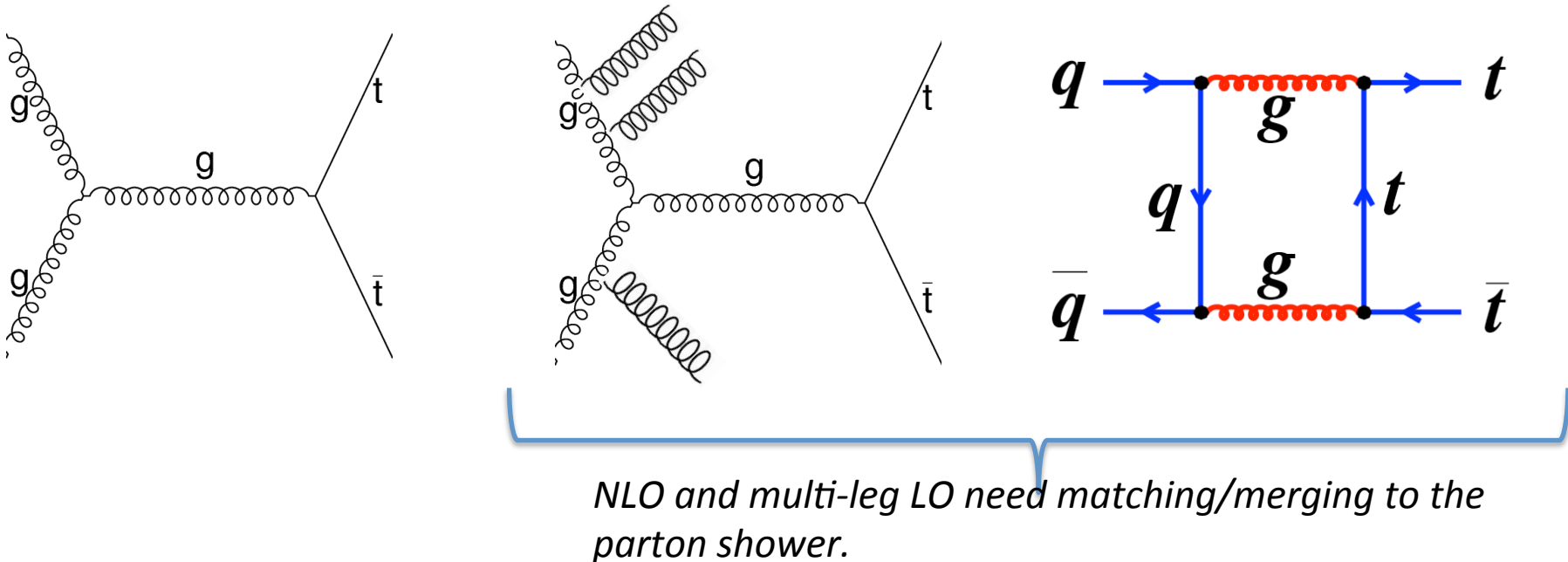
sea quarks
dominate.



Valence quarks dominate.

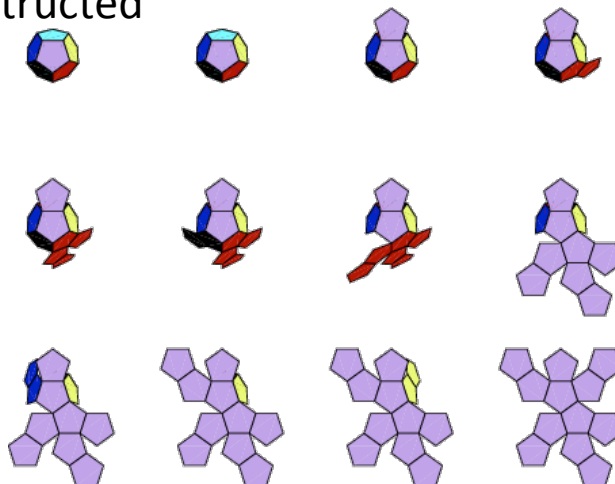
Hard Process

- Calculation in perturbative QCD
 - ◆ LO $\rightarrow$ LO ME + Radiation from parton shower.
 - ◆ Multi-leg LO $\rightarrow$ LO + Additional partons in the hard process but no loops + radiation from parton shower.
 - ◆ NLO $\rightarrow$ LO + Additional partons in the hard process including loops (+ parton shower).

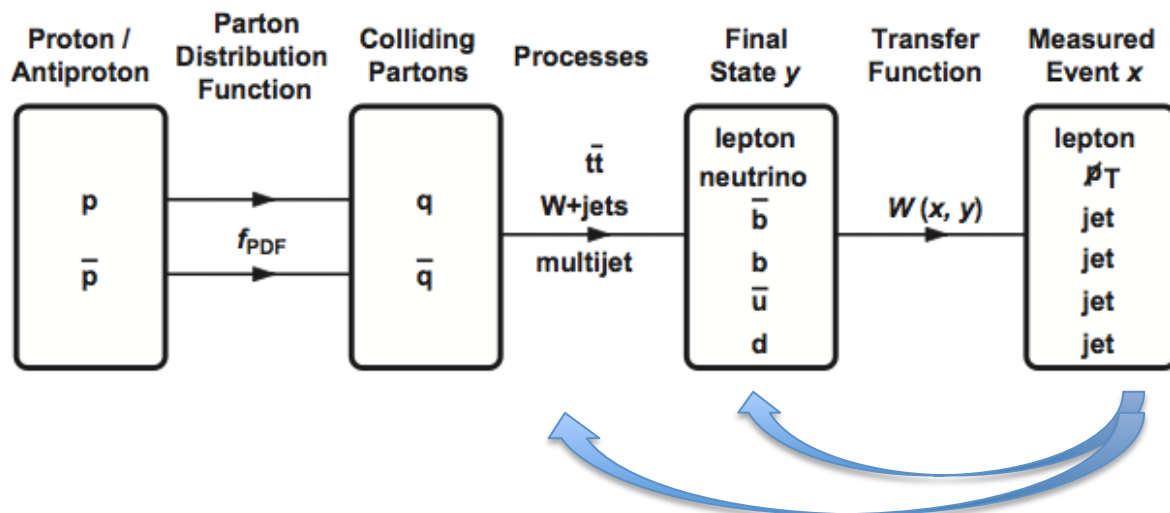


Unfolding

reconstructed
level

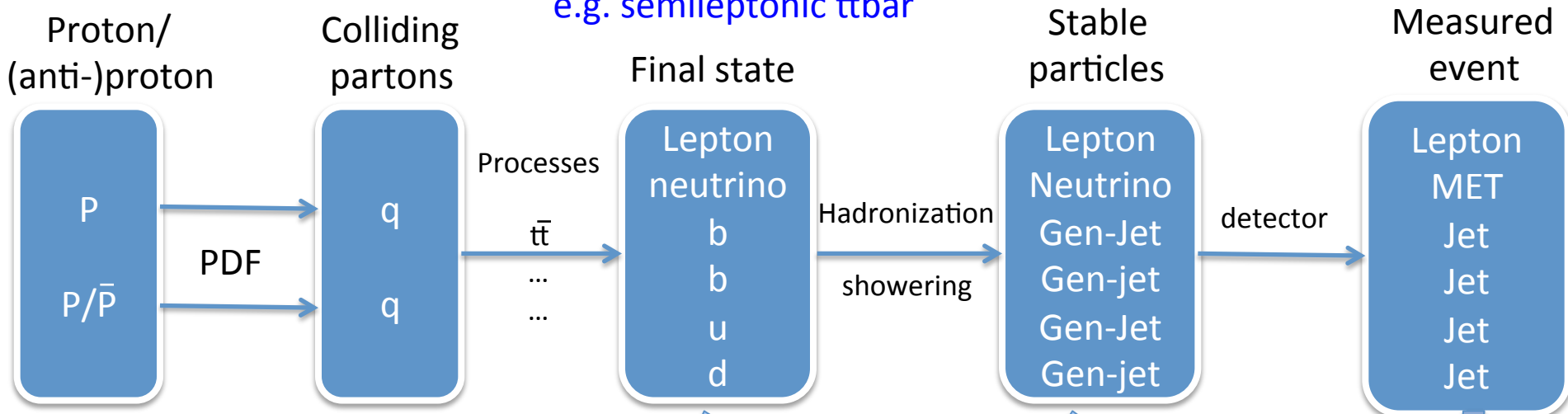


parton/particle
level



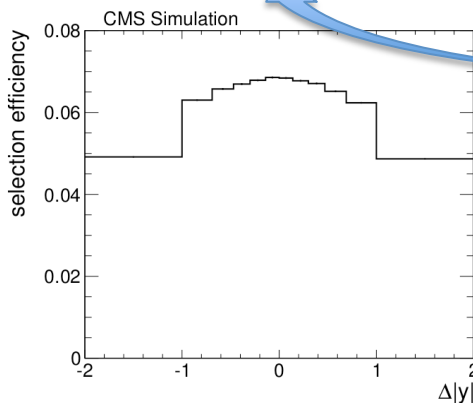
Unfolding

e.g. semileptonic $t\bar{t}b\bar{b}$

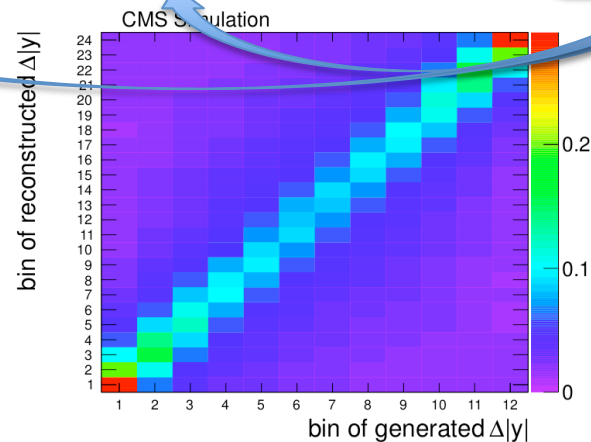


The goal is to compare to theory predictions (at the particle/parton level).

Commonly used unfolding methods:
iterative D'Agostini, SVD



selection efficiency
→ diagonal matrix

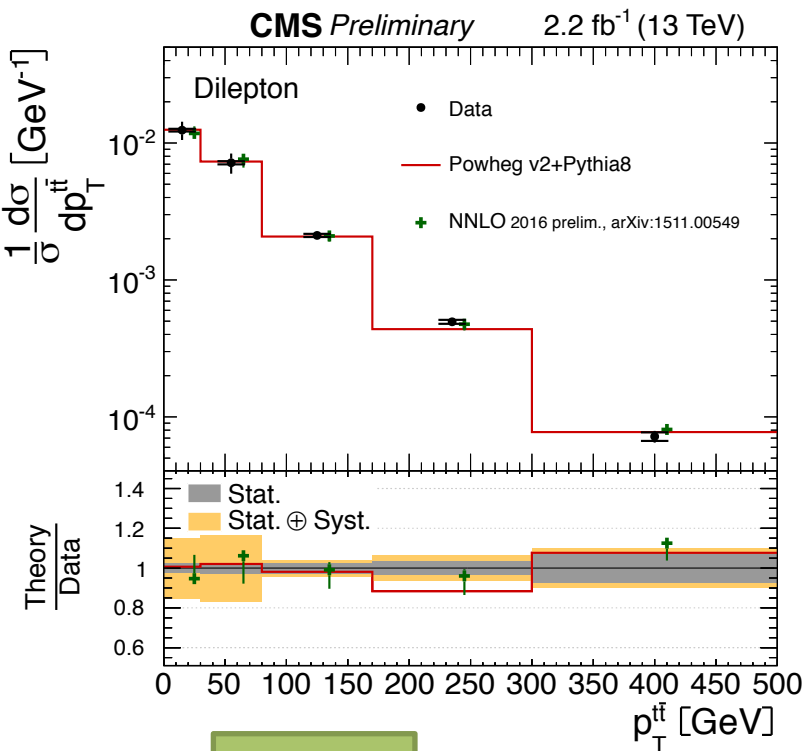


(non-diagonal)
bin migration matrix

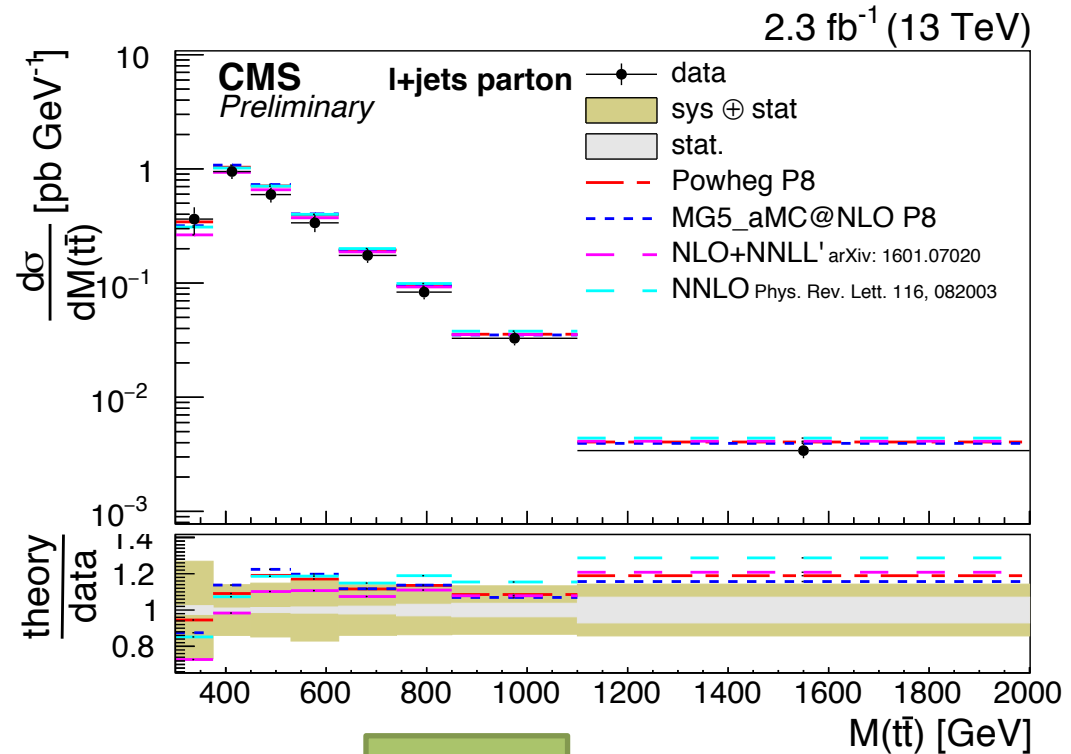
e.g., CMS-PAS-TOP-12-033

Top Pair Differential Cross Sections

- Test QCD description of the top quark (both as signal and background)
- Test and tune **new MCs (NLO ME + LO PS MC)**



TOP-16-011

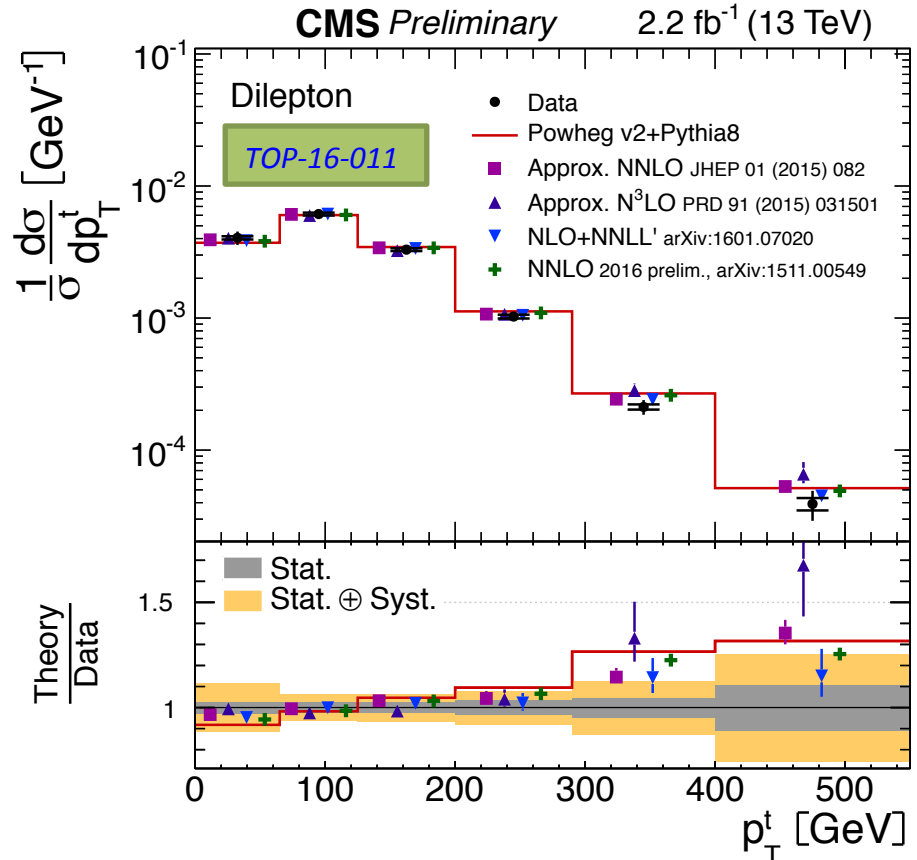
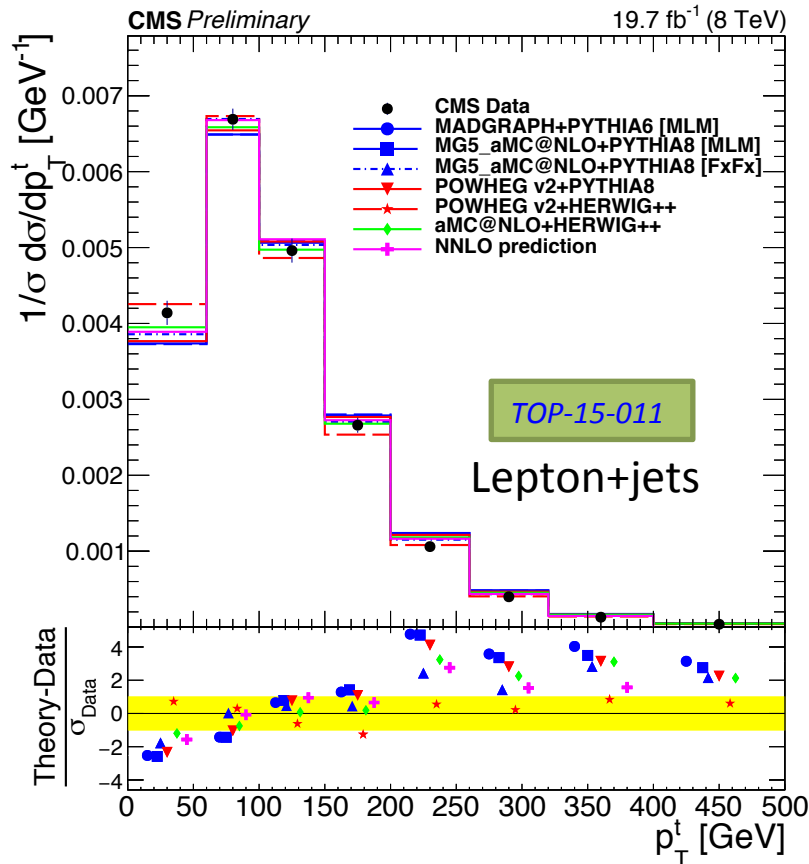


TOP-16-008

- Differential distributions described reasonably well.

The Top Quark p_T

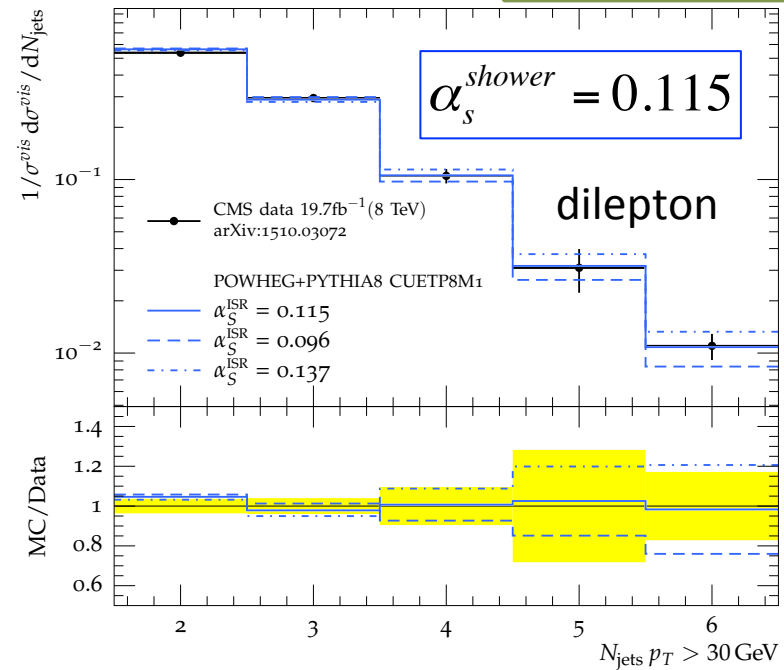
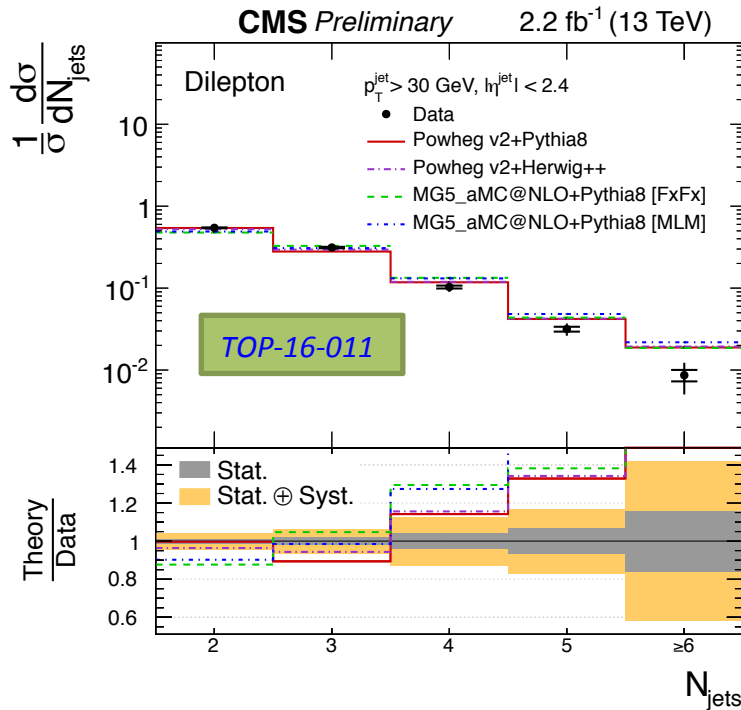
- LHC Run 1 “discovery”: harder spectrum in LO/NLO+PS predictions than in data.
 - NNLO+NNLL $\rightarrow$ significantly better description of top p_T .
- First results at 13 TeV: similar behavior.



Jet Multiplicity at $\sqrt{s} = 13$ TeV

- Low jet multiplicities $\rightarrow$ Sensitive to Matrix element and matching to parton shower.
- High jet multiplicities $\rightarrow$ parton shower
- $t\bar{t}$ +jets important background to $t\bar{t}H$.

arXiv:1510.03072;
Rivet: CMS_2015_11397174



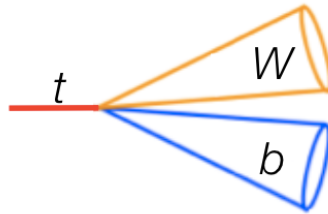
- New ME generator + PS codes in Run II
- Predictions overshoot the data for jet large multiplicities when out of the box parameters are used (in Monash-based tunes).
- First fix: α_s^{shower}

Monash Tune: Skands, Carrazza, Rojo, EPJ C 74 (2014) 1

Boosted Top Pair Production

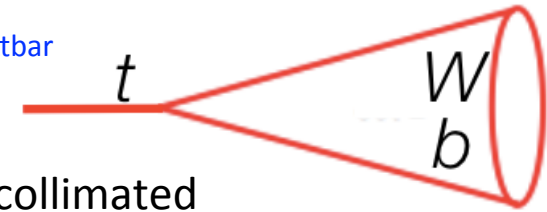
arXiv:1605.00116

Resolved topology:
Each parton matched
to a single jet.



High top p_T or high $m_{t\bar{t}}$

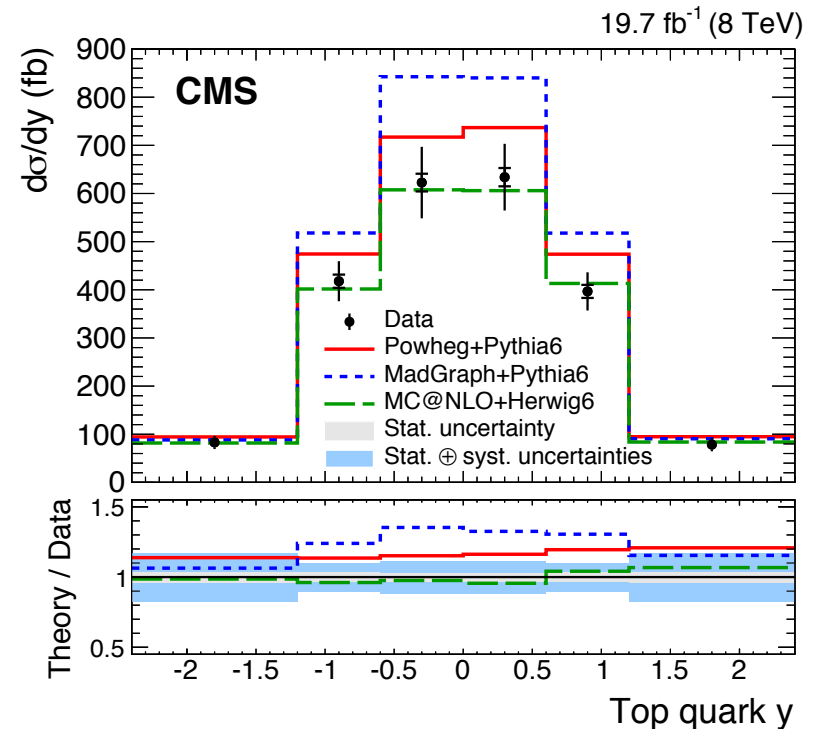
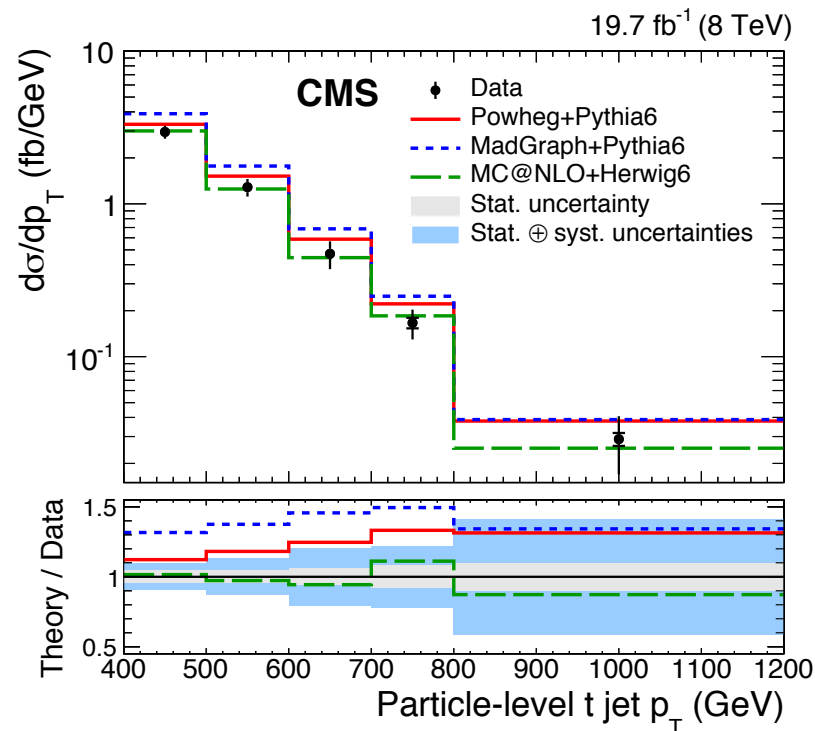
Boosted topology:
→ Decay products collimated



"fat jet", $R=0.8$

$m_{\text{jet}} \sim m_{\text{top}}$

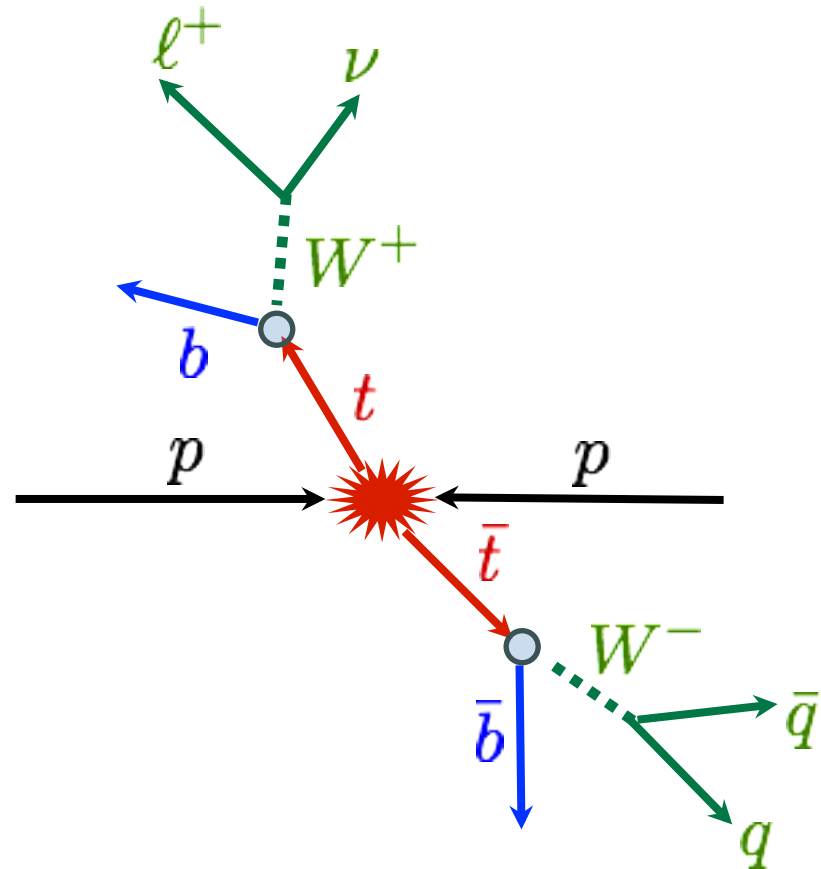
- Measurements at parton and particle levels.



QUESTIONS & BREAK

Top Mass Measurements

- Basic methods
 - ◆ Full invariant mass reconstruction → The most powerful and standard
 - ◆ Partial reconstruction using a variable correlated to top mass → less powerful but different systematic uncertainties
 - ◆ Indirect measurement through $t\bar{t}$ and $t\bar{t}$ +jet cross sections, ... → top quark pole mass

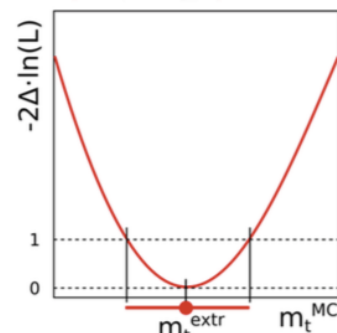
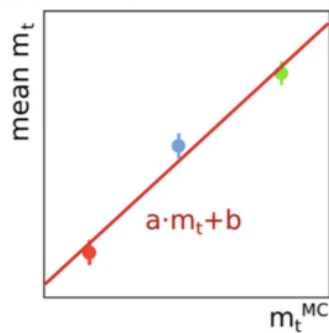
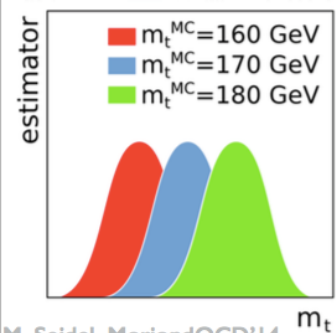
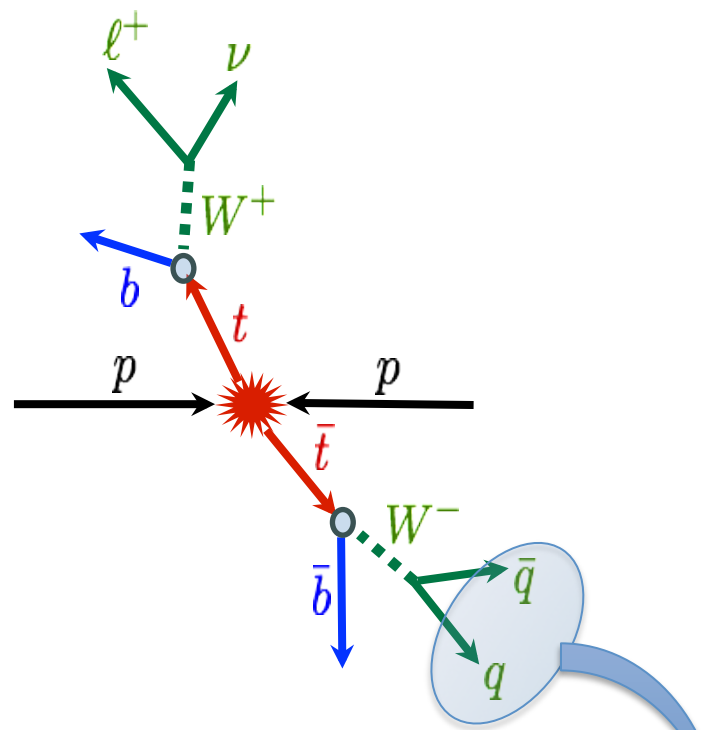


Full Mass Reconstruction

General features:

- ◆ Assign each jet to a top decay product (constrained kinematic fits)
- ◆ Fit to templates
- ◆ Calibration of the method based on $m_t^{\text{MC}} = m_t^{\text{meas}}$
- ◆ Determination of m_t^{MC} (and JES simultaneously) from data.

Main challenge: Jet reconstruction, Jet energy scale uncertainties, modeling.

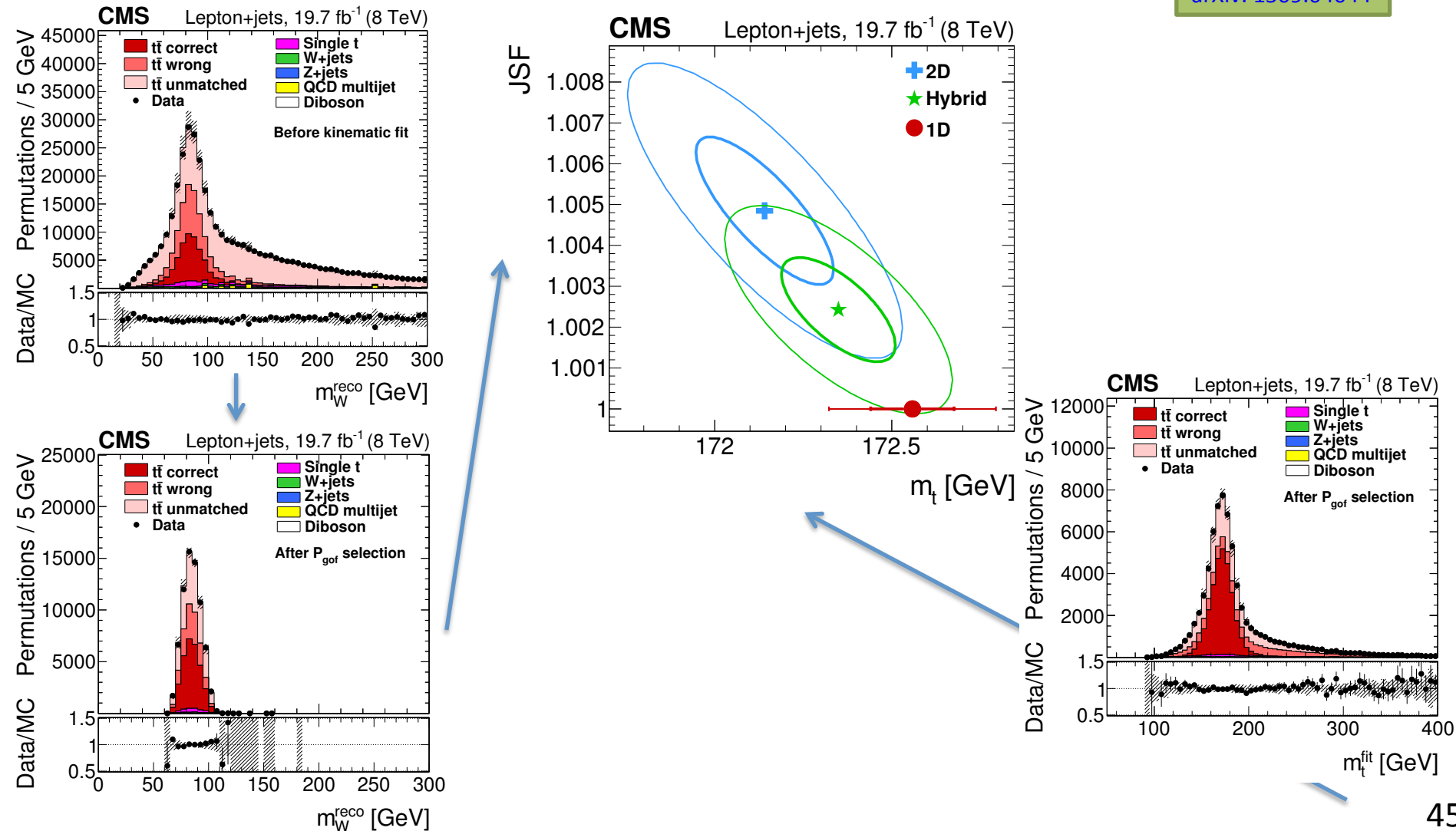


- ➔ JES calibration with dijet and γ/Z +jet events $\rightarrow$ $\sim 1\text{-}3\%$
- ➔ $< 1\%$ when complemented with in-situ JES calibration.

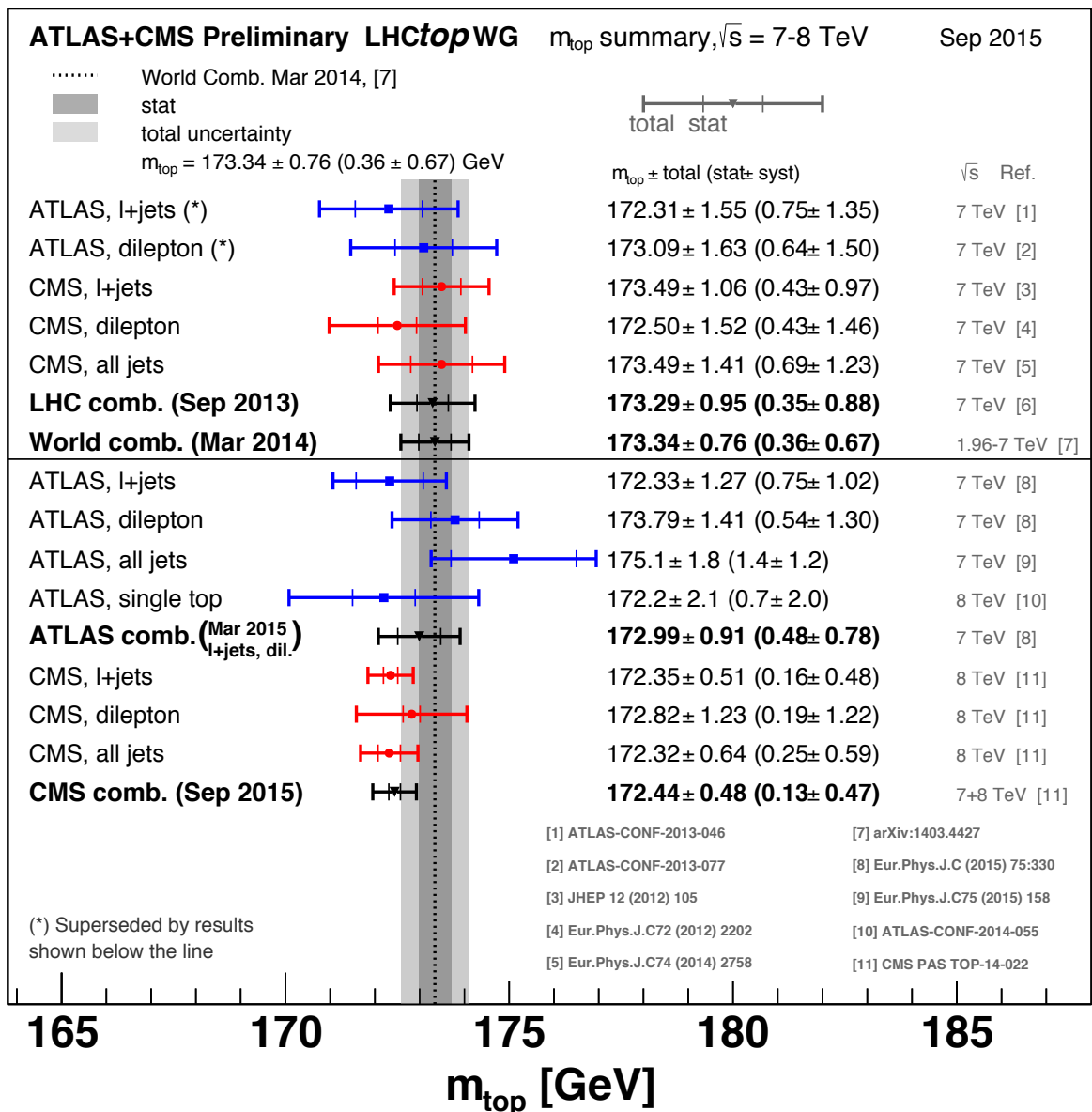
E.g. Full Mass reconstruction: The Ideogram Method

- Template method with multiple permutations (correct, wrong, unmatched) per event.
- All different permutations taken into account.
- Kinematic fit $\rightarrow$ improve mass reconstruction.

arXiv: 1509.04044



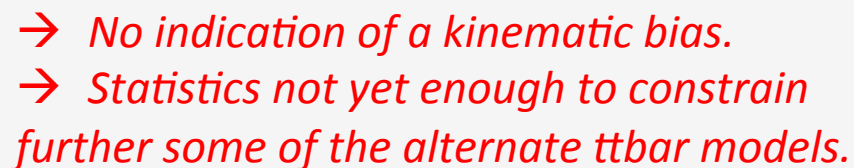
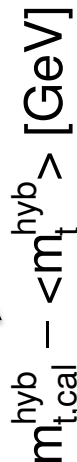
Summary of Top Mass Measurements using full Mass reconstruction



- Precision 0.3% $\sim 2\Lambda_{\text{QCD}}$
- Dominant systematic uncertainties: flavor-dependent JEC and b jet modeling.

arXiv:1509.04044

- Measurement calibrated in each bin –
Average from the inclusive measurement.



Top Quark Mass - Definitions

- Free quarks not observable (confining property of QCD)
- All quarks except the top quark hadronize → Top quark mass theoretical framework dependent.
- Two common definitions:
 - ◆ Pole mass (See e.g. arXiv:9612329) $\sqrt{p^2} = m_t - i\Gamma_t/2$
 - Perturbatively defined
 - Position of the pole in the renormalized quark propagator
 - “intuitive mass” (directly related to the production rate of $t\bar{t}$ pairs)
 - Suffers from ambiguities due to non-perturbative corrections.
 - Ambiguity of $\sim \Lambda_{\text{QCD}}$
 - ◆ “Running (or short distance mass) mass” (m_t^{MSbar})
 - Renormalization scale dependent.

The two definitions can be related analytically with an uncertainty $< \sim \Lambda_{\text{QCD}}$

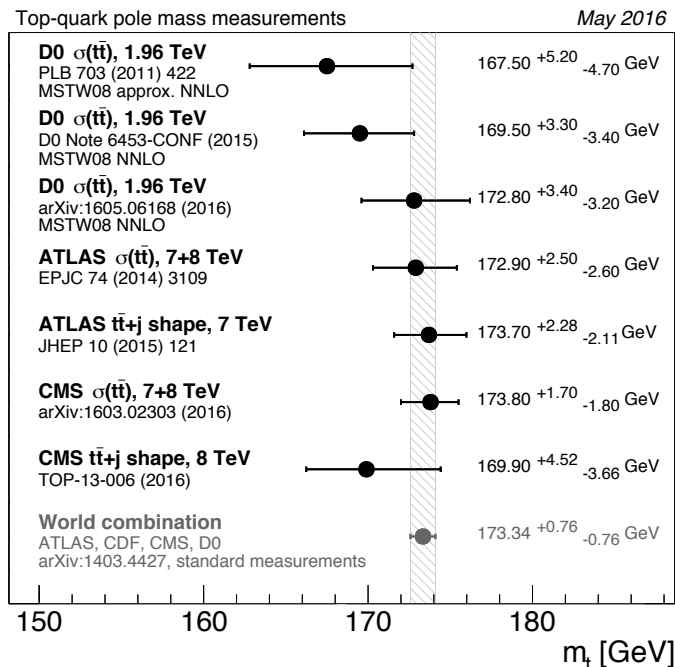
e.g. see Marquard et al. PRL 114 (2015) 142002

Top Quark Mass Definitions

◆ Monte Carlo Mass

- No straightforward definition in standard top mass measurements
- Direct top quark measurements rely on the complicated relation between the experimental observable and m_t .
- MEs at fixed order (LO or NLO) QCD + higher orders by parton showers

$$m_t^{MC} \neq m_t^{pole} \neq m_t^{MS} \neq m_t^{XX}$$

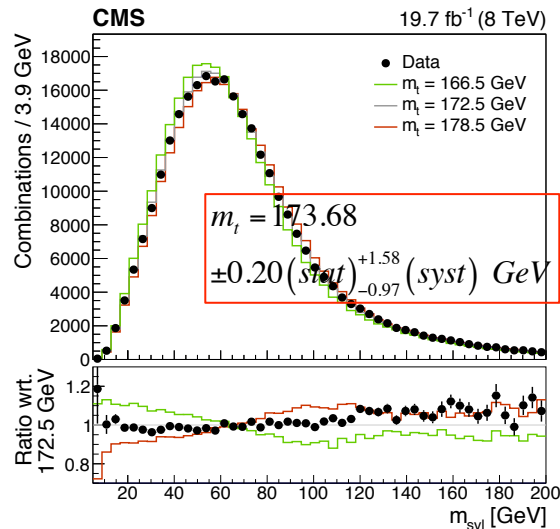
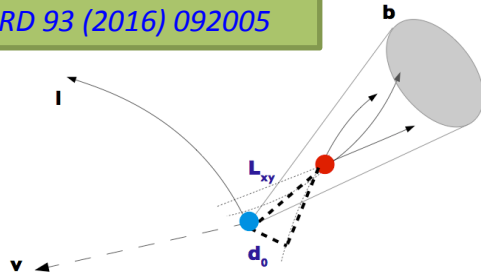


- With the current precision, top-quark pole mass measurements consistent with the standard measurements.

Recent Alternative Top Quark Mass Measurements

Invariant mass of the secondary vertex w/ ≥ 3 tracks + lepton.

PRD 93 (2016) 092005



Minimal experimental uncertainties.

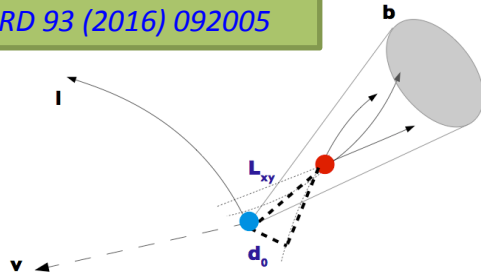
Large dependence on fragmentation modeling.

M_{svtx} mass:
b fragmentation

Recent Alternative Top Quark Mass Measurements

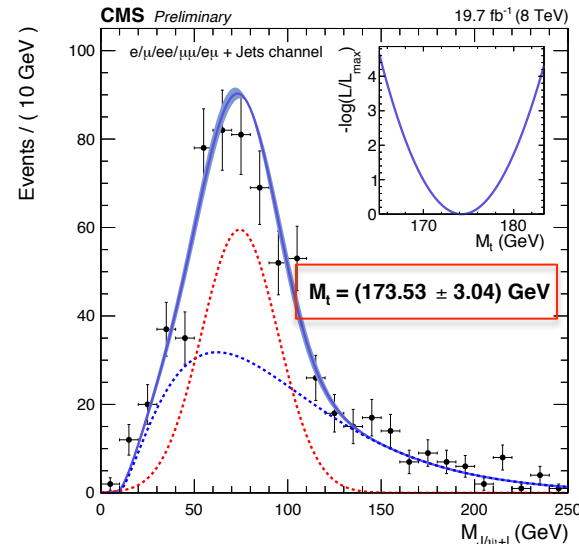
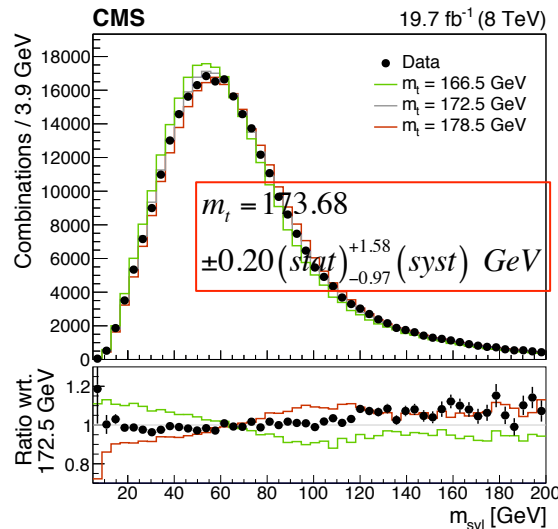
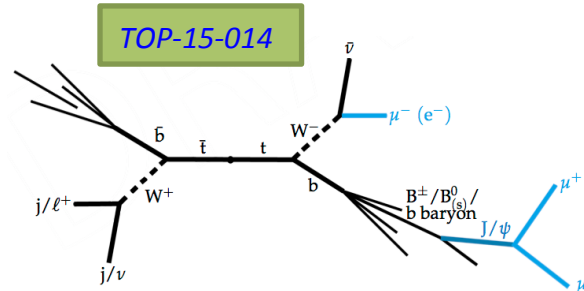
Invariant mass of the secondary vertex w/ ≥ 3 tracks + lepton.

PRD 93 (2016) 092005



J/ψ+lepton mass

TOP-15-014



*Minimal experimental uncertainties.
Large dependence on fragmentation modeling.*

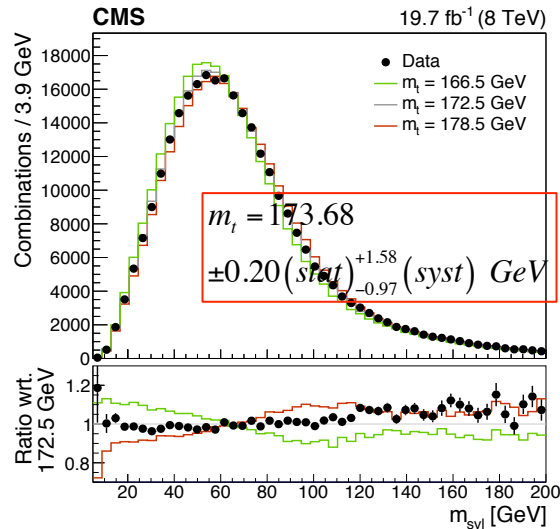
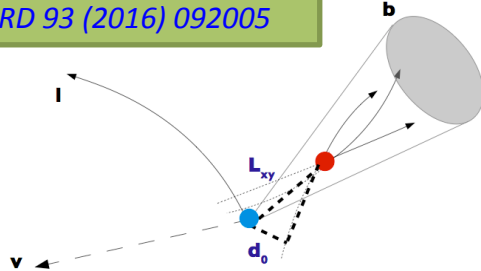
M_{svtx} mass:
b fragmentation

J/ψ+lepton mass:
Result statistically limited

Recent Alternative Top Quark Mass Measurements

Invariant mass of the secondary vertex w/ ≥ 3 tracks + lepton.

PRD 93 (2016) 092005

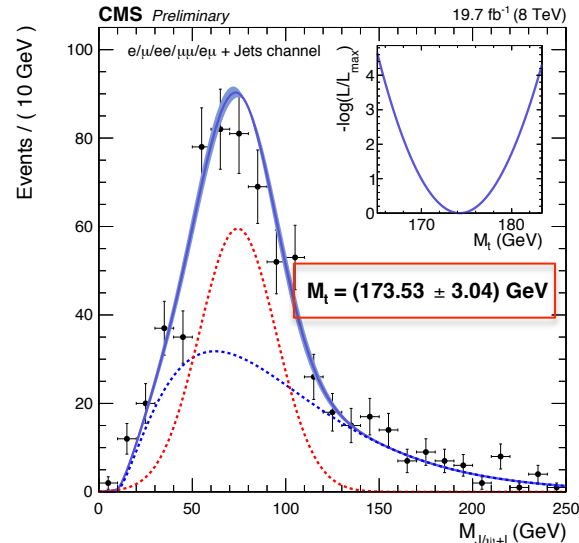
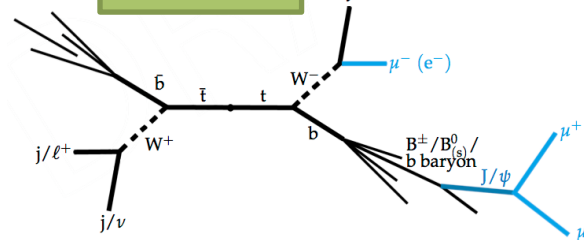


Minimal experimental uncertainties.
Large dependence on fragmentation modeling.

M_{svtx} mass:
b fragmentation

J/ψ+lepton mass

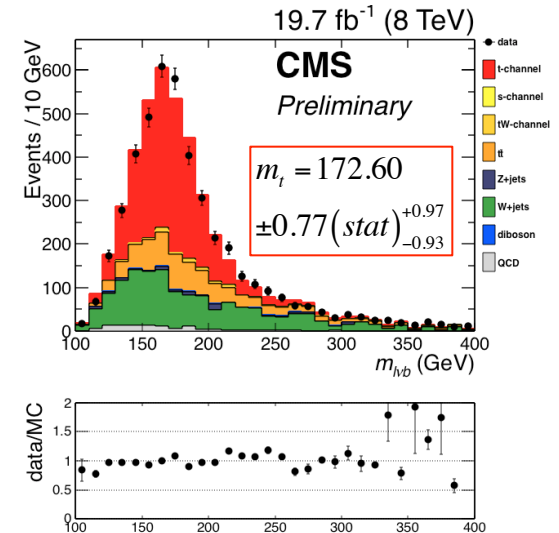
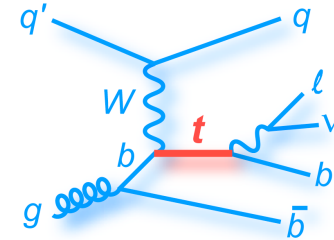
TOP-15-014



J/ψ+lepton mass:
Result statistically limited

M_{lvb} in single top topology

TOP-15-001



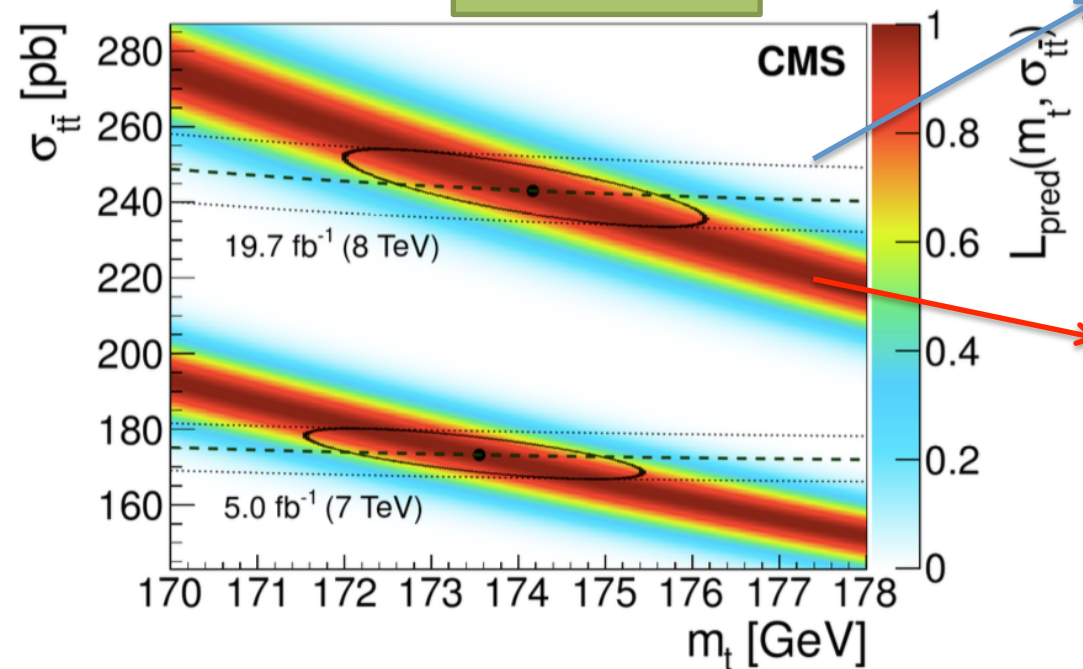
Alternative event topology
Partially uncorrelated systematics
Different color flow $\rightarrow$ check for
“unknown” syst.

Top Quark Pole Mass from $t\bar{t}$ Production Cross Section: Fix $\alpha_s(m_Z)$ and PDF $\rightarrow$ Determine m_t^{pole}

$$\sigma_{pp \rightarrow t\bar{t}}(s, m_t) = \sum_{i,j=\text{partons}} \int dx_1 dx_2 f_i^{\text{pdf}}(x_1, \mu_f^2) f_j^{\text{pdf}}(x_2, \mu_f^2) \hat{\sigma}_{ij \rightarrow t\bar{t}}(\hat{s}, m_t, \mu_f, \mu_r, \alpha_s(\mu_r))$$

- Full phase space cross sections at parton level with full Run-I data at 7 and 8 TeV in the most precise channel ($e\mu$).
- Minimize theory x experimental likelihoods.

arXiv:1603.02303



Dependence due to efficiency and acceptance depending weakly on m_t .

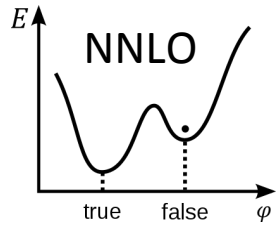
Recall:
$$\sigma = \frac{N_{\text{obs}} - N_{\text{bkg}}}{(A \times \epsilon) \times B \times L}$$

It is harder to produce heavier particles.

	m_t [GeV]
NNPDF3.0	$173.8^{+1.7}_{-1.8}$
MMHT2014	$174.1^{+1.8}_{-2.0}$
CT14	$174.3^{+2.1}_{-2.2}$

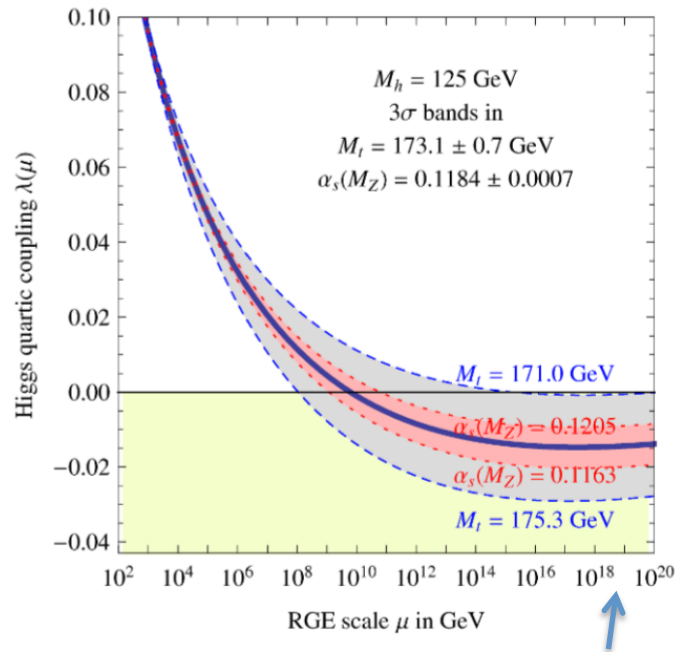
Dominant uncertainties:
Luminosity, beam energy

The Top Quark Mass and the Electroweak Vacuum

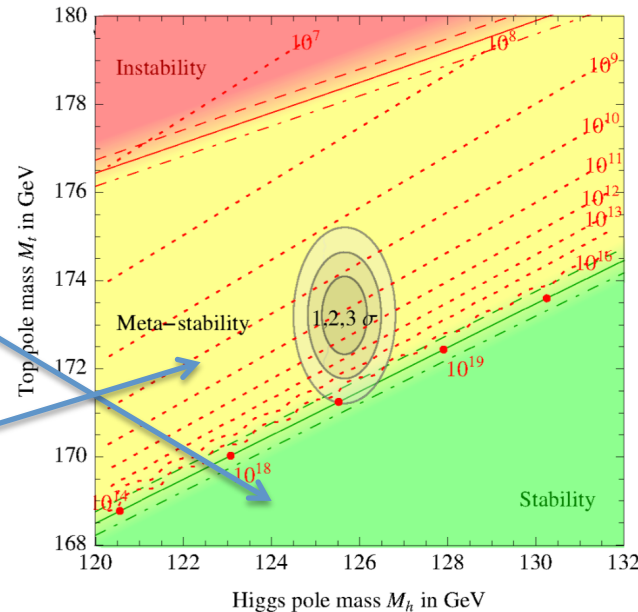


$$V^{\text{eff}} \approx -\frac{1}{2}m^2(\mu)\phi^2(\mu) + \lambda(\mu)\phi^4(\mu) \sim \lambda(\mu)\phi^4(\mu)$$

when $\phi(\mu) \gg v$



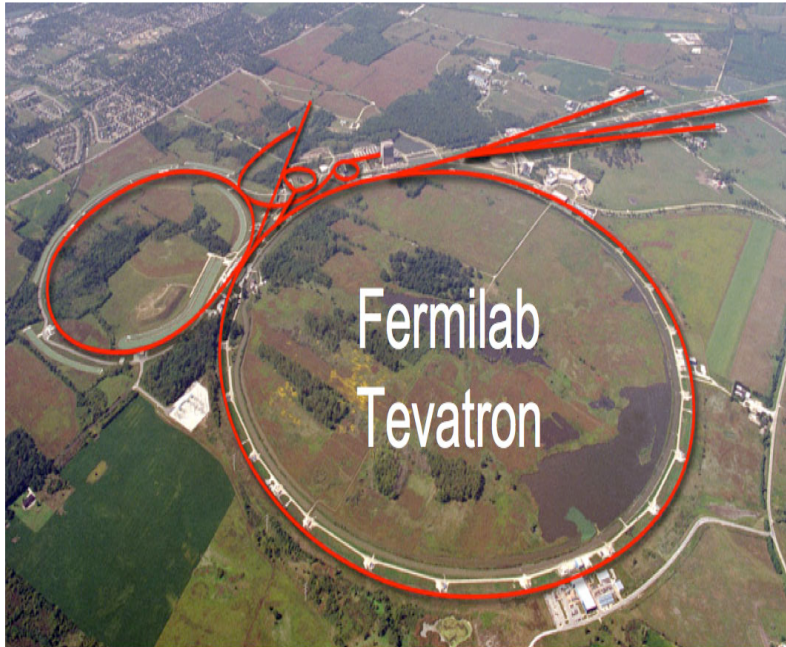
Planck scale



v : electroweak minimum

- The measured values of the top quark and the higgs boson mass
 - ◆ SM is consistent and could be valid up to Planck scale.
 - ◆ Vacuum may be Meta-stable.

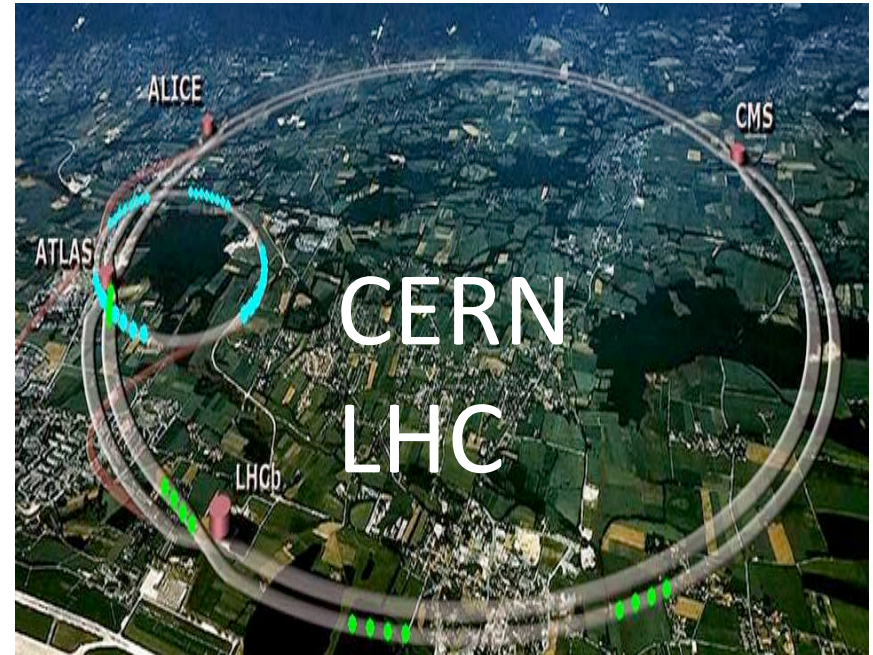
Asymmetries at Hadron Colliders



$P\bar{P}$ collider

Parity $\rightarrow$ changes the direction of
proton and anti-proton
Charge $\rightarrow$ changes the direction of
proton and anti-proton

CP symmetric $\sigma_{total} = \bar{\sigma}_{total}$
not C and P symmetric separately



PP collider

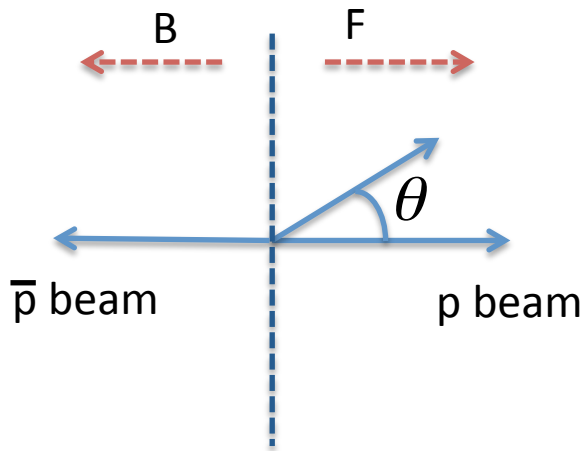
Parity $\rightarrow$ changes nothing
Charge $\rightarrow$ Makes LHC an anti-proton
collider.

Not CP symmetric $\sigma_{total} \neq \bar{\sigma}_{total}$
not C symmetric but P symmetric.

Asymmetries at Hadron Colliders

$P\bar{P}$ collider (Tevatron)

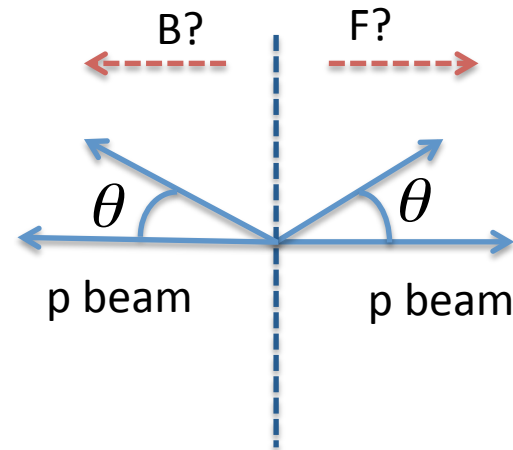
Parity asymmetric



Allows the definition of a forward (backward) hemisphere based on the P direction.

PP collider (LHC)

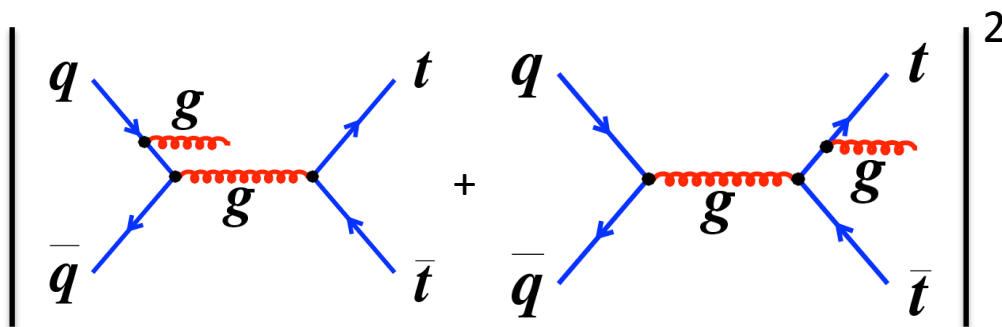
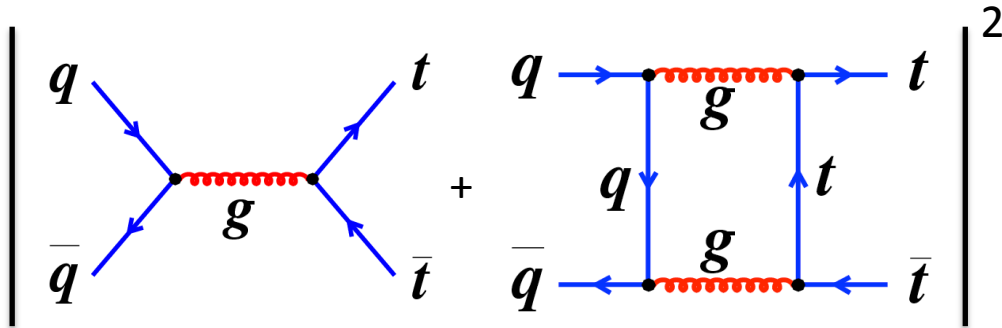
Parity symmetric



Does not allow the definition of a forward (backward) hemisphere based on the P direction, **unless we consider the Parton Distribution Functions (PDFs.)**

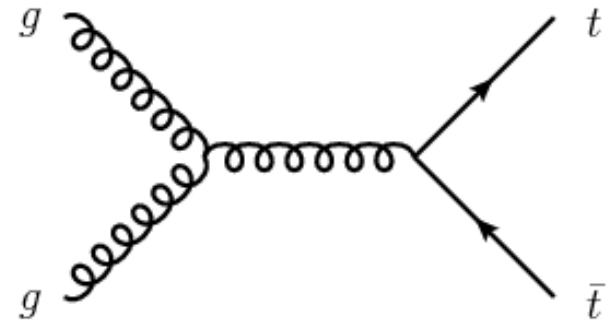
Asymmetry from Interference - $t\bar{t}$

Interference: tree-level + box diagrams
(positive asymmetry)



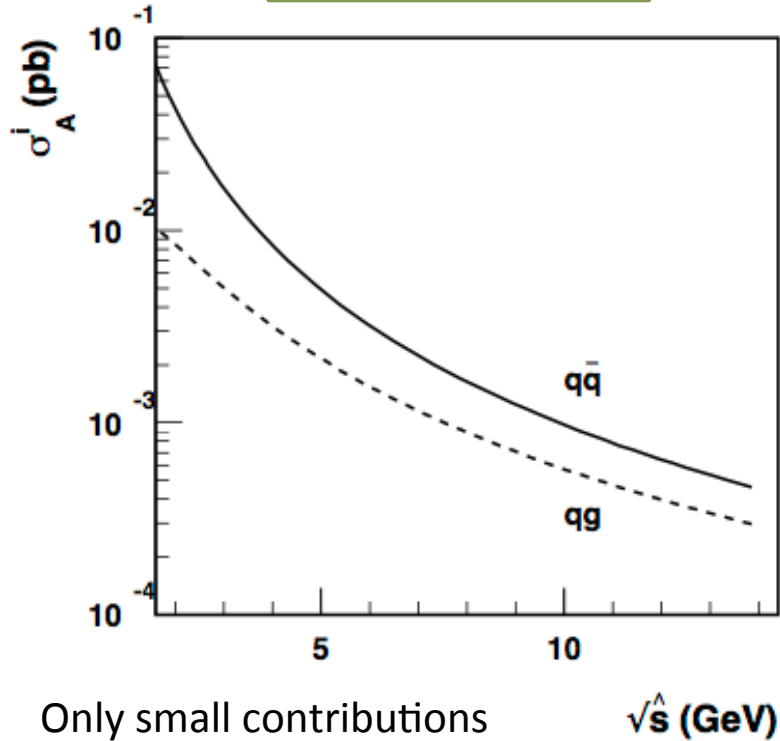
Interference: ISR+FSR
(negative asymmetry)

- No asymmetry at LO
- No asymmetry from gluon fusion
- At NLO: Interferences between $q\bar{q}$ diagrams

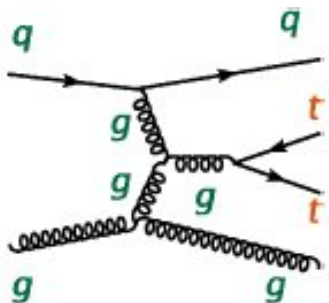


Asymmetry from Interference - $t\bar{t}$

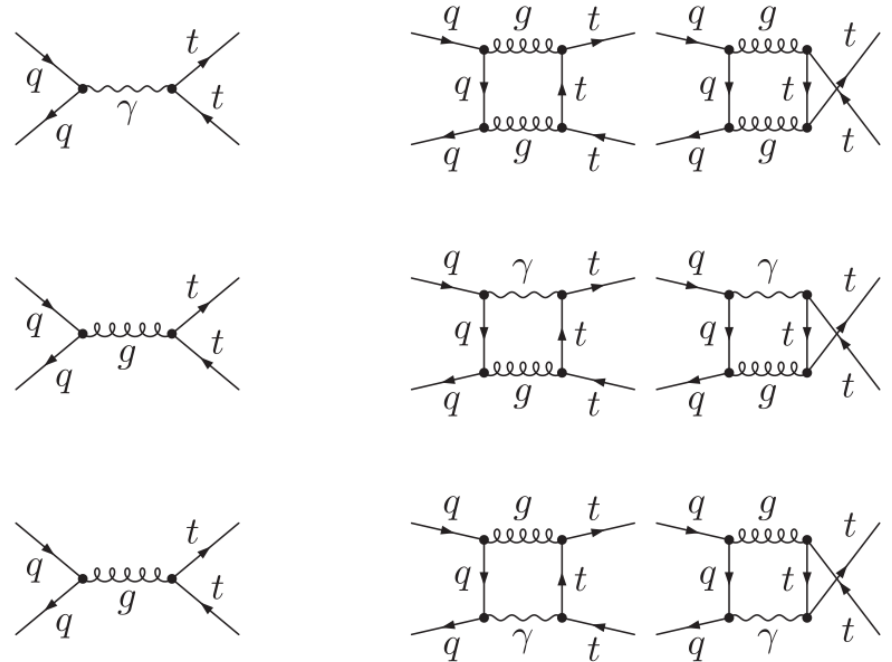
Kuhn & Rodrigo,
PRD 59 (1999) 054017



Only small contributions from quark-gluon scattering

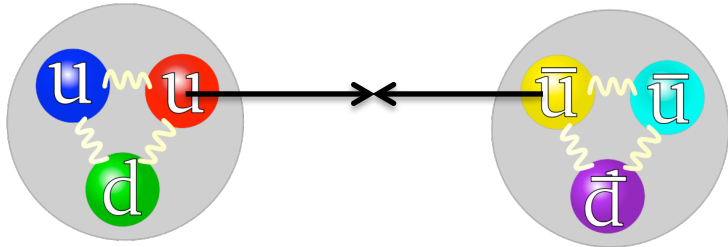


Hollik & Pagani
PRD 84 (2011) 093003

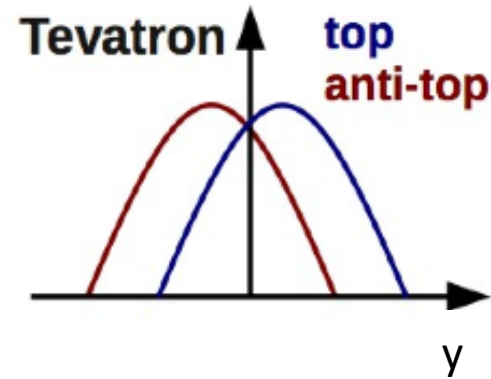


Significant ($\sim 25\%$) contributions from QCD-electroweak interference terms.

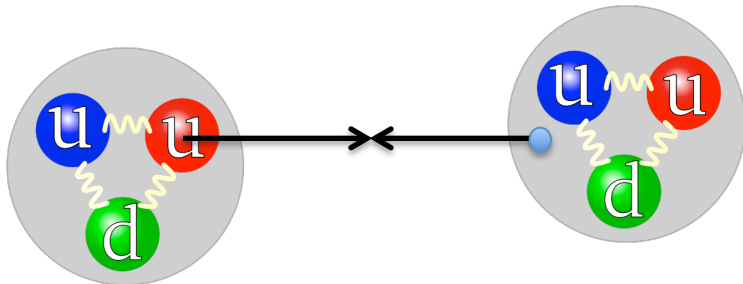
Asymmetry from Interference - $t\bar{t}$



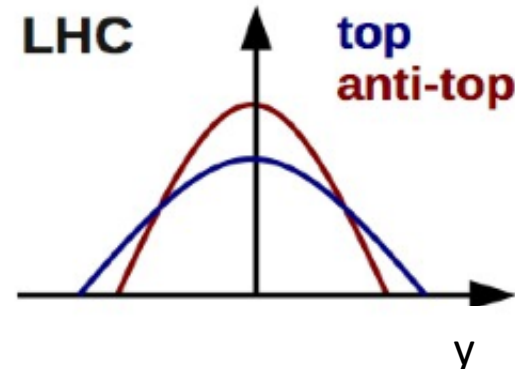
Tevatron: annihilation of two valence quarks (PDF symmetric).



Forward-backward asymmetry (A_{FB})



LHC: annihilation of one valence and a sea anti-quark (PDF asymmetric) and **moreover gluon fusion dominates.**
→ much smaller asymmetry.

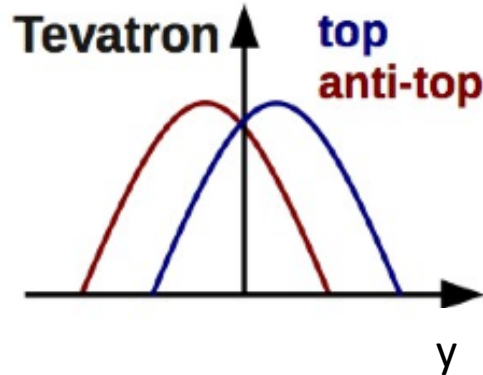


Charge asymmetry (A_C)

On average, $P(\text{valence quark}) > P(\text{sea anti-quark})$
→ top quark rapidity broader than the anti-quark rapidity

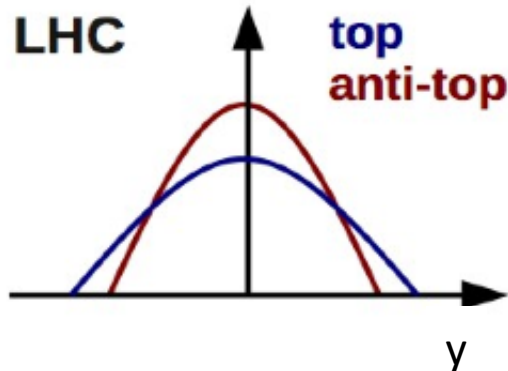
→ any large asymmetry will indicate the existence of new physics.

Asymmetry from Interference - $t\bar{t}$



Forward-backward asymmetry (A_{FB})

$$A_{FB} = \frac{N(\Delta y > 0) - N(\Delta y < 0)}{N(\Delta y > 0) + N(\Delta y < 0)}, \quad \Delta y = y_t - y_{\bar{t}}$$

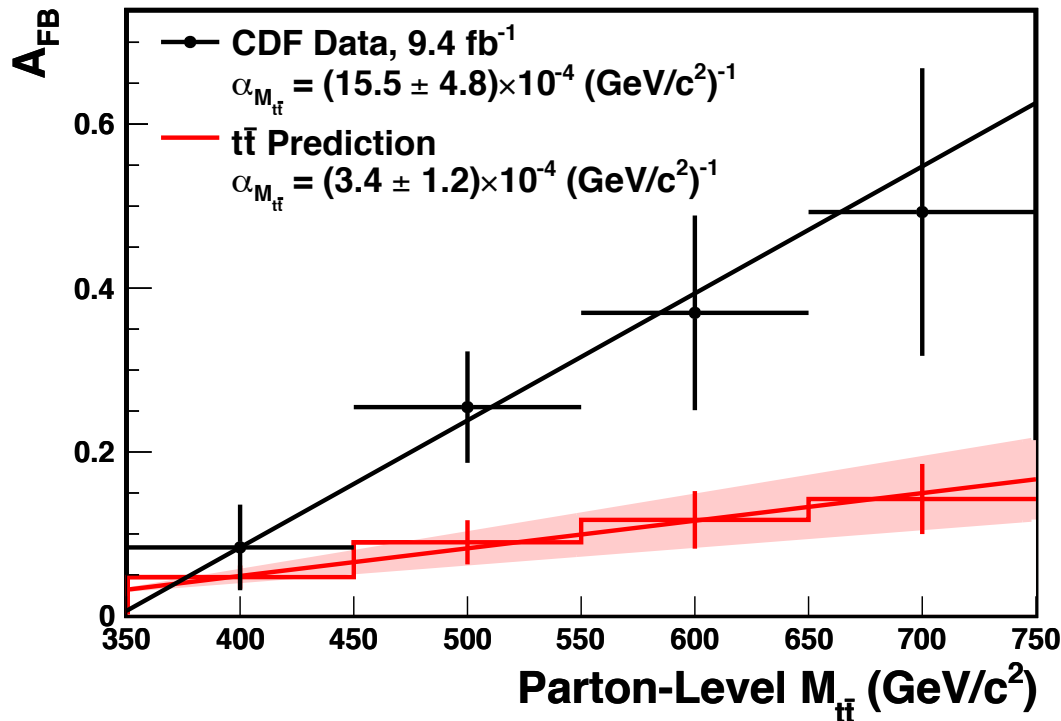


Charge asymmetry (A_C)

$$A_{FB} = \frac{N(\Delta |y| > 0) - N(\Delta |y| < 0)}{N(\Delta |y| > 0) + N(\Delta |y| < 0)}, \quad \Delta |y| = |y_t| - |y_{\bar{t}}|$$

$t\bar{t}$ Asymmetry at the Tevatron: Deviations from SM

First Reported in 2009 by CDF and D0



arXiv:1211.1003
PRD 87, 092002 (2013)

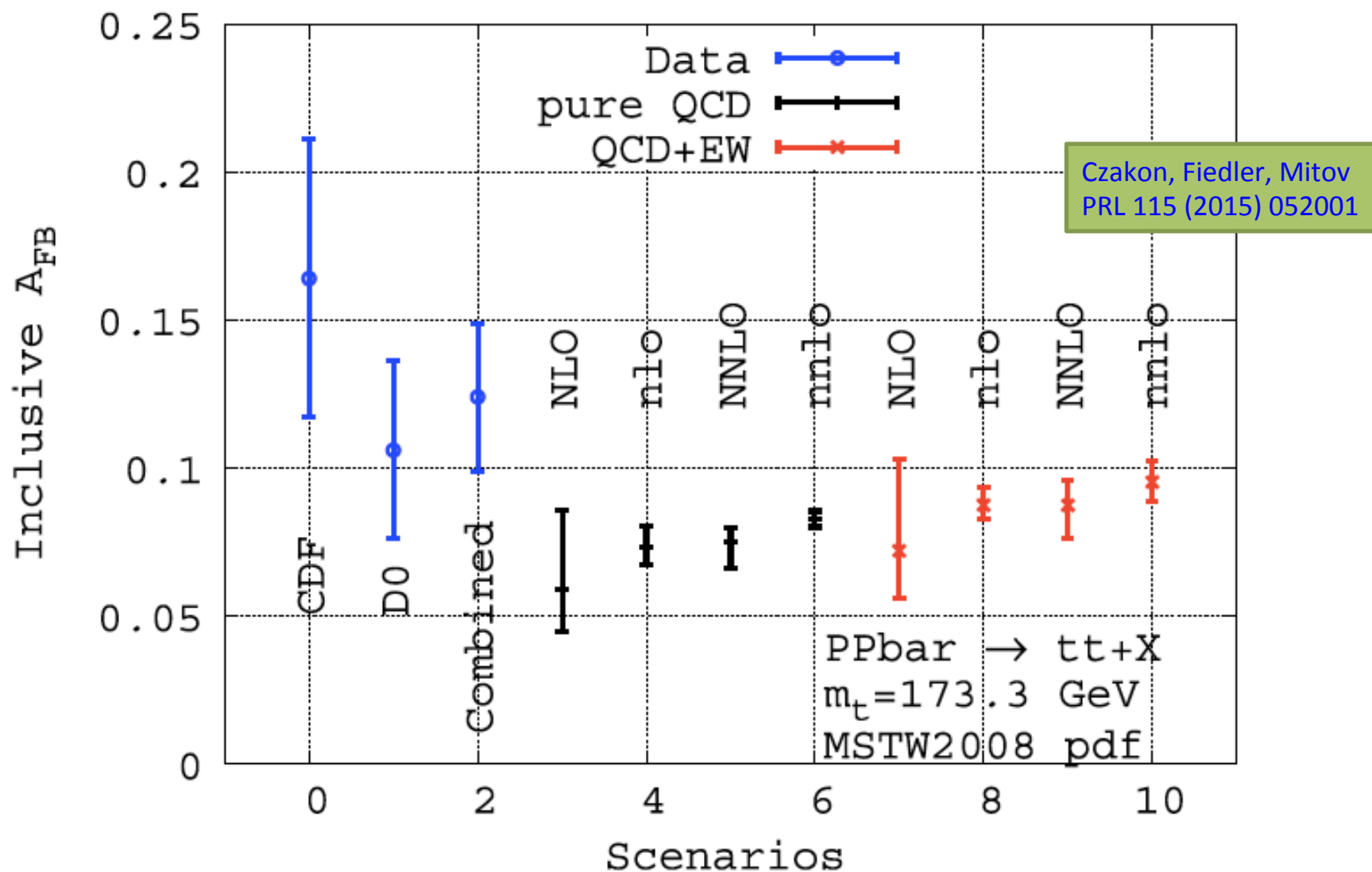
Inclusive A_{FB} : $\sim 2\sigma$ deviation
 $A_{FB}(m_{t\bar{t}} > 450 \text{ GeV})$: $\sim 3\sigma$

- Statistical fluctuation?
 - ◆ results dominated by statistical uncertainties
- Missing theory effect?
 - ◆ calculations were only at the lowest order
- Mistake in the measurement method?
- Missing uncertainties?

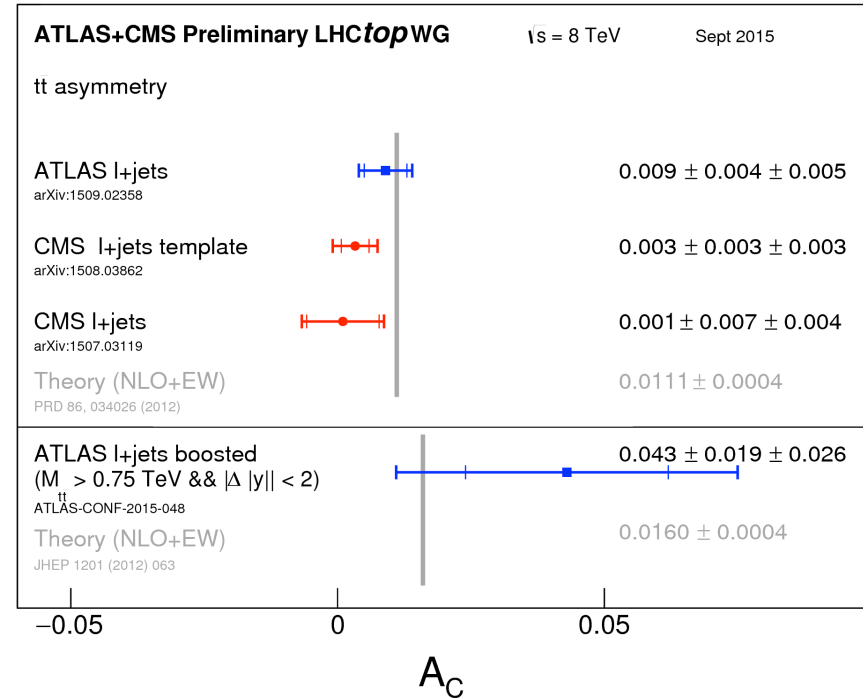
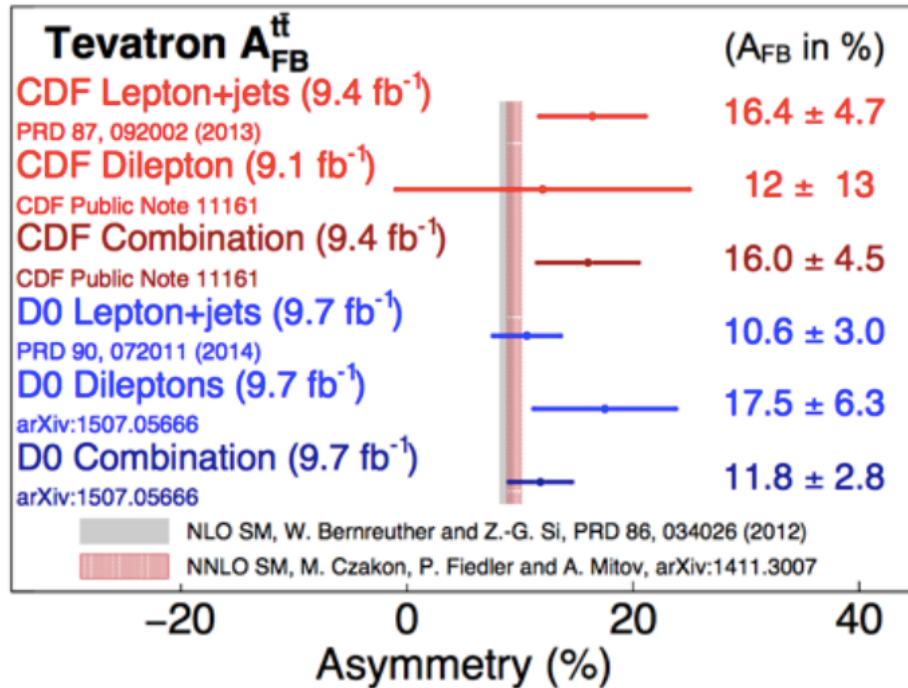
→ If none,
may be new physics?

(but > 100 papers with
New physics interpretation)

tt Asymmetry at the Tevatron @ 2015

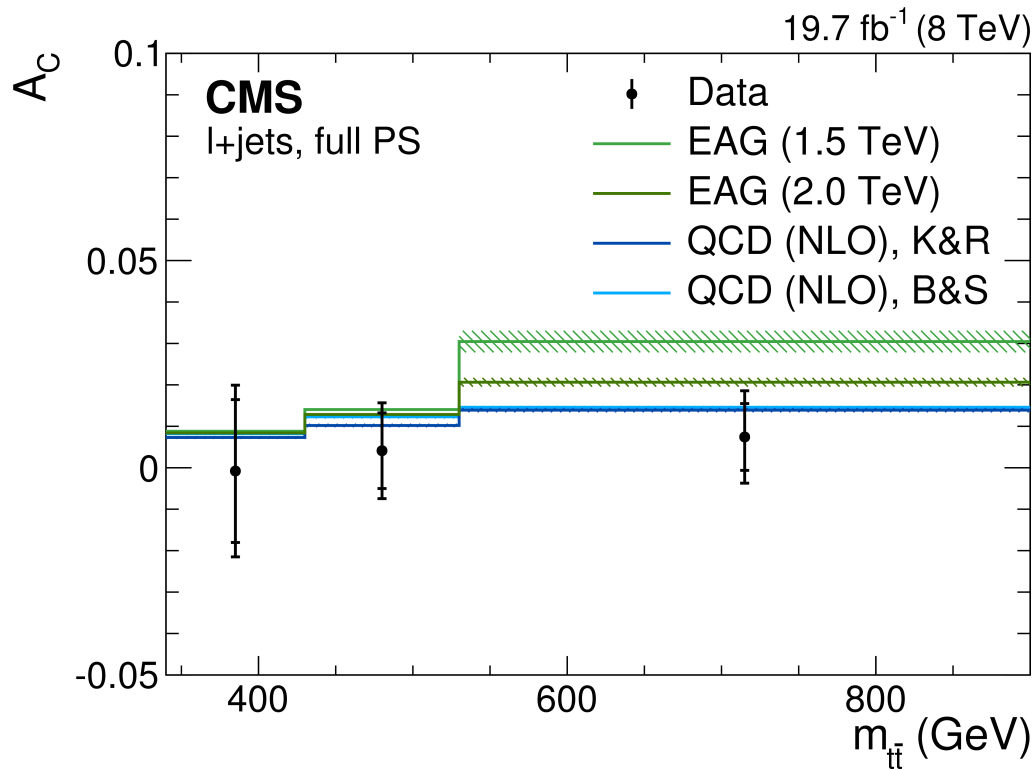


$t\bar{t}$ Asymmetry at the Tevatron and LHC



- $b\bar{b}$ asymmetry measurements consistent with LO predictions (LHCb arXiv:1406.4789).

$t\bar{t}$ Asymmetry at the LHC

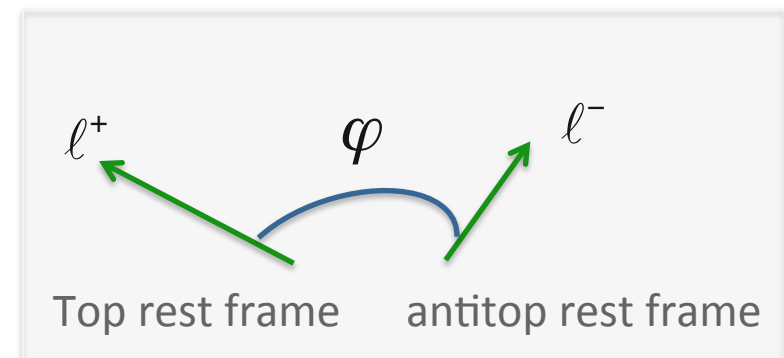
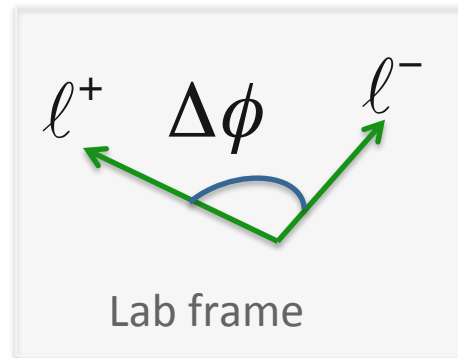
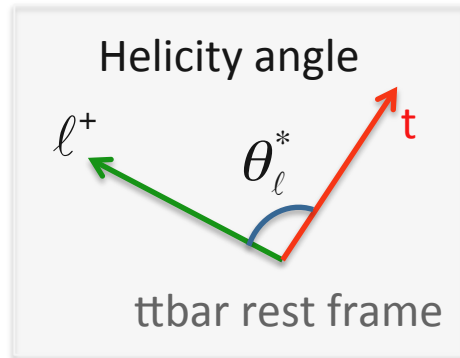


arXiv:1507.03119

- $M > \sim 450$ GeV, $A_C \sim 2\sigma$ below predictions from EFT with new physics scale of 1.5 TeV.

$t\bar{t}$ production: Tops are unpolarized but heavy quark spins are correlated

Angles with or without top quark reconstruction:

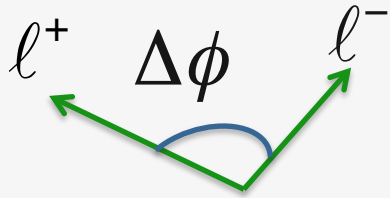


Or a multivariate method using more information from the events; e.g. Matrix Element Method:

$$P(x_i|H) = \frac{1}{\sigma_{obs}} \int f_{PDF}(q_1) f_{PDF}(q_2) dq_1 dq_2 \frac{(2\pi)^4 |M(y, H)|^2}{q_1 q_2 s} W(x, y) d\Phi_6$$

Top Quark Spin Correlations - Dilepton Channel

PRD 93 (2016) 052007

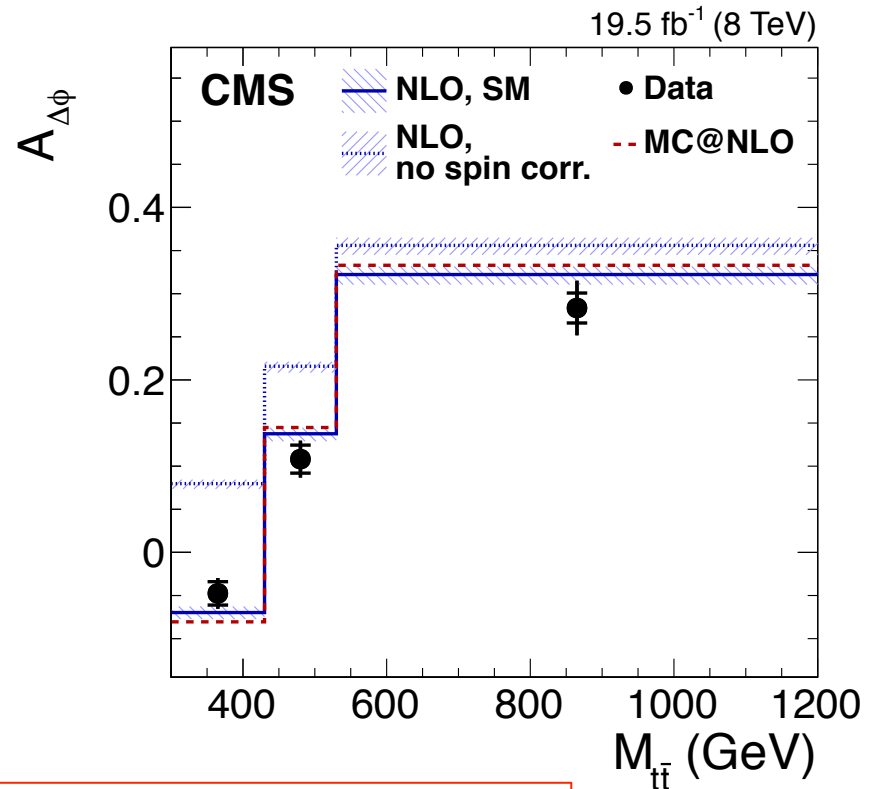
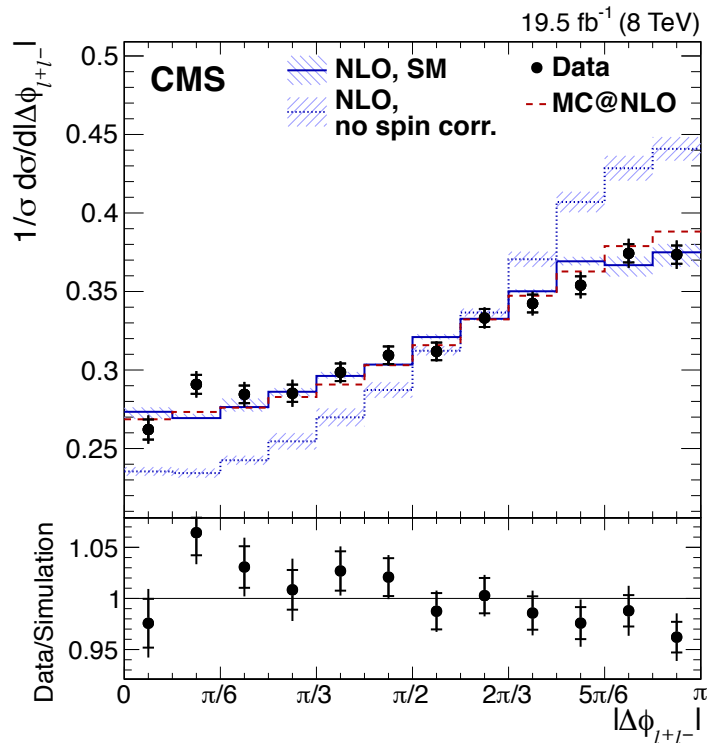


Lab frame

$\Delta\phi$ distribution becomes flatter when tops are correlated.

$$A_{\Delta\phi} = \frac{N(|\Delta\phi_{\ell^+\ell^-}| > \pi/2) - N(|\Delta\phi_{\ell^+\ell^-}| < \pi/2)}{N(|\Delta\phi_{\ell^+\ell^-}| > \pi/2) + N(|\Delta\phi_{\ell^+\ell^-}| < \pi/2)}$$

$$f \equiv \frac{N_{SM}}{N_{SM} + N_{non-SM}}, \quad f_{SM} = 1$$

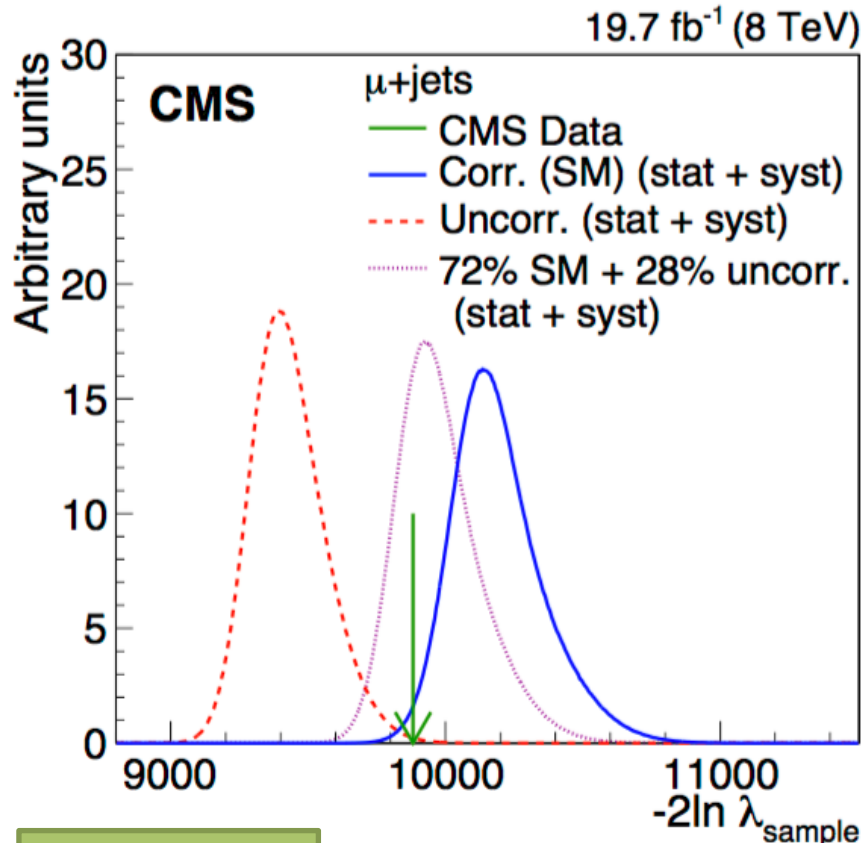


$$f_{SM} \left(\text{from } A_{\Delta\phi} \text{ vs } M_{t\bar{t}} \right) = 1.12 \pm 0.06 (stat) \pm 0.08 (syst)_{-0.11}^{+0.08} (theor)$$

$t\bar{t}$ Spin Correlations – Lepton+Jets Channel

Leading order ME method to calculate event likelihoods for SM and uncorrelated hypotheses (H) using MadWeight [JHEP 12 \(2010\) 068](#)

$$P(x_i|H) = \frac{1}{\sigma_{obs}} \int f_{PDF}(q_1) f_{PDF}(q_2) dq_1 dq_2 \frac{(2\pi)^4 |M(y, H)|^2}{q_1 q_2 s} W(x, y) d\Phi_6$$



$$\rightarrow -2 \ln \lambda = -2 \ln \frac{P(H_{non-SM})}{P(H_{SM})}$$

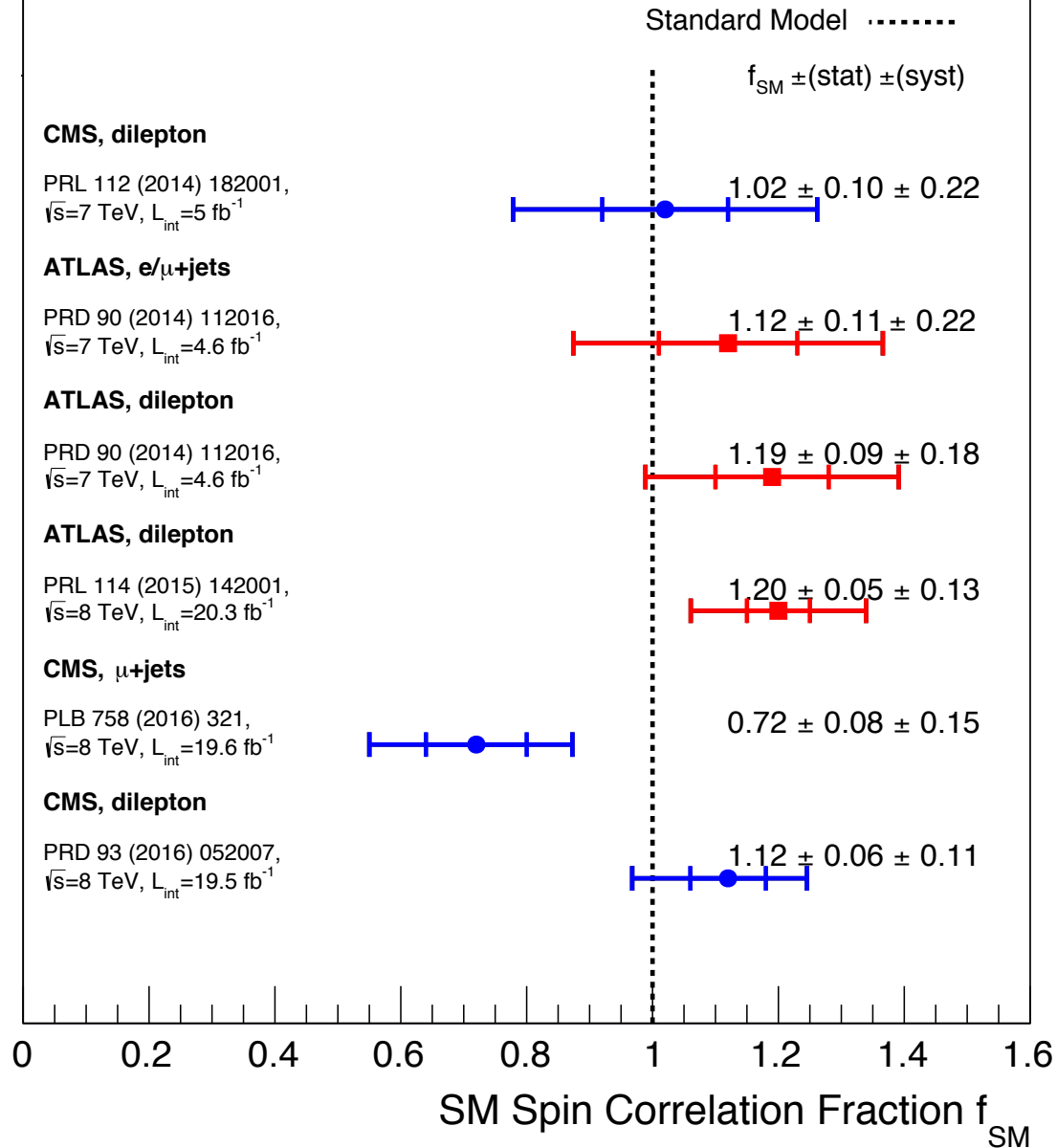
$$f = 0.72 \pm 0.08 (stat)^{+0.15}_{-0.13} (syst)$$

Most precise result in
l+jets to-date

Dominated by:
JES, QCD scale, top quark mass

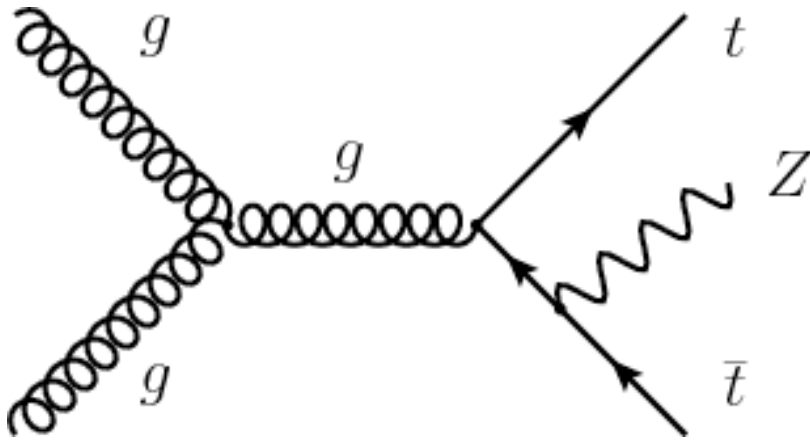
$t\bar{t}$ Spin Correlation Measurements Summary

May 2016

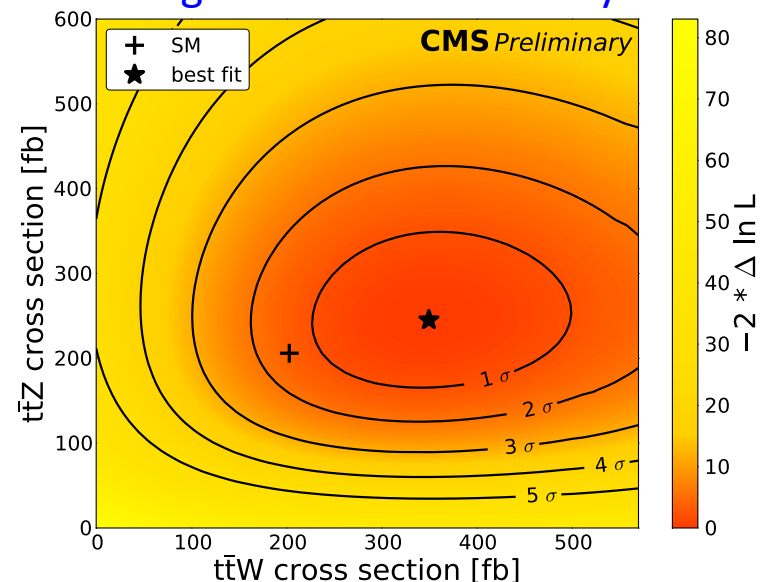


Top Quark Couplings

- $t\bar{t}Z$ and $t\bar{t}\gamma$ → Direct access to top-electroweak couplings.
- $t\bar{t}W$ and $t\bar{t}Z$: important backgrounds for top-Higgs coupling measurements.
- $t\bar{t}Z/W$ and $t\bar{t}\gamma$ measured and limits on anomalous couplings, four-top production and $t\bar{t}H$ have been placed at 8 TeV.



Constraints on the axial and vector components of the top-Z coupling using effective field theory.

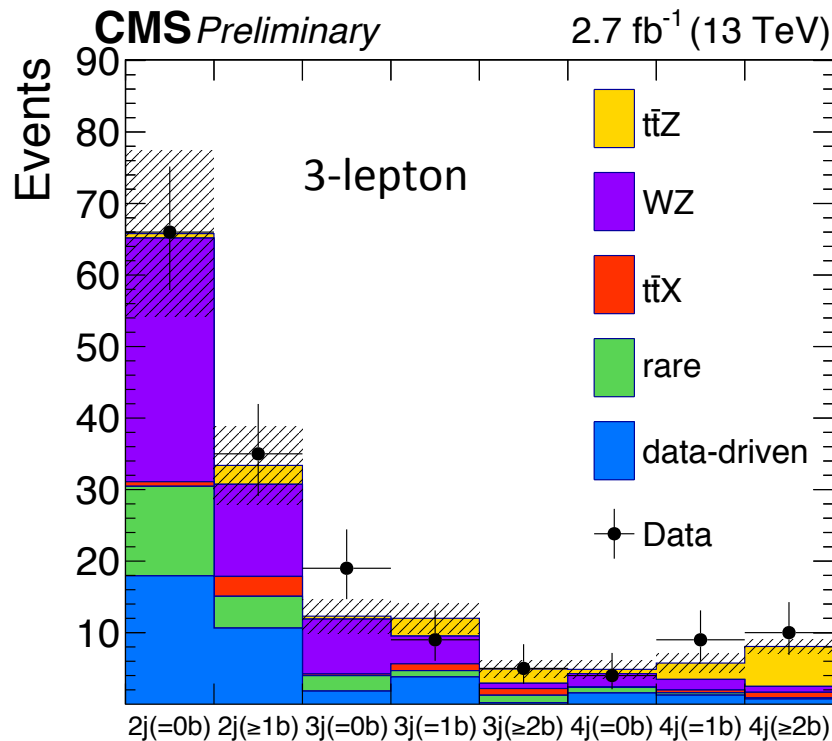


Top Quark Couplings

TOP-16-009

■ Run II:

- ◆ $\sigma(t\bar{t}Z)$ @13 TeV $\rightarrow \sim 4 \times \sigma(t\bar{t}Z)$ @8 TeV
- ◆ $t\bar{t}Z$ cross section from 3-lepton and 4-lepton final states.
- ◆ Exploit jet and b-jet multiplicities to enhance the signal.

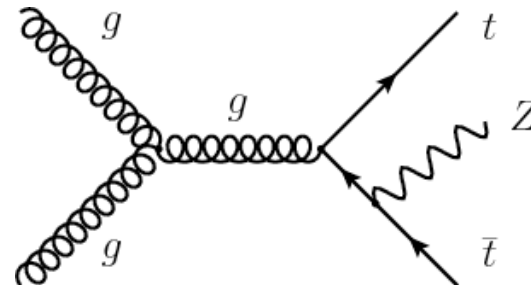


Expected significance: 3.1 SD
Observed significance: 3.6 SD

$$\sigma_{t\bar{t}Z} = 1065_{-313}^{+352} (stat)_{-142}^{+168} (syst) \text{ fb}$$

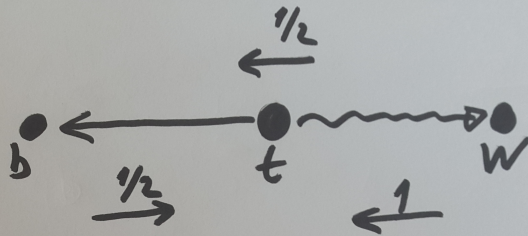
$$\sigma_{t\bar{t}Z}^{NLO} = 839.3_{-92}^{+80} (scale) \pm 25 (pdf) \pm 25 (\alpha_s) \text{ fb}$$

Frixione et al. arXiv:1504.03446; Alwall et al. arXiv:1405.0301

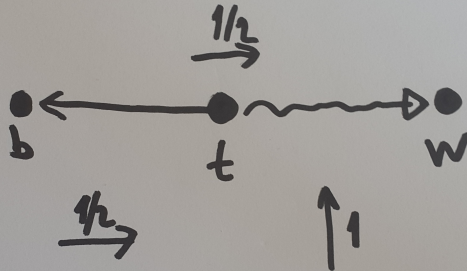


W Boson Polarization

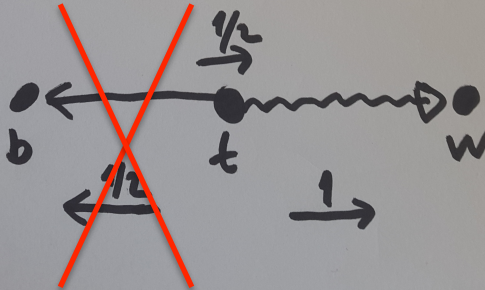
- Wtb vertex $\rightarrow$ electroweak V-A structure.
- W helicity fractions (F_x) sensitive to the Wtb vertex structure.



Left-handed
(negative helicity)



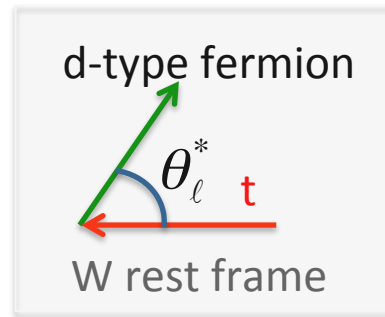
longitudinal
(zero helicity)



Right-handed
(positive helicity)

Massless b -quark always left-handed and top quark left or right handed $\rightarrow$ Angular momentum conservation: Top quark decay to a right-handed W boson is forbidden.

W Boson Polarization



$$\frac{d\sigma}{d\cos\theta^*} \approx \frac{3}{8} (1 - \cos\theta^*)^2 F_L + \frac{3}{4} (\sin\theta^*)^2 F_0 + \frac{3}{8} (1 + \cos\theta^*)^2 F_R$$

$$F_L \sim 0.3$$

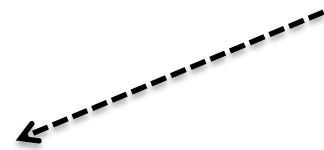
Left-handed
(negative helicity)

$$F_0 \sim 0.7$$

longitudinal
(zero helicity)

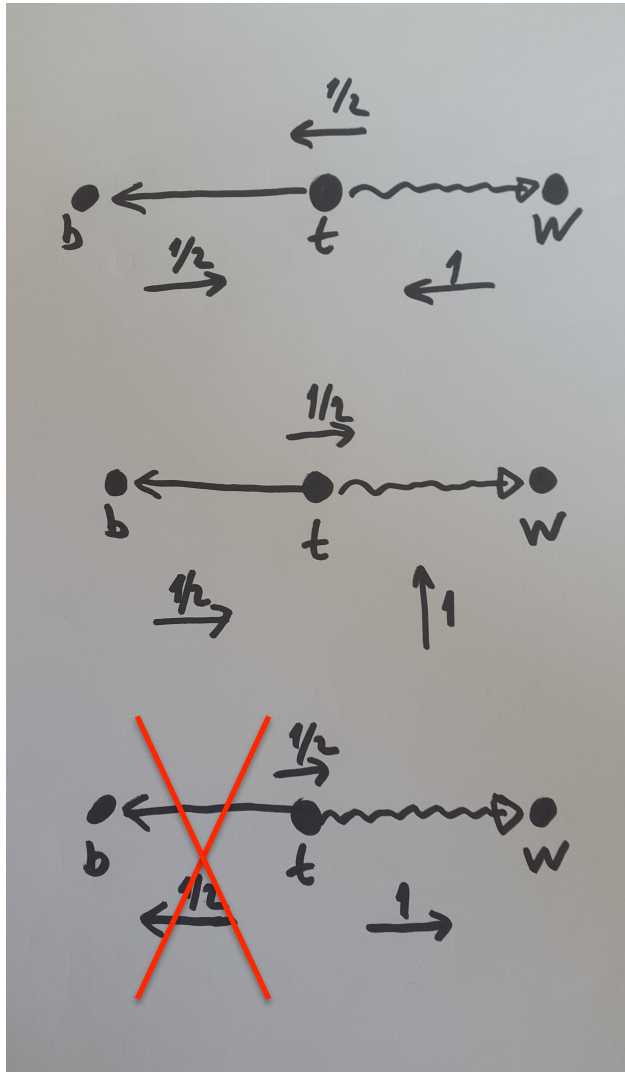
$$F_R \sim 0$$

Right-handed
(positive helicity)



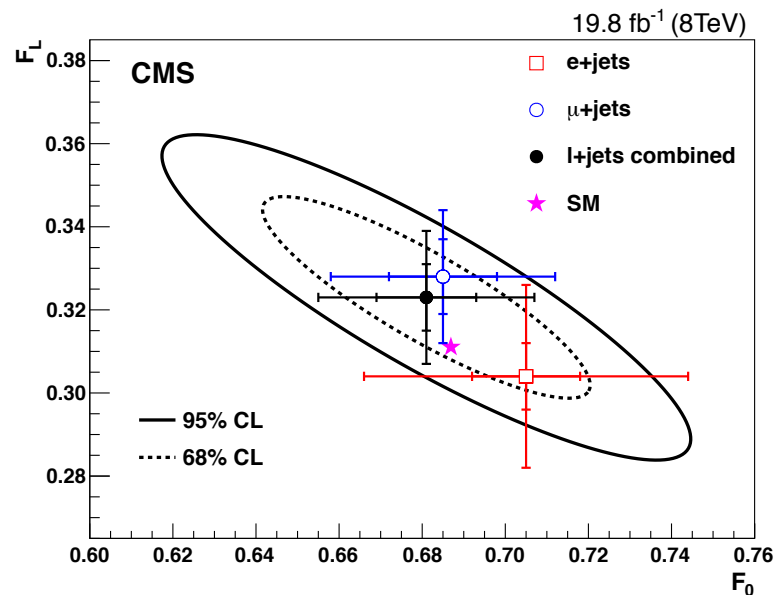
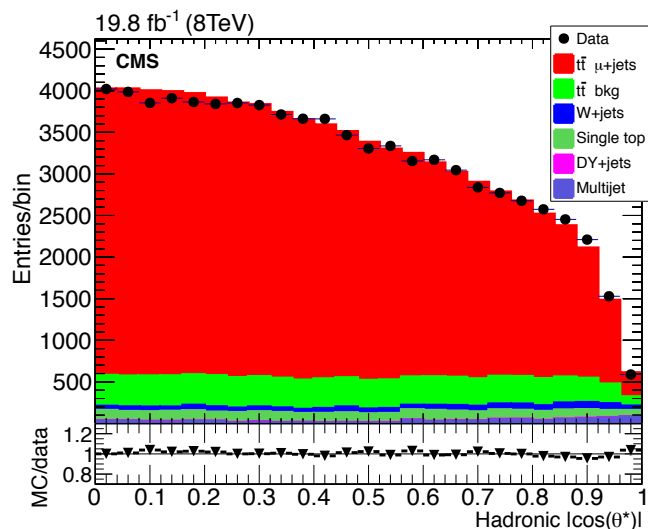
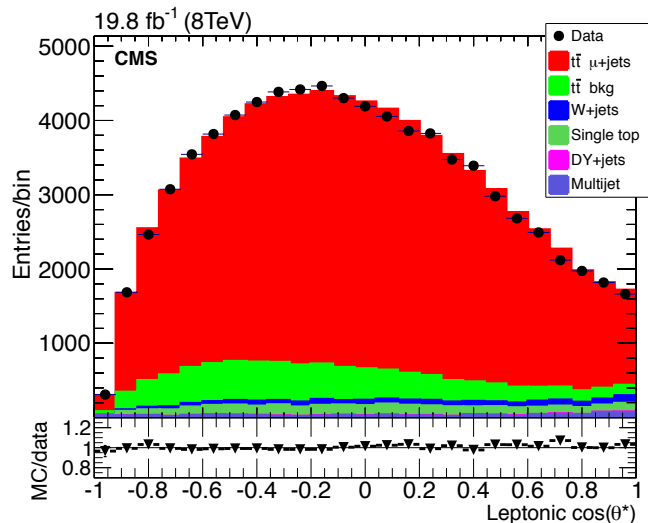
Top quark prefers to couple more to
longitudinally polarized W bosons.

Higher orders (at NNLO QCD) with $m_b \neq 0$ modify the helicity
fractions by $\sim 2\%$.



W Boson Polarization

$e/\mu + 4 \text{ jets (2 b-tagged)}$



$$F_0 = 0.681 \pm 0.012(stat) \pm 0.023(syst)$$

$$F_L = 0.323 \pm 0.008(stat) \pm 0.014(syst)$$

$$F_R = -0.004 \pm 0.005(stat) \pm 0.014(syst)$$

Dominant uncertainties: Top quark mass and QCD scales.

Most precise measurement of helicity fractions to date.

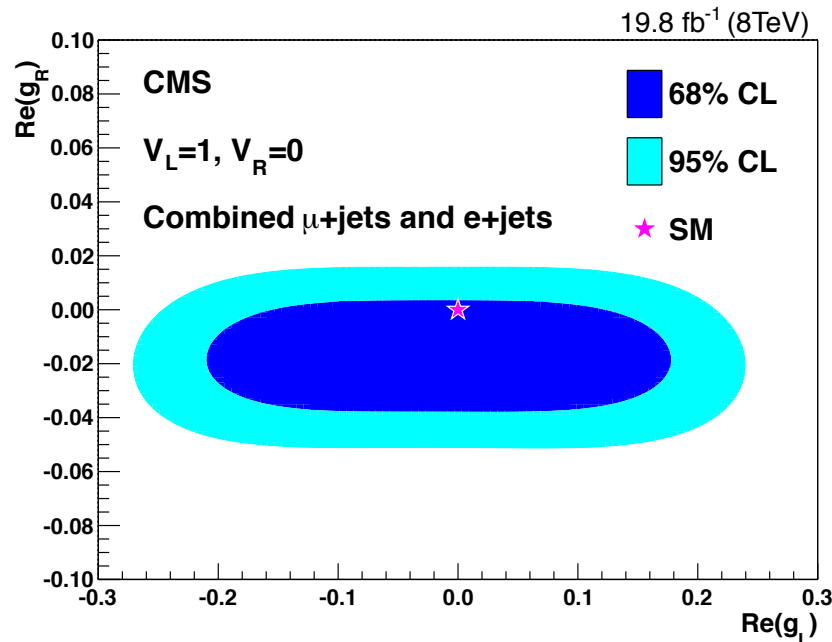
W Boson Polarization

- Wtb : magnitude determined by $|V_{tb}|$.
- BSM contributions to Wtb vertex modify helicity fractions.
- In the effective operative framework:

$$\mathcal{L}_{Wtb} = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu (V_L P_L + V_R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (g_L P_L + g_R P_R) t W_\mu^- + \text{h.c.}$$

$$SM : V_L = V_{tb} \approx 1$$

$$V_R = g_L = g_R = 0$$



*CMS-PAPER-TOP-13-008,
 submitted to PLB*

Summary

- Top quark plays an important role in precision measurements and new particles searches.
- Top re-discovered at the LHC.
- Most LHC Run I measurements dominated by systematic uncertainties.
 - ◆ $\sigma_{tt} < 4\%$ better than NNLO accuracy
 - ◆ m_t with ~ 500 MeV precision.
 - ◆ Precise properties measurements and constraints on anomalous couplings.
- So far, all results in agreement with SM predictions.
 - ◆ And no evidence of any invisible particles.

LHC Run II

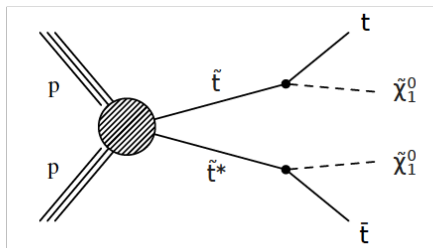
- Inclusive $t\bar{t}$ cross section already at NNLO precision.
- Single top t-channel precisely established.
- In both cases starting to probe differential spectra to understand new MCs
- Establish couplings to all bosons in Run II.
- Direct or indirect indications of new physics?

QUESTIONS

BONUS

Top Squark Pair Production

arXiv:1603.02303



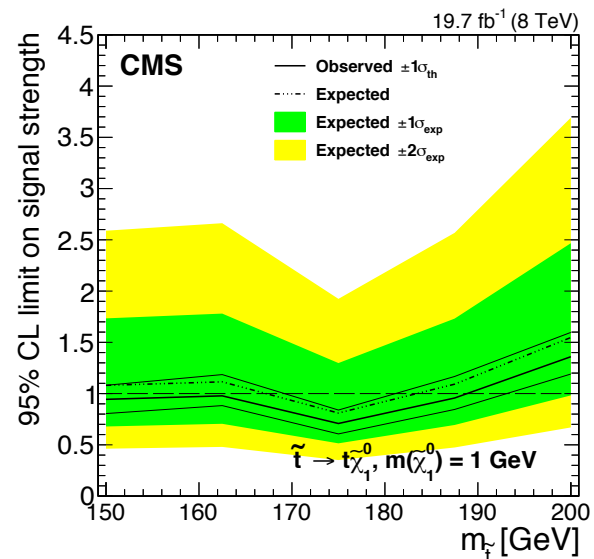
$$m(\tilde{t}) \approx m(\tilde{\chi}_1^0) + m_t \longrightarrow \sigma_{t\bar{t}} \text{ (and } t\bar{t} \text{ spin correlations)}$$

more sensitive than standard SUSY searches
for low $m(\tilde{\chi}_1^0)$ and $m(\tilde{t}) \approx m_t$

$\tilde{t}\tilde{t}^*$ production, $\tilde{t} \rightarrow t \tilde{\chi}_1^0 / c \tilde{\chi}_1^0$

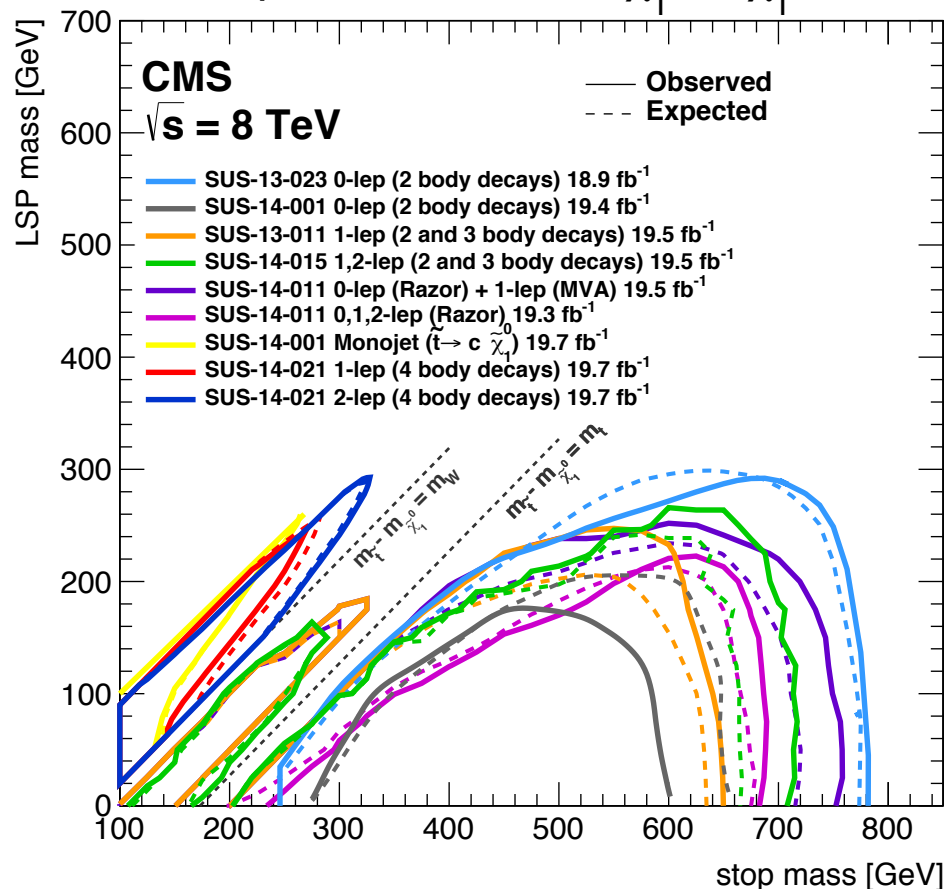
Simplified model with two parameters:

$$m(\tilde{t}), m(\tilde{\chi}_1^0)$$



$$m(\tilde{t}; \tilde{\chi}_1^0 = 1 \text{ GeV}) > 189 \text{ GeV}$$

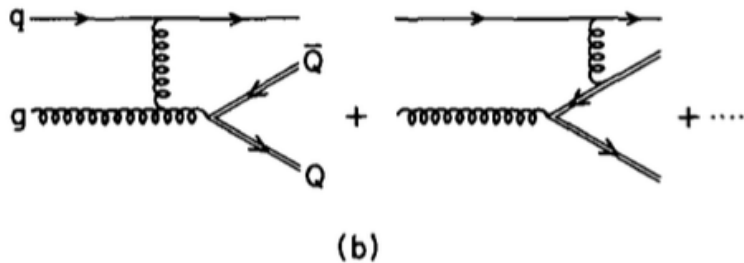
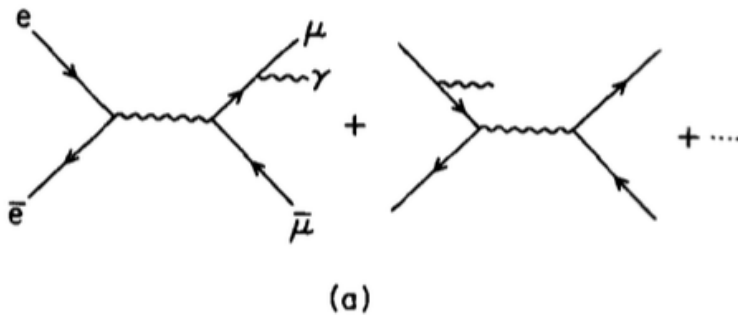
$$m(\tilde{t}; \tilde{\chi}_1^0) \notin 185 - 189 \text{ GeV}$$



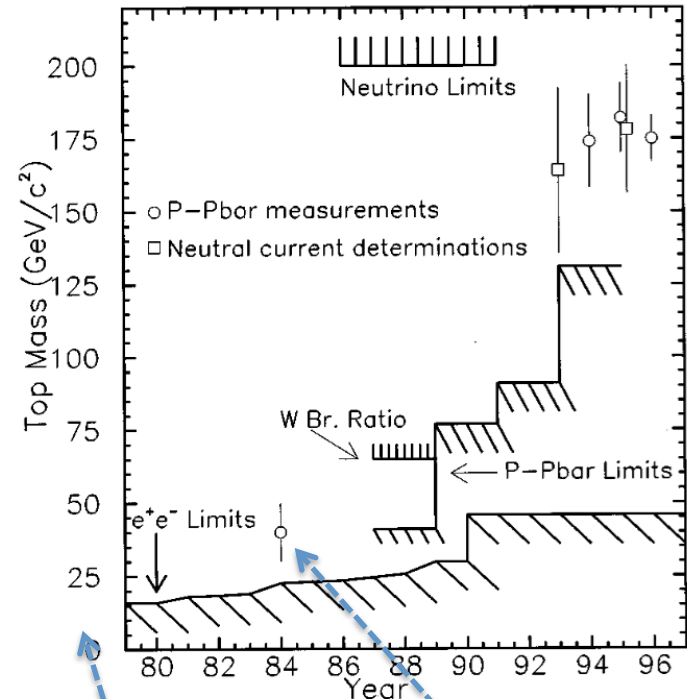
Asymmetry from Interference - $t\bar{t}$

- First calculation of asymmetry by Halzen et al. 1987 (PLB 195, 74) for $m_t = 45 \text{ GeV}$!
- Making analogy to QED.
- But considered only real gluon emission.

$$q\bar{q} \rightarrow Q\bar{Q}g$$



$$qg \rightarrow Q\bar{Q}q$$



Campagnari & Franklin
Rev. Mod. Phys. 69, 137 (1997)

Example predictions of m_t :

→ 5-65 GeV

(J. Ellis, et. al. NPB 131 (1977) 285)

→ 16-19 GeV

(T. Yanagida, PRD 20 (1979) 2986)

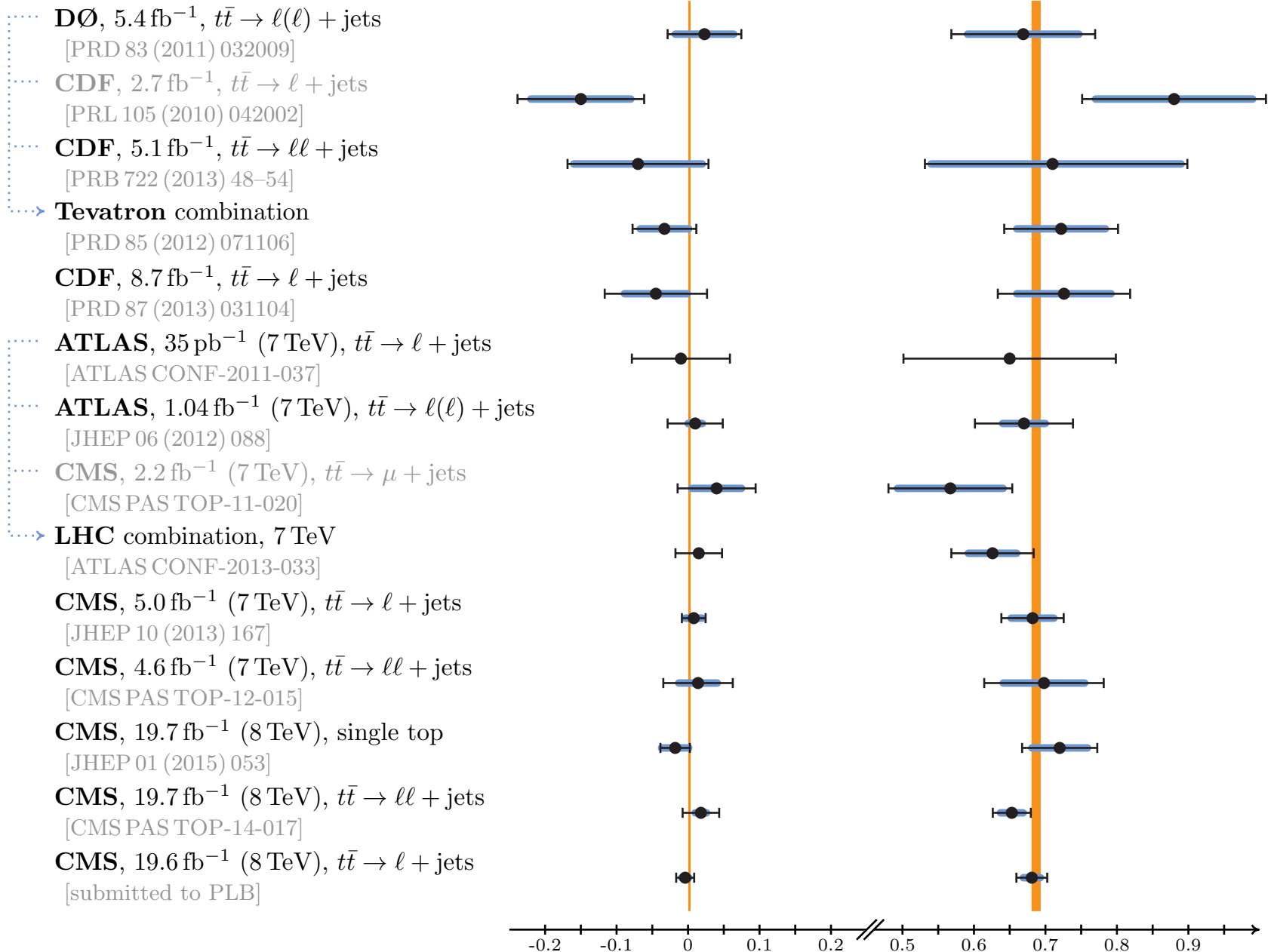
→ ~148 GeV

(H. Terazawa, PRD 22 (1980) 2921)

1984 UA1 measurement
 $m_t = 40 \pm 10 \text{ GeV}$.

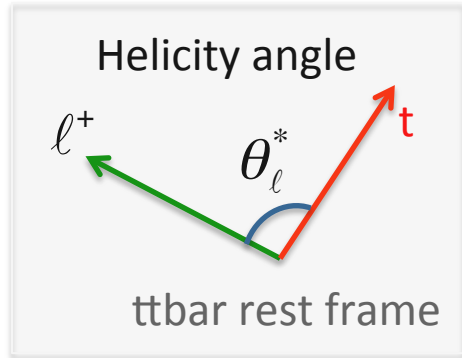
— SM expectations [PRD 81 (2010) 111503]

Uncertainty: $\blacksquare$ total, $\blacksquare$ stat. only



Top Quark Polarization in $t\bar{t}$ Dilepton Channel

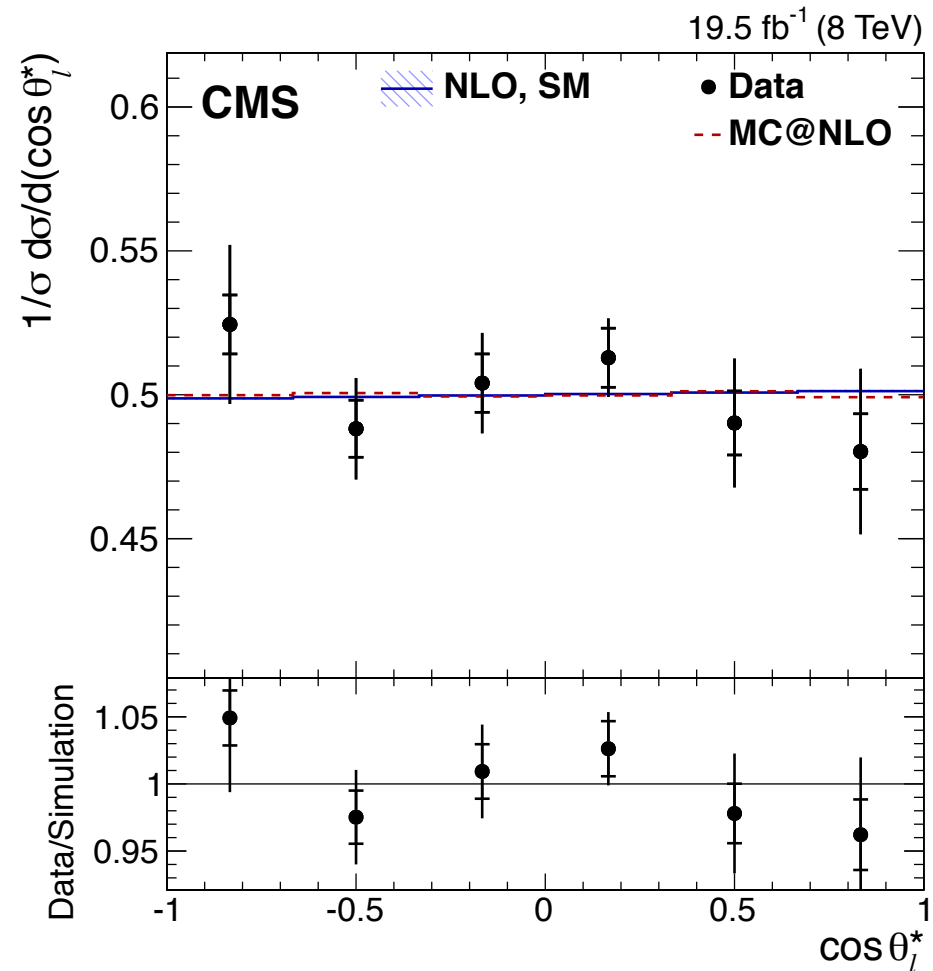
PRD 93 (2016) 052007



$$\frac{1}{2}P^\pm = A_{P^\pm} = \frac{N(\cos\theta_{\ell^\pm}^* > 0) - N(\cos\theta_{\ell^\pm}^* < 0)}{N(\cos\theta_{\ell^\pm}^* > 0) + N(\cos\theta_{\ell^\pm}^* < 0)}$$

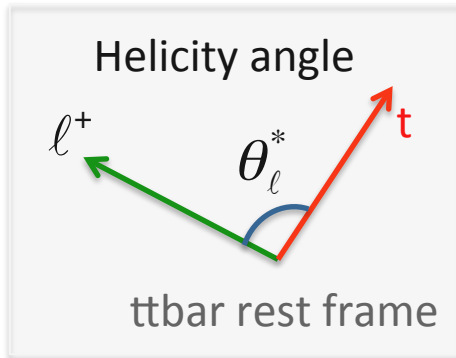
$$P^{SM(CP\text{-conserving})} = (A_{P_+} + A_{P_-}) = -0.022 \pm 0.058$$

$$P^{CP\text{-violating}} = (A_{P_+} - A_{P_-}) = 0.000 \pm 0.016$$



Top Quark Spin Correlation in Dilepton Channel

PRD 93 (2016) 052007



$$\frac{d^2\sigma}{d\cos\theta_+ d\cos\theta_-} = \frac{\sigma}{4} (1 + \alpha_+ P_+ \cos\theta_+ + \alpha_- P_- \cos\theta_- + A\alpha_+ \alpha_- \cos\theta_+ \cos\theta_-)$$

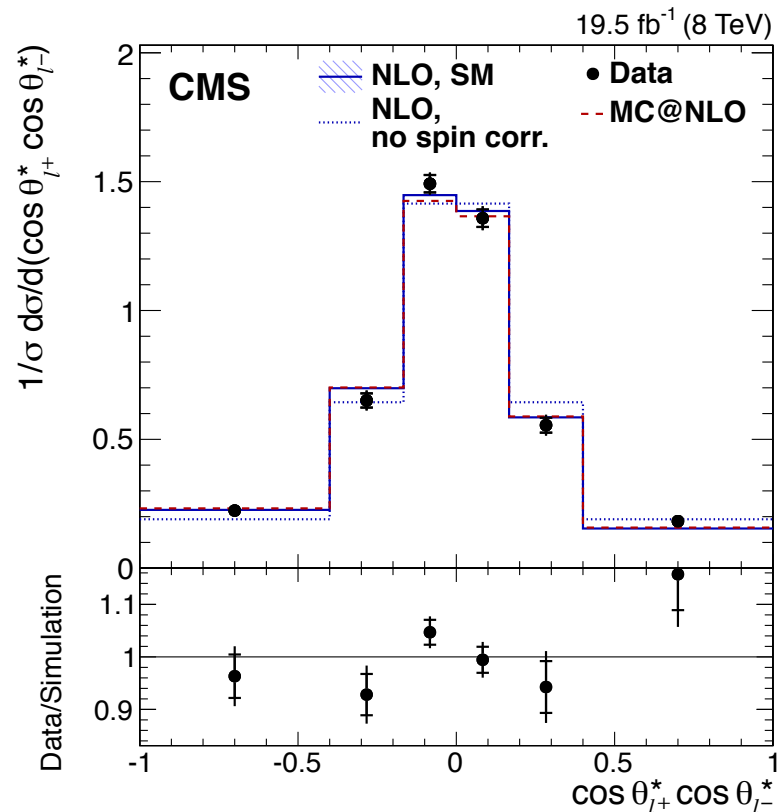
$$A_{c_1 c_2} = \frac{N(c_1 c_2 > 0) - N(c_1 c_2 < 0)}{N(c_1 c_2 > 0) + N(c_1 c_2 < 0)}$$

$$c_1 = \cos\theta_{\ell^+}^* \quad C_{hel} = -4A_{c_1 c_2}$$

$$c_2 = \cos\theta_{\ell^-}^* \quad (\text{spin correlation coefficient})$$

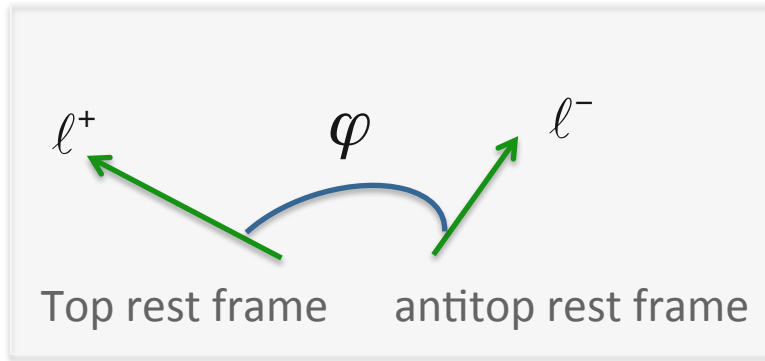
$$f_{c_1 c_2}^{SM} = 0.87 \pm 0.27$$

$$f \equiv \frac{N_{SM}}{N_{SM} + N_{non-SM}}, \quad f_{SM} = 1$$



Top Quark Spin Correlation in Dilepton Channel

PRD 93 (2016) 052007

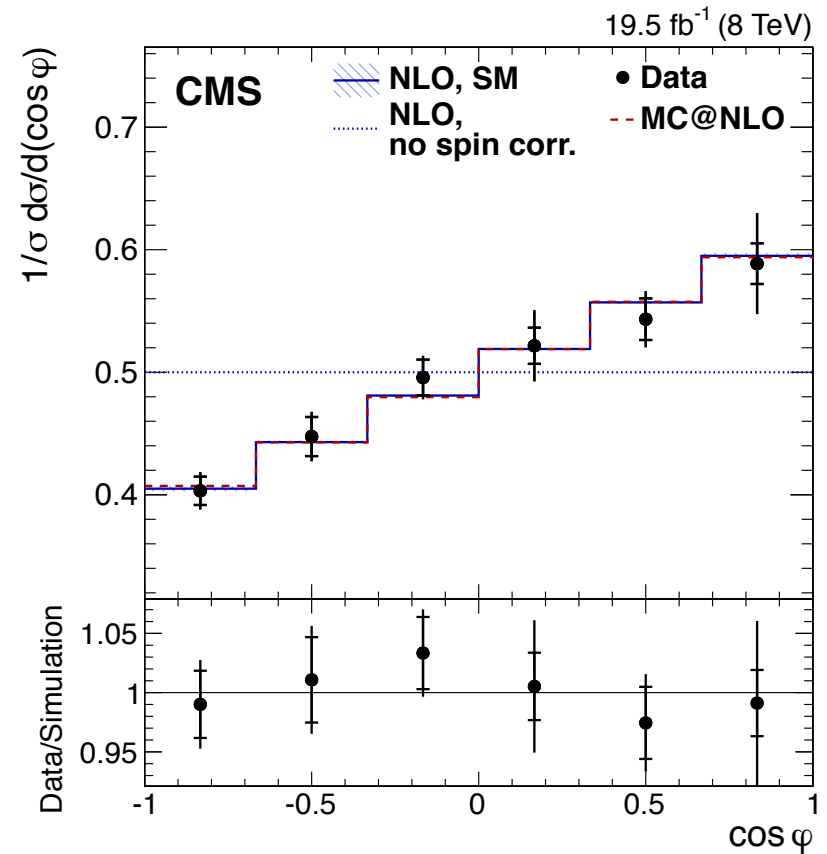


$$A_{\cos\varphi} = \frac{N(\cos\varphi > 0) - N(\cos\varphi < 0)}{N(\cos\varphi > 0) + N(\cos\varphi < 0)}$$

$$D = -2A_{\cos\varphi} \text{ (spin correlation coefficient)}$$

$$f_{\cos\varphi}^{SM} = 0.90 \pm 0.15$$

$$f \equiv \frac{N_{SM}}{N_{SM} + N_{non-SM}}, \quad f_{SM} = 1$$



Anomalous Top-Gluon Interaction

PRD 93 (2016) 052007

- SM: dipole moments generated radiatively and are very small.
- BSM: dipole moment couplings can occur at tree level.

Anomalous interaction from a heavy-particle exchange ($M > m_t$) :

$$\mathcal{L}_{eff} = -\frac{\tilde{\mu}_t}{2} \bar{t} \sigma^{\mu\nu} T^a t G_{\mu\nu}^a - \frac{\tilde{d}_t}{2} i \sigma^{\mu\nu} \gamma_5 T^a t G_{\mu\nu}^a$$

Chromo magnetic dipole moment
CP conserving

$$D = D_{SM} + \text{Re}(\hat{\mu}_t) D_{NP}$$

$$-0.053 < \text{Re}(\hat{\mu}_t) < 0.026 \quad @95\% \text{ C.L.}$$

Chromo electric dipole moment
CP violating

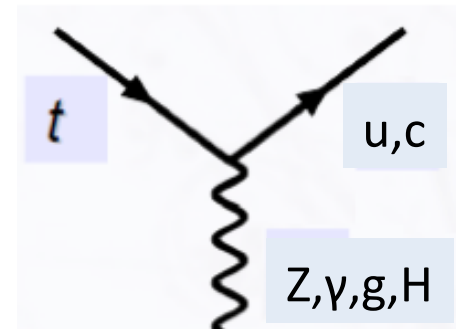
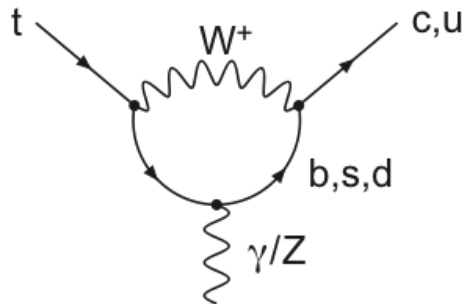
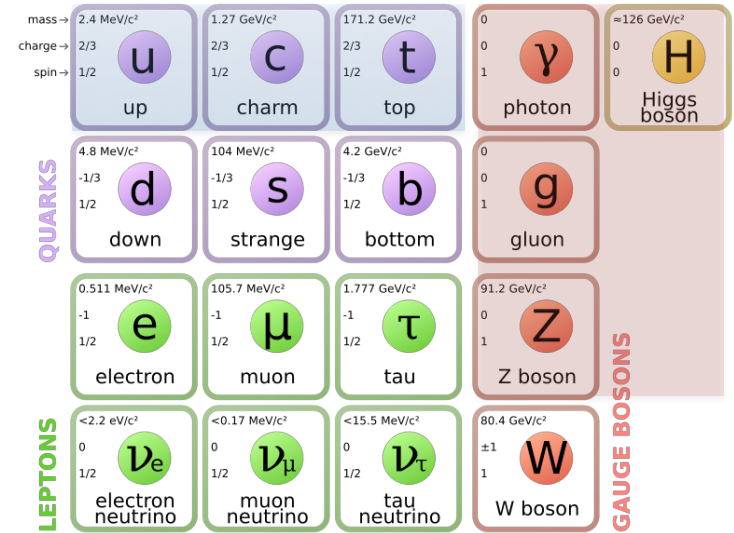
$$P^{CP\text{-violating}} = \text{Im}(\hat{d}_t) P_{NP}^{CP\text{-violating}}$$

$$-0.068 < \text{Im}(\hat{d}_t) < 0.067 \quad @95\% \text{ C.L.}$$

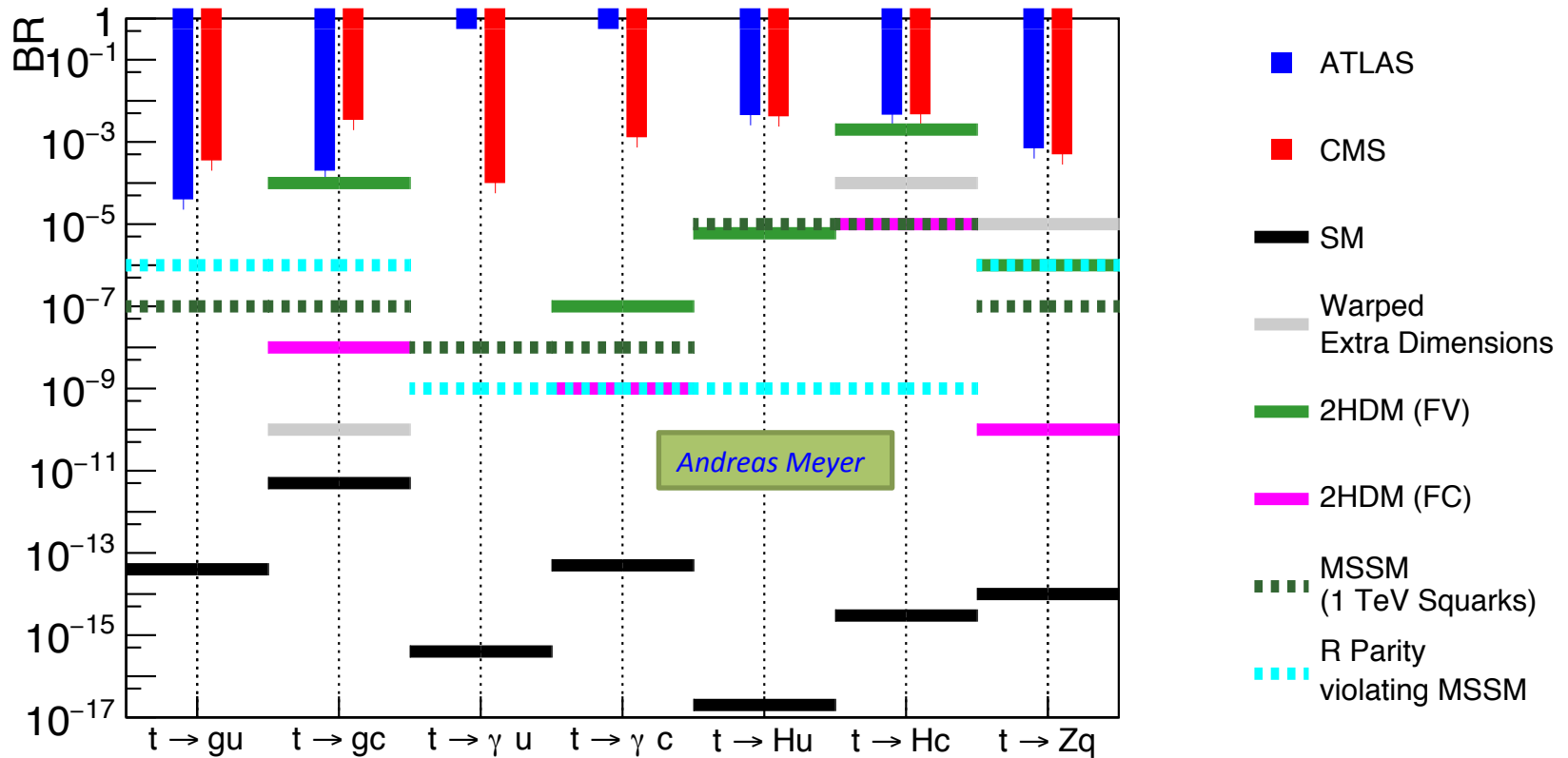
Bernreuther & Si,
PLB 725 (2013) 115
PLB 744 (2015) 413

Flavor Changing Neutral Currents

- SM: Forbidden at tree level
- Suppressed at higher orders due to GIM mechanism.
- Occurs only at the level of loop corrections with
 $\mathcal{B}(t \rightarrow Xq) \sim 10^{-15} - 10^{-10} \%$
- BSM $\mathcal{B}(t \rightarrow Xq) \sim 10^{-7} - 10^{-1} \%$
- Measurements $\sim 10^{-2} - 1 \%$



FCNC vs Data in Some Particular Models



- No sign of FCNC in $t\bar{t}b\bar{a}r$ and single top
- Measurements statistics dominated.